

## 並行分散計算特論 (9)

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System  $\approx$  Specification

System:  $\text{new } \vec{a}.(P_1 | \dots | P_n)$

Specification: in Seq Proc. Exp.

## Example: Lottery

### Specification

$$\text{Lotspec} \stackrel{\text{def}}{=} \tau.b_1.\text{Lotspec} + \dots + \tau.b_n.\text{Lotspec}$$

N agents to rotate a token to be selected

$$A(a, b, c) \stackrel{\text{def}}{=} \vec{a}.C(a, b, c)$$

$$B(a, b, c) \stackrel{\text{def}}{=} b.C$$

$$C(a, b, c) \stackrel{\text{def}}{=} \tau.B(a, b, c) + c.A(a, b, c)$$

$$\text{new } \vec{a}(C_1 | A_2 | \dots | A_n)$$

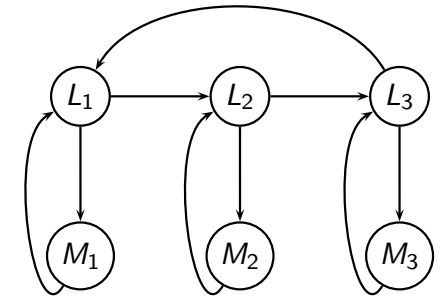
## Example: Lottery

if  $n=3$

$$L_1 = \text{new } a_1 a_2 a_3 (C_1 | A_2 | A_3)$$

$$L_2 = \text{new } a_1 a_2 a_3 (A_1 | C_2 | A_3)$$

$$L_3 = \text{new } a_1 a_2 a_3 (A_1 | A_2 | C_3)$$



## Verification of Lottery

### Theorem

$L_1 \approx \text{Lotspec}$

**Proof sketch:** Show the following  $\mathcal{S}$  is a weak bisimulation:

$$\mathcal{S} = \{(L_i, \text{Lotspec}) \mid 1 \leq i \leq n\} \cup \{(L'_i, b_i \cdot \text{Lotspec})\}$$