

# Modification of magnetic properties and structure of Kr<sup>+</sup> ion-irradiated CrPt<sub>3</sub> films for planar bit patterned media

T. Kato,<sup>1,a)</sup> S. Iwata,<sup>1</sup> Y. Yamauchi,<sup>2</sup> and S. Tsunashima<sup>2</sup>

<sup>1</sup>*Department of Quantum Engineering, Nagoya University, Furo-cho, Chikusa-ku, Nagoya, Aichi 464-8603, Japan*

<sup>2</sup>*Department of Electrical Engineering and Computer Science, Nagoya University, Furo-cho, Chikusa-ku, Nagoya, Aichi 464-8603, Japan*

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30 keV Kr<sup>+</sup> ions were irradiated onto L<sub>12</sub> ordered CrPt<sub>3</sub> (20 nm) alloy films fabricated by a magnetron sputtering deposition followed by an appropriate heat treatment, and the modification of the structure and magnetic properties of the CrPt<sub>3</sub> films was investigated in detail. The fabricated L<sub>12</sub> CrPt<sub>3</sub> (20 nm) onto a fused quartz substrate exhibited a quite large perpendicular anisotropy of  $5 \times 10^6$  ergs/cc, due to the large lattice distortion of 1%. The large perpendicular anisotropy decreased with increasing the ion dose, and became almost zero at the ion dose of  $2 \times 10^{14}$  ions/cm<sup>2</sup> due to the loss of the magnetic order of CrPt<sub>3</sub>. The suppression of the magnetic order of CrPt<sub>3</sub> by the Kr<sup>+</sup> ion irradiation is attributed to the transformation of the structure from the L<sub>12</sub> phase to a disordered fcc phase, which was confirmed by x-ray diffraction analysis. Unlike the magnetization and perpendicular anisotropy, the anisotropy field of CrPt<sub>3</sub> does not decrease significantly with the increase in the Kr<sup>+</sup> ion dose, and exhibited more than 20 kOe even at the ion dose of  $1 \times 10^{14}$  ions/cm<sup>2</sup>. This is considered to be attributed that the lattice distortion of CrPt<sub>3</sub> unchanged even at the Kr<sup>+</sup> ion dose of  $2 \times 10^{14}$  ions/cm<sup>2</sup>. © 2009 American Institute of Physics. [doi:10.1063/1.3212967]

## I. INTRODUCTION

Bit patterned media have attracted considerable interest as future high density magnetic recording media, since they provide a promising technology to postpone the problem of superparamagnetic limit, i.e., thermal instability of the recorded bits in the media. One of the problems for the practical use of the bit patterned media is topography of discrete magnetic bits defined by lithographical fabrication, because the rough surface of the disk disturbs stable flying of the hard disk drive (HDD) head. Ion-beam irradiation has been proposed as a new approach to pattern magnetic materials locally without etching magnetic materials, i.e., without altering the surface topography,<sup>1,2</sup> and ion irradiation into Co/Pt,<sup>1-4</sup> Co/Pd,<sup>5,6</sup> and Co/Au<sup>7,8</sup> multilayers (MLs) has been reported for the modification of their perpendicular anisotropies. However, in the Co/Pt, Co/Pd, and Co/Au MLs patterned by ion irradiation, the adjacent magnetic bits are not magnetically isolated due to the exchange coupling through in-plane magnetized spacing, which will limit the ultimate density of the media.

Previously, we have reported the ion-beam patterned medium using a CrPt<sub>3</sub> alloy film.<sup>9</sup> The CrPt<sub>3</sub> shows ferrimagnetism when it has an ordered L<sub>12</sub> phase, while paramagnetism when it has a disordered fcc phase, and Hellwig *et al.*<sup>10</sup> reported that 700 keV N<sup>+</sup> ion irradiation can destroy the ferrimagnetism of CrPt<sub>3</sub>. However, such high-energy and low-mass ion irradiation is not practical for fabrication of nanopatterned media due to the deep ion penetration depth (~500 nm).<sup>11</sup> Thus we have reported the Kr<sup>+</sup> or Ar<sup>+</sup> ion

irradiation onto CrPt<sub>3</sub>, and presented the read-back signals from a bit patterned CrPt<sub>3</sub> disk fabricated by nanoimprint patterning and ion irradiation.<sup>9</sup>

In this paper, variation of the structure and magnetic properties of CrPt<sub>3</sub> with 30 keV Kr<sup>+</sup> ion irradiation is discussed in detail. In case of high-energy light ion irradiation, initial crystal structure and microstructure (grain size) are known to be maintained,<sup>11</sup> while the heavy ion irradiation may change such structures and surface roughness. The large perpendicular anisotropy of CrPt<sub>3</sub>, which is the most important property as a recording medium, results from the lattice distortion induced in a CrPt<sub>3</sub> film.<sup>12</sup> The structural change due to the Kr<sup>+</sup> ion irradiation may limit the ultimate density of the CrPt<sub>3</sub> bit patterned media. Thus the modification of the structure by the heavy ion irradiation (30 keV Kr<sup>+</sup>) and the associated change in the magnetic properties were investigated.

## II. EXPERIMENTAL METHOD

L<sub>12</sub> phase CrPt<sub>3</sub> films were obtained by postannealing of Cr/Pt MLs. The [Cr(0.4 nm)/Pt(1.5–1.7 nm)]<sub>10</sub> MLs were prepared by alternating sputtering of Cr and Pt. We used fused quartz (SiO<sub>2</sub>) or thermally oxidized (500 nm SiO<sub>2</sub>) silicon as a substrate. The samples were annealed in vacuum ( $<3 \times 10^{-4}$  Pa) at a temperature of 850 °C for 15 min, and then cooled down to room temperature at a rate of about 10 °C/min. 30 keV Kr<sup>+</sup> ions were produced by using ion implantation system and irradiated onto L<sub>12</sub> phase CrPt<sub>3</sub> to suppress its magnetic order. The Kr<sup>+</sup> ion was selected using mass separation electromagnet, and the ion-beam current

<sup>a)</sup>Electronic mail: takeshik@nuee.nagoya-u.ac.jp.

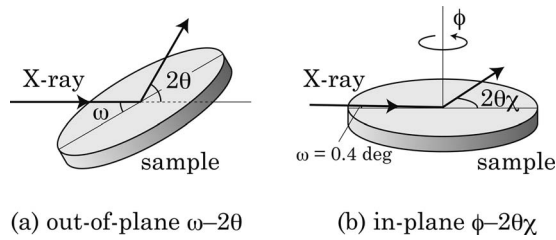


FIG. 1. Schematic drawing of the two types of x-ray scans: (a) out-of-plane  $\omega$ - $2\theta$  scan and (b) in-plane  $\phi$ - $2\theta\chi$  scan. The x-ray incident angle  $\omega$  was set to be  $0.4^\circ$  for the in-plane  $\phi$ - $2\theta\chi$  scan.

density was typically set to be about  $0.25 \mu\text{A}/\text{cm}^2$ . The ion dose into the CrPt<sub>3</sub> film was varied from  $5 \times 10^{12}$  to  $2 \times 10^{15}$  ions/cm<sup>2</sup>.

The film structure was characterized by x-ray diffraction (XRD) with Cu  $K\alpha$  radiation. Two types of scanning were performed to analyze the structure in detail: out-of-plane  $\omega$ - $2\theta$  scan and in-plane  $\phi$ - $2\theta\chi$  scan. The schematic drawing of the two types of x-ray scans is shown in Fig. 1. The diffraction from lattice planes parallel and perpendicular to the film surface was analyzed by  $\omega$ - $2\theta$  and  $\phi$ - $2\theta\chi$  scans, respectively. For the in-plane  $\phi$ - $2\theta\chi$  scan, x-ray incident angle  $\omega$  was set to be  $0.4^\circ$ . Hysteresis loops were measured by using an alternating gradient field magnetometer, and perpendicular anisotropy was estimated by a torque magnetometer applying a maximum field of 15 kOe at temperatures of 300–550 K.

### III. RESULTS AND DISCUSSIONS

Figure 2 shows the temperature dependence of the amplitude of torque curve of a vacuum annealed CrPt<sub>3</sub> (20 nm) ordered alloy film onto a SiO<sub>2</sub> substrate. The torque curves

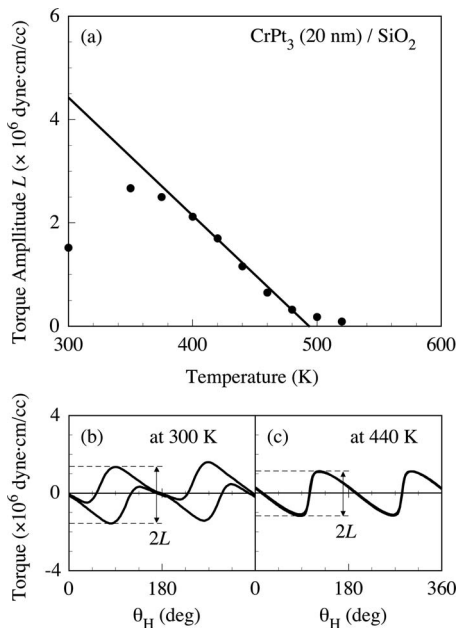


FIG. 2. Temperature dependence of the amplitude of torque curve of a vacuum annealed CrPt<sub>3</sub> (20 nm) ordered alloy film onto a fused quartz (SiO<sub>2</sub>) substrate. The lower two figures (b) and (c) show torque curves taken at 300 and 440 K, respectively. The definition of the torque amplitude  $L$  was illustrated in (b) and (c).

taken at 300 and 440 K are shown in Figs. 2(b) and 2(c), respectively. The definition of the amplitude  $L$  was illustrated in the figures. As previously reported, the CrPt<sub>3</sub> (20 nm) onto SiO<sub>2</sub> exhibits a saturation magnetization  $M_s$  of 250 emu/cc and a large coercivity  $H_c$  of  $>12$  kOe, which are suitable for the application to the perpendicular recording media.<sup>9</sup> However, due to its large perpendicular anisotropy, the anisotropy constant at room temperature cannot be estimated simply by the amplitude of the torque curve because of the insufficient external field to rotate the magnetization (see the torque curve at 300 K). As shown in Fig. 2, the amplitude of the torque curve increased with reducing the temperature from 500 to 400 K, but it starts to decrease with further decrease in the temperature. This is due to the insufficient external field to rotate the magnetization during the torque curve measurement. To roughly estimate the perpendicular anisotropy of CrPt<sub>3</sub> (20 nm) onto SiO<sub>2</sub>, the torque amplitude was extrapolated linearly to room temperature. The uniaxial anisotropy  $K_u$  of typical magnetic recording materials exhibits a nearly linear decrease in  $K_u$  as a function of temperature.<sup>13</sup> Both classical single ion approach<sup>14</sup> and more recent theoretical calculations<sup>15</sup> predict the uniaxial anisotropy  $K_u$  scales as  $K_u \sim M_s(T)^2$  (in the high temperature region). If we assume the decrease in  $M_s$  proportional to  $T^{0.5}$  in the high temperature region just as the well-known mean field approximation, the linear decrease in  $K_u$  as a function of the temperature is described by these theories. Thus, we assumed the linear dependence of  $K_u$  on the temperature for the present CrPt<sub>3</sub> (20 nm) onto SiO<sub>2</sub>. In this case, the effective anisotropy constant  $K_{\text{eff}}$  is also supposed to decrease linearly with temperature, and thus it was estimated to be  $4.4 \times 10^6$  ergs/cc at room temperature. The perpendicular anisotropy constant  $K_u$  of CrPt<sub>3</sub> was represented by the sum of the  $K_{\text{eff}}$  and the shape anisotropy  $2\pi M_s^2$ , and resulted in  $5 \times 10^6$  ergs/cc. The perpendicular anisotropy of CrPt<sub>3</sub> alloy films originates from a strain induced uniaxial anisotropy, and the strain is considered to result from the difference of the thermal expansion coefficient between the CrPt<sub>3</sub> and SiO<sub>2</sub> substrates. The strain will be relaxed in the thick film, and the relaxation of the strain results in the reduction in the perpendicular anisotropy. The CrPt<sub>3</sub> film studied here has total thicknesses of 20 nm, so that larger perpendicular anisotropy  $K_u$  than that of the previous report (total thickness 60 nm)<sup>12</sup> was obtained.

Figure 3 shows the dependence of the  $M_s$ ,  $H_c$ ,  $K_u$ , and saturation field  $H_k$  of the ion-irradiated CrPt<sub>3</sub> (20 nm) films on the 30 keV Kr<sup>+</sup> ion dose amount. The saturation field  $H_k$  was calculated simply as  $H_k = 2K_{\text{eff}}/M_s$ , where  $K_{\text{eff}} = K_u - 2\pi M_s^2$ . The  $M_s$ ,  $H_c$ , and  $K_u$  of CrPt<sub>3</sub> ordered alloy films start to decrease from the Kr<sup>+</sup> irradiation dose of  $10^{13}$  ions/cm<sup>2</sup>, and these parameters became zero by a quite low ion dose of  $2 \times 10^{14}$  ions/cm<sup>2</sup>. This ion dose of Kr<sup>+</sup>,  $2 \times 10^{14}$  ions/cm<sup>2</sup>, is much lower than that of the previous report using 700 keV N<sup>+</sup> ions.<sup>10</sup> Atomic force microscope (AFM) measurements show that such a low ion dose of  $2 \times 10^{14}$  ions/cm<sup>2</sup> has no influence on the surface topology and the film thickness. In the previous report on 22 keV Ga<sup>+</sup> ion irradiation into Co/Pd MLs, Ga<sup>+</sup> ion dose of  $2 \times 10^{15}$  ions/cm<sup>2</sup> is reported to cause the film etching of

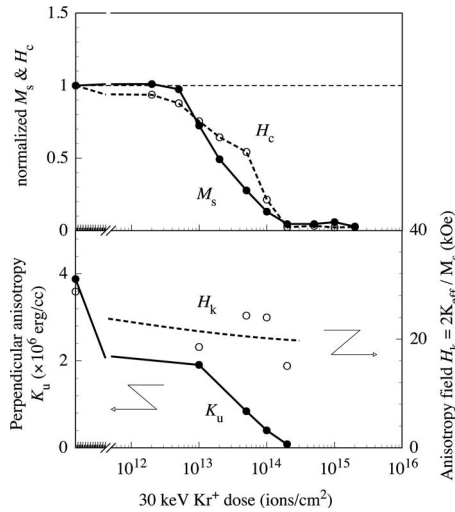


FIG. 3. 30 keV  $\text{Kr}^+$  ion dose dependence of saturation magnetization  $M_s$ , coercivity  $H_c$ , perpendicular anisotropy  $K_u$ , and saturation field  $H_k$  of the ion-irradiated  $\text{CrPt}_3$  (20 nm) films onto a thermally oxidized Si substrate. The  $M_s$  and  $H_c$  are normalized as the values before irradiation to be 1.

$\sim 2$  nm.<sup>16</sup> If we assume the same sputtering yield for the present 30 keV  $\text{Kr}^+$  irradiation, the etching depth after the irradiation of  $2 \times 10^{14}$  ions/cm<sup>2</sup> is estimated to be 0.2 nm, which is lower than the resolution limit of our AFM, 0.5 nm. Unlike the dose dependence of  $M_s$ ,  $H_c$ , and  $K_u$ , the  $H_k$  does not decrease significantly with the increase in the ion dose, and exhibits more than 20 kOe even at the ion dose of  $1 \times 10^{14}$  ions/cm<sup>2</sup>. This indicates that the variation of  $K_u$  with increasing the ion dose is similar to that of  $M_s$ . The large  $H_k$  observed at an ion dose of  $1 \times 10^{14}$  ions/cm<sup>2</sup> may be related that the lattice distortion of  $\text{CrPt}_3$  unchanged with the  $\text{Kr}^+$  ion irradiation, which will be described later.

Figure 4 shows the (a) out-of-plane and (b) in-plane x-ray profiles of as-ordered  $\text{CrPt}_3$  films on a thermally oxidized Si substrate. The as-ordered  $\text{CrPt}_3$  film exhibits strong 111 and 222 reflections, which indicates the (111) orientation of the film. In the in-plane profile, 110 and 211 superlattice

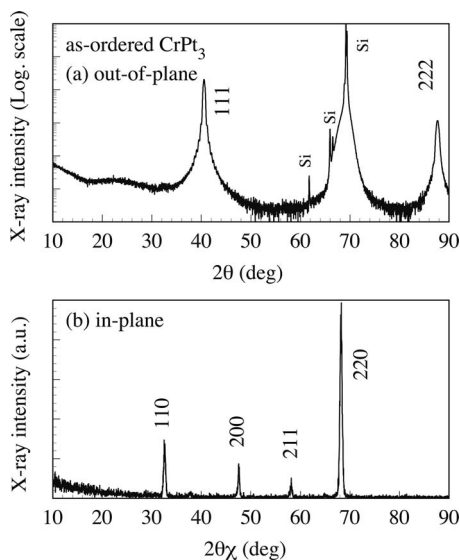


FIG. 4. (a) Out-of-plane and (b) in-plane x-ray profiles of as-ordered  $\text{CrPt}_3$  films on a thermally oxidized Si substrate.

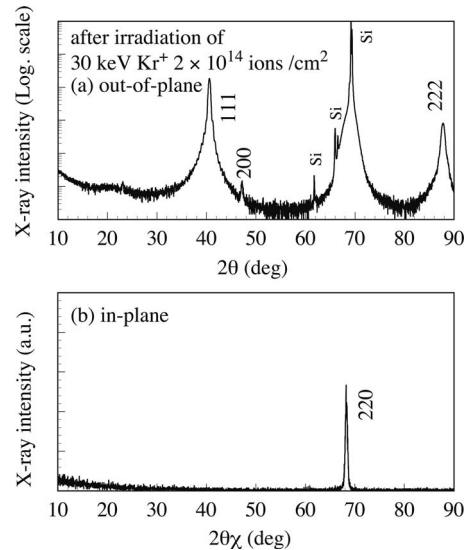


FIG. 5. (a) Out-of-plane and (b) in-plane x-ray profiles of  $\text{CrPt}_3$  films after irradiation of 30 keV  $\text{Kr}^+$   $2 \times 10^{14}$  ions/cm<sup>2</sup>.

lines, indicating the formation of the  $L1_2$  phase, were clearly seen. No diffraction peaks indicating the oxidation of  $\text{CrPt}_3$  and/or intermixing between the substrate ( $\text{SiO}_2$ ) and the film were seen in Figs. 4(a) and 4(b). The order parameter estimated from the integrated intensities of the 110 superlattice line and 220 fundamental line was  $S=0.9$ , and thus the as-ordered  $\text{CrPt}_3$  film is considered to have an almost perfect  $L1_2$  ordered structure. The in-plane and out-of-plane lattice constants of  $\text{CrPt}_3$  are  $a_i=3.89$  Å and  $a_p=3.85$  Å, respectively. Thus, the lattice distortion  $\varepsilon=(a_i-a_p)/a_p$ , contributing to the large perpendicular anisotropy of  $\text{CrPt}_3$ , was estimated to be about 1%. Figure 5 shows the (a) out-of-plane and (b) in-plane profiles of a  $\text{CrPt}_3$  (20 nm) film after  $\text{Kr}^+$  ion irradiation of  $2 \times 10^{14}$  ions/cm<sup>2</sup>. The out-of-plane x-ray profile after the ion irradiation shows a strong (111) orientation, and was almost identical to that of as-ordered  $\text{CrPt}_3$  shown in Fig. 4(a). On the other hand, as shown in Fig. 5(b), the 110 and 211 superlattice lines completely disappeared after the ion dose of  $\text{Kr}^+$ ,  $2 \times 10^{14}$  ions/cm<sup>2</sup>, which means the  $\text{CrPt}_3$  film was transformed from a  $L1_2$  phase to a disordered fcc phase by the ion irradiation. From Figs. 4 and 5, we found that the  $\text{Kr}^+$  ion irradiation of  $2 \times 10^{14}$  ions/cm<sup>2</sup> does not affect the lattice distortion of  $\text{CrPt}_3$ , contributing its large perpendicular anisotropy. The in-plane and out-of-plane lattice constants of  $\text{CrPt}_3$  after the  $\text{Kr}^+$  irradiation of  $2 \times 10^{14}$  ions/cm<sup>2</sup> remained  $a_i=3.89$  Å and  $a_p=3.85$  Å, respectively. When the  $\text{CrPt}_3$  disordered by  $\text{Kr}^+$  ion irradiation is annealed again at 850 °C, the  $\text{CrPt}_3$  re-exhibits ferrimagnetism and the strong perpendicular anisotropy due to the recovery of the  $L1_2$  ordering.

Figure 6 shows the dependence of the lattice distortion  $\varepsilon$  and order parameter  $S$  on the 30 keV  $\text{Kr}^+$  ion dose amount. The lattice distortion was estimated from the out-of-plane and in-plane lattice constants,  $a_p$  and  $a_i$ , respectively, as  $\varepsilon=(a_i-a_p)/a_p$ . The order parameter  $S$  decreased with increasing  $\text{Kr}^+$  ion dose. The decreases in the ordering parameter will cause the reduction in the Curie temperature of  $\text{CrPt}_3$ , which will be observed as the decrease in  $M_s$  and  $K_u$  as



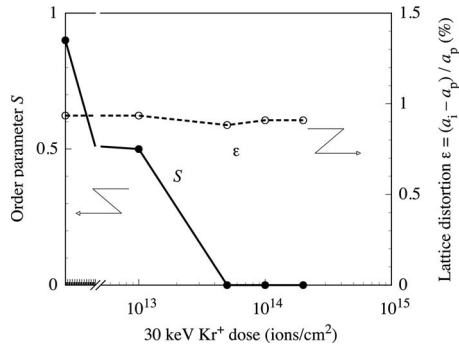


FIG. 6. Dependence of the lattice distortion  $\varepsilon$  and order parameter  $S$  on the 30 keV  $\text{Kr}^+$  ion dose amount. The lattice distortion was estimated from the out-of-plane and in-plane lattice constants,  $a_p$  and  $a_i$ , respectively, as  $\varepsilon = (a_i - a_p) / a_p$ .

discussed in Fig. 3. The ordering parameter  $S$  became almost zero at the ion dose of  $5 \times 10^{13}$  ions/cm<sup>2</sup> as shown in Fig. 6. This ion dose is smaller than that necessary to suppress the magnetization of  $\text{CrPt}_3$ ,  $2 \times 10^{14}$  ions/cm<sup>2</sup> in Fig. 3. This is considered to be due to the limited penetration depth of incident x ray in the in-plane  $\phi$ - $2\theta\chi$  scan. For fixing the incident x-ray  $\omega = 0.4^\circ$ , the x-ray probing depth will be limited to be about 10 nm from the surface. Thus the structure of  $\text{CrPt}_3$  within this probing depth will be reflected in the in-plane profile. By TRIM code simulation, it was confirmed that the number of vacancies in  $\text{CrPt}_3$  generated by the 30 keV  $\text{Kr}^+$  ion impact decreased with increasing the distance from the surface. The lattice distortion  $\varepsilon$  was unchanged even when the  $\text{Kr}^+$  ion dose was increased to  $2 \times 10^{14}$  ions/cm<sup>2</sup>, as shown in Fig. 6. We consider this is the reason why a large anisotropy field  $H_k$  was observed even at a high  $\text{Kr}^+$  ion dose as shown in Fig. 3, since the lattice distortion is the origin of the large perpendicular anisotropy of  $\text{CrPt}_3$ . In order to apply the  $\text{CrPt}_3$  to an ion-irradiated patterned medium, the relaxation of the lattice distortion by the ion irradiation will be a significant problem, because the irradiated (relaxed) region may affect the distortion and perpendicular anisotropy of the nonirradiated region. However, such a relaxation was not confirmed in the 30 keV  $\text{Kr}^+$  ion irradiation up to  $2 \times 10^{14}$  ions/cm<sup>2</sup>, and thus the  $\text{CrPt}_3$  ordered alloy is considered to be a candidate for the future high density ion-irradiated bit patterned media.<sup>9</sup>

#### IV. CONCLUSION

$L1_2$  ordered  $\text{CrPt}_3$  alloy films were prepared by postannealing of magnetron sputtered Cr/Pt MLs. The fabricated  $L1_2$   $\text{CrPt}_3$  (20 nm) onto a  $\text{SiO}_2$  substrate exhibited a quite large perpendicular anisotropy of  $5 \times 10^6$  ergs/cc, due to the large lattice distortion of 1%. The  $\text{CrPt}_3$  film was irradiated by 30 keV  $\text{Kr}^+$  ions, and the modification of the structure and magnetic properties has been investigated in detail. The satu-

ration magnetization, coercivity, and perpendicular anisotropy decreased with increasing  $\text{Kr}^+$  ion dose and became almost zero at a quite low ion dose of  $2 \times 10^{14}$  ions/cm<sup>2</sup>, which is a quite useful property for the high density ion-irradiated patterned media. The suppression of the magnetic order of  $\text{CrPt}_3$  by the  $\text{Kr}^+$  ion irradiation is attributed to the transformation of the structure from the  $L1_2$  phase to a disordered fcc phase, which was confirmed by XRD analysis. Unlike the magnetization and perpendicular anisotropy, the anisotropy field does not decrease significantly with the increase in the ion dose, and exhibits more than 20 kOe even at the ion dose of  $1 \times 10^{14}$  ions/cm<sup>2</sup>. This is considered to be related to the fact that the lattice distortion of  $\text{CrPt}_3$  unchanged even when the  $\text{Kr}^+$  ion dose was increased to  $2 \times 10^{14}$  ions/cm<sup>2</sup>. The results obtained here indicate that the  $\text{Kr}^+$  ion irradiation onto  $\text{CrPt}_3$  is a promising technology to develop future high density ion-irradiated bit patterned media.

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