

# Electric Field Simulation of Permittivity and Conductivity Graded Materials ( $\epsilon/\sigma$ -FGM) for HVDC GIS Spacers

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## ABSTRACT

This paper discusses the application of the novel technology - functionally graded material (FGM) which combines both spatial permittivity ( $\epsilon$ ) and conductivity ( $\sigma$ ) distributions with the aim to control the electric field around DC-GIS spacer. Some distribution types of  $\epsilon$  and/or  $\sigma$  in the spacer bulk, such as U-type and graded to higher conductivity (GHC) are investigated through electric field simulation, in comparison to the uniform spacer with constant  $\epsilon$  and  $\sigma$  distributions. The electric field relaxation effect of each distribution type of  $\epsilon/\sigma$ -FGM under DC steady state, DC polarity reversal, DC-on, and lightning impulse voltage superimposed on DC steady state condition are obtained. The results show that  $\epsilon/\sigma$ -FGM with U-type permittivity and GHC-type conductivity distribution of which low  $\sigma$  is applied near the high voltage side of the DC-GIS spacer is the most effective in reducing the maximum electric field under all stated conditions.

Index Terms — functionally graded materials (FGM), electric field grading, DC steady state, polarity reversal, conductivity, permittivity

## 1 INTRODUCTION

**THE** requirement of a larger scale of power transmission over long distances has encouraged the development of high voltage direct current (HVDC) system which offers high power transmission efficiency with low transmission losses. As power generation from renewable energy also expands in recent years, HVDC system beneficially serves for purposes such grid interconnections and frequency conversions. Besides, the compact structure of DC power apparatus is advantageous in terms of space, cost, and particularly SF<sub>6</sub> gas reduction [1-2].

On the other hand, unlike AC, designing an insulation system for DC power apparatus has its own complications, since more parameters other than material aging, such as thermo-electrical interdependencies need to be considered [3]. Specifically, the solid insulation of GIS or GIL, such as the spacer becomes the critical component that usually leads to insulation failure. Immediately after the DC voltage is applied, capacitive fields

take place around the spacer which transit to resistive fields over time under DC steady state. The field transition is influenced by both the permittivity and the conductivity of the material, where the conductivity in turn is affected by the temperature gradient and the electric field distribution within the insulation system. These factors can lead to local electric field enhancement, that if uncontrolled may cause insulation breakdown [3-5].

For that reason, controlling the electric field distribution around GIS spacer under DC operating conditions is indispensable. Many attempts in reducing the electric field stress have been taken, such as applying shielding electrodes and radii ratios optimization which complicate the design, yet limits the performance improvement. Electric field grading concepts through geometry (bulk) and potential (surface) are reviewed for this problem [6].

In our past works, a scale model of functionally graded materials (FGM) with graded permittivity has been proposed and applied to AC-GIS spacer. The simulation result shows that

the maximum electric field strength in SF<sub>6</sub> gas can be reduced by 64% compared to a spacer with uniform permittivity. Additionally, the discharge inception voltage can be improved by 70% at 0.4 MPa [7-8].

Similar research on  $\varepsilon$ -FGM was also conducted by other groups who proposed permittivity modification on various types of spacer through numerical topology optimization. The method results in improved electric field distribution and reduced the maximum electric field more than 50%. In addition, an  $\varepsilon$ -FGM fabrication concept through 3D printing technology was introduced. However, this approach is still considered as expensive and requires modification for FGM implementation [9]. Another paper has reported about charge transport mechanism and surface charge control methods on novel HVDC spacers in which one of them is through surface conductivity modification [10].

Therefore, for DC application, an FGM with graded permittivity and/or conductivity applied to the spacer bulk is required to fulfill the purpose of electric field grading, under steady-state DC stress and time-varying stress that occurs during DC-on, polarity reversal, or superimposed lightning impulse voltage on DC steady state [11-12]. In this paper, two different types of FGM with graded permittivity ( $\varepsilon$ ) and/or conductivity ( $\sigma$ ) distribution, which are the U-type and graded-to-higher conductivity (GHC)-type, are discussed for electric field grading under different DC stresses. The electric field simulation is performed to verify the electric field relaxation effect around  $\varepsilon/\sigma$ -FGM spacer in comparison to the spacer with uniform (constant)  $\varepsilon$  and  $\sigma$ .

## 2 CONCEPT OF DC-FGM AND SIMULATION MODEL

### 2.1 CONCEPT OF DC-FGM

The basic concept of electric field grading by FGM can be explained by the electric field distributions in a GIS which consist of capacitive and resistive electric fields. Derived from Ampere's Law of Maxwell's equation, the total current density is shown by equation (1),

$$\vec{J} = \vec{J}_c + \vec{J}_d = \sigma \vec{E} + \frac{\partial \vec{E}}{\partial t} \quad (1)$$

where  $\vec{J}_c$  is the conduction current by moving charges,  $\vec{J}_d$  is the displacement current resulted from the time-dependent electric field,  $\sigma$  and  $\varepsilon$  are the electric conductivity and the permittivity of the material to which the electric field  $\vec{E}$  is applied. By applying vector identity and Fourier transform, the continuity equation is obtained and can be simply written as equation (2),

$$\nabla \cdot \left( \varepsilon - j \frac{\sigma}{2\pi f} \right) \nabla \varphi = 0 \quad (2)$$

where  $f$  is assumed to be the frequency of the applied AC voltage, and  $\varphi$  is the potential.

Depending on the applied voltage, for AC (capacitive) fields, the displacement current with decisive  $\varepsilon$  is usually dominant. On the other hand, for DC (resistive) fields that occur in DC steady state condition, only the conduction current with  $\sigma$  of the material is needed to be considered.

Nevertheless, both AC and DC fields take place under the applied voltage pattern in DC application, as illustrated in Figure 1. Mixed electric fields can occur during DC polarity reversal, turn off, and other conditions which possibly happen during operation, such as the superimposed lightning impulse (LI) voltage on DC steady state. Considering these phenomena, in order to control the electric field distributions in the insulation system of a HVDC GIS, the FGM application to the spacer should incorporate both  $\varepsilon$  and  $\sigma$  grading, which is called as  $\varepsilon/\sigma$ -FGM. An example of this scheme is also illustrated in Figure 2. In this work,  $\varepsilon$  and  $\sigma$  distributions in the spacer bulk are assumed to be independent of each other.

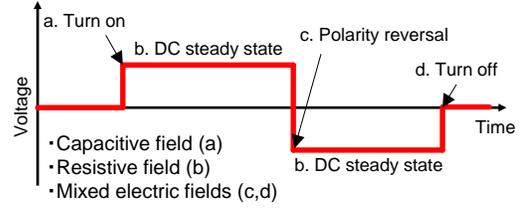


Figure 1. Voltage pattern in HVDC power apparatus.

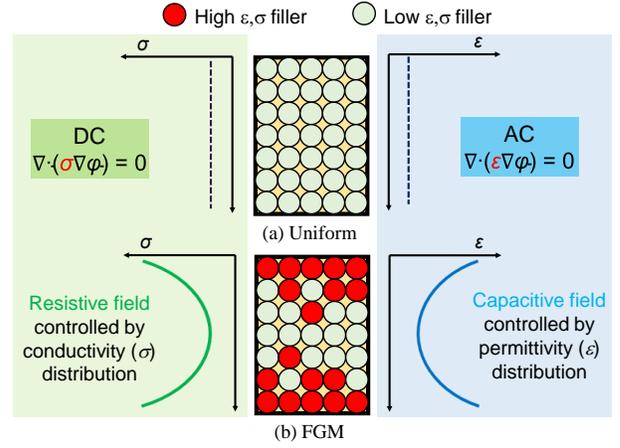
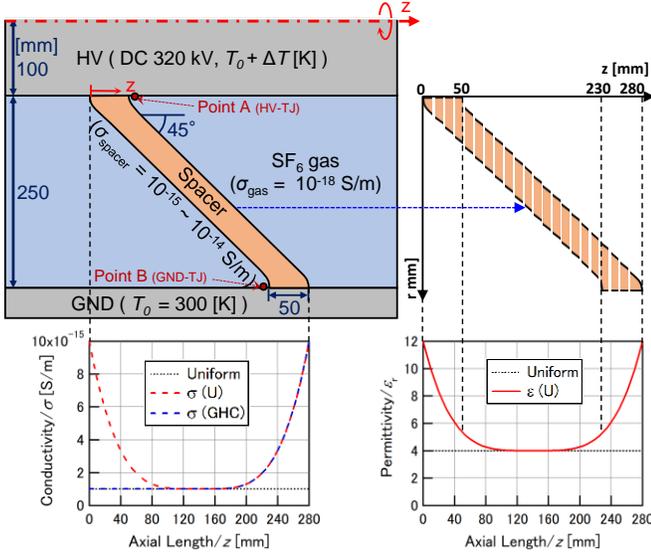


Figure 2. Electric field control by permittivity and conductivity distributions of the insulating material.

### 2.2 PERMITTIVITY/CONDUCTIVITY DISTRIBUTION OF $\varepsilon/\sigma$ -FGM AND SIMULATION CONDITIONS

The main idea of grading the material properties throughout the spacer's material is to differentiate the spacer parts that get higher stress than the others with higher  $\sigma$ , so that  $E$  around those parts can be relaxed. Therefore, smooth grading of  $\sigma$  and/or  $\varepsilon$  is required to develop more uniformly distributed  $E$  stress within the spacer bulk and along the spacer length.

There are two types of  $\sigma$  grading and one type of  $\varepsilon$  grading which are simulated in the current works. Together with the simulation model of 320 kV DC GIS cone-type spacer [13-14], the shape and range of graded  $\varepsilon/\sigma$ -FGM in comparison with uniform spacer is shown in Figure 3. These graded  $\varepsilon$  and  $\sigma$  are applied to the FGM spacer longitudinally along  $z$  axis by controlling the density of the filler with high  $\varepsilon$  and  $\sigma$  through flexible mixture casting (FMC) method [8]. This method allows the composite mixture to be accumulated in a spacer mold from  $z = 0$  up to  $z = 280$  mm, so that the  $\varepsilon$  and  $\sigma$  values change gradually in  $z$  direction as shown in Figure 3.



**Figure 3.** DC FGM cone-type spacer simulation model with conductivity and permittivity distribution types.

The conductivity distribution  $\sigma(U)$  with U-type  $\sigma$  grading has the highest  $\sigma$  ( $10^{-14}$  S/m) at the spacer interface with the high voltage (HV) side as well as at the spacer interface with the ground (GND) side. The high  $\sigma$  from both ends is graded toward the lowest  $\sigma$  ( $10^{-15}$  S/m) at the middle part of the spacer. This type of grading is expected to be able to reduce high  $E$  in the vicinity of the concave surface of the spacer near the HV side (the triple junction of HV side/ HV-TJ) and in the vicinity of the convex surface of the spacer near the GND side (GND-TJ). Hence,  $E$  is more uniformly distributed in the middle part of the spacer with lower  $\sigma$ .

The conductivity distribution  $\sigma(\text{GHC})$  with grading-to-higher-conductivity is considered for  $E$  relaxation at DC polarity reversal (DC-PR). According to [15], the electric field at DC-PR ( $E_{\text{PR}}$ ) can be calculated by equation (3),

$$E_{\text{PR}} = |2E_{\text{AC}} - E_{\text{+DC}}| \quad (3)$$

where  $E_{\text{AC}}$  and  $E_{\text{DC}}$  are the capacitive and resistive field, respectively. The spacer with  $\sigma(U)$  having higher  $\sigma$  near HV-TJ will cause  $E_{\text{DC}}$  component at HV-TJ reduced, hence the  $E_{\text{PR}}$  increases. For this purpose,  $\sigma(\text{GHC})$  is more likely to lead to better results, as it has low  $\sigma$  around HV-TJ up to the middle part of the spacer, resulting in enhanced  $E_{\text{DC}}$  component around that area. Thus,  $E_{\text{PR}}$  is reduced.

Additionally, due to  $E_{\text{AC}}$  occurrence under DC-PR or other conditions with superimposed voltages,  $\epsilon$  grading in U-type where the spacer parts at the interface with HV and GND sides have high  $\epsilon$  ( $\epsilon_r = 12$ ) and the middle part of the spacer has low  $\epsilon$  ( $\epsilon_r = 4$ ) is expected to reduce high  $E$  around HV electrode/spacer and GND electrode/spacer interfaces [7].

$E$  simulation is conducted using Comsol Multiphysics® by finite element method. Some combinations of  $\epsilon$  and  $\sigma$  distributions are applied to the cone-type spacer model in Figure 3 under four voltage conditions given in Table 1. Based on the  $E$  simulation results under DC steady state and polarity reversal, the most effective FGM spacer model to the electric field grading is selected and compared with the uniform spacer under DC-on and superimposed LI on DC steady state.

**Table 1.** Electric field simulation conditions.

Applied Voltage	FGM		
	Uniform $\epsilon/\sigma$ distribution	$\sigma$ distribution $\epsilon$ distribution	
DC steady state	Constant ( $\epsilon_r = 4$ , $\sigma = 10^{-15}$ S/m)	constant	U-type
		U-type	constant
		U-type	U-type
		GHC	U-type
Polarity reversal	Constant ( $\epsilon_r = 4$ , $\sigma = 10^{-15}$ S/m)	constant	U-type
		U-type	constant
		U-type	U-type
		GHC	U-type
DC-on		GHC	U-type
Superimposed LI on DC steady state		GHC	U-type

In the simulation,  $\sigma$  depends on the temperature ( $T$ ) and the electric field strength ( $E$ ) as described in equation (4) [2-3, 16],

$$\sigma(T, E) = \sigma_0 \exp\left(-\frac{W}{kT}\right) \exp(aE) \quad (4)$$

where  $\sigma_0$  is the specific conductivity constant in S/m,  $W = 0.95$  eV is the thermal activation energy,  $k$  is Boltzmann constant in eV/K, and  $a = 0.08$  mm/kV is the electric field dependency coefficient. The temperature effect is examined by changing the temperature of the high voltage conductor as  $T_0 + \Delta T$  with  $\Delta T$  ranging from 0 to 70 K, while keeping the temperature of the ground tank at  $T_0 = 300$  K. This temperature distribution is calculated by the heat conduction analysis based on equation (5),

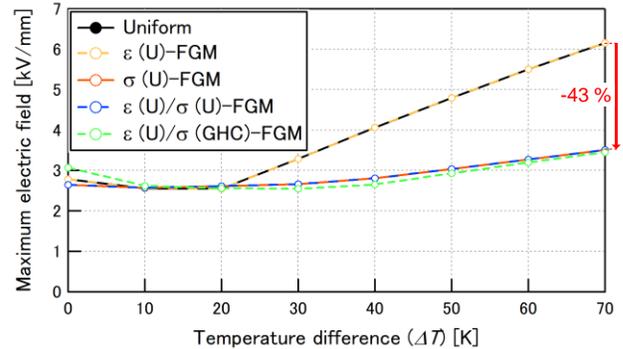
$$\nabla \cdot (\kappa \nabla T) = 0 \quad (5)$$

where  $\kappa$  is the thermal conductivity.

## 3 ELECTRIC FIELD SIMULATION RESULTS OF $\epsilon/\sigma$ -FGM SPACERS

### 3.1 DC STEADY STATE

In DC steady state simulation, 320 kV DC voltage is applied to the HV conductor. Then, the maximum electric field strength ( $E_{\text{max}}$ ) in gas around the uniform and each type of FGM spacers is calculated with  $\Delta T$  from 0 to 70 K, as shown in Figure 4.



**Figure 4.** Maximum electric field strength in gas around the spacer under DC steady state.

The graph shows that  $E_{\text{max}}$  around the uniform spacer at each  $\Delta T$  is the same as that around  $\epsilon(U)$ -FGM spacer. Similarly,  $E_{\text{max}}$  around  $\sigma(U)$ -FGM spacer is the same as that around  $\epsilon(U)/\sigma(U)$ -FGM spacer. This result proves that under DC steady state condition, whether it is graded or not,  $\epsilon$  of the spacer does not contribute to  $E$  distribution in the insulation system, because  $\epsilon$

is not decisive under DC steady state. Only the FGM spacers with graded  $\sigma$  can suppress  $E_{\max}$  despite the increase in  $\Delta T$ .  $E_{\max}$  reduction of  $\varepsilon(U)$ -FGM and  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacers reaches 43% at  $\Delta T = 70$  K.

However, at  $\Delta T < 10$  K,  $E_{\max}$  around  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer is higher than those of the uniform spacer and  $\sigma(U)$ -FGM spacer. This is because at lower  $\Delta T$  at which the  $E_{\max}$  location is within the HV-TJ, the  $\sigma$  distribution  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer near the HV side is at the same level as that of the uniform spacer (low  $\sigma$ ), hence  $E$  in the vicinity of HV-TJ is enhanced compared to  $\sigma(U)$ -FGM spacer that has higher  $\sigma$  in that part. This can be seen in Figure 5 which shows  $E$  distribution around the spacer models at  $\Delta T$  of 0 K, 30 K, and 60 K along with the spots of  $E_{\max}$ .

Besides, unlike the uniform spacer, since the  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer has higher  $\sigma$  at the end part near the ground side, the equipotential lines are pushed from the ground side toward the middle and the part near HV side that has lower  $\sigma$ . Hence, at lower  $\Delta T$ ,  $E$  of  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer is even higher than that of the uniform spacer.

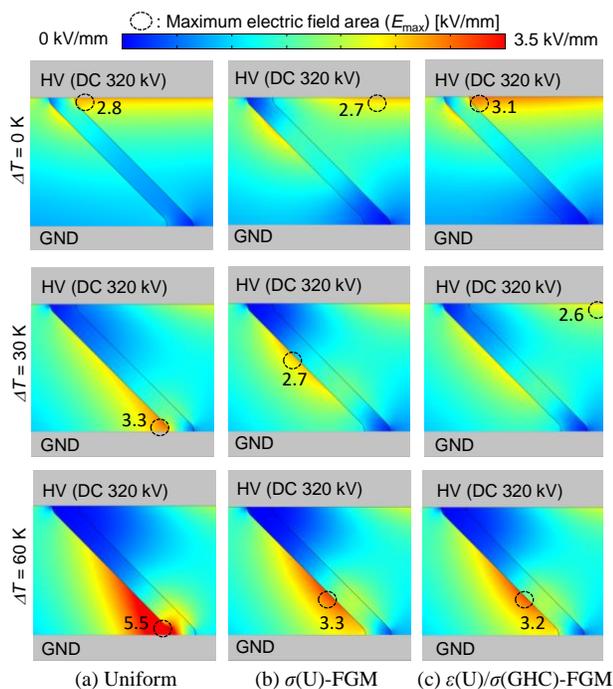


Figure 5.  $E$  distribution around spacers under DC steady state.

### 3.2 DC POLARITY REVERSAL

At DC-PR, there is a sudden change in the voltage magnitude from positive 320 kV to negative 320 kV over a short switching time. Therefore, both  $\varepsilon$  and  $\sigma$  are decisive on  $E$  distribution. According to equation (3),  $E_{\text{DC}}$ ,  $E_{\text{AC}}$ , and  $E_{\text{PR}}$  around uniform and various FGM spacers at  $\Delta T = 20$  K are presented in Figures 6, 7, and 8, respectively.

Figures 6a and 6b show that  $E$  distribution around the uniform spacer is similar to that of  $\varepsilon(U)$ -FGM spacer, which proves that  $\varepsilon$  grading without  $\sigma$  grading in an FGM spacer does not affect  $E$  distribution under DC steady state condition. On the other hand, Figures 6c, 6d, and 6e show that  $E$  distribution around FGM spacers with graded  $\sigma$ , regardless of the  $\varepsilon$  grading, is different

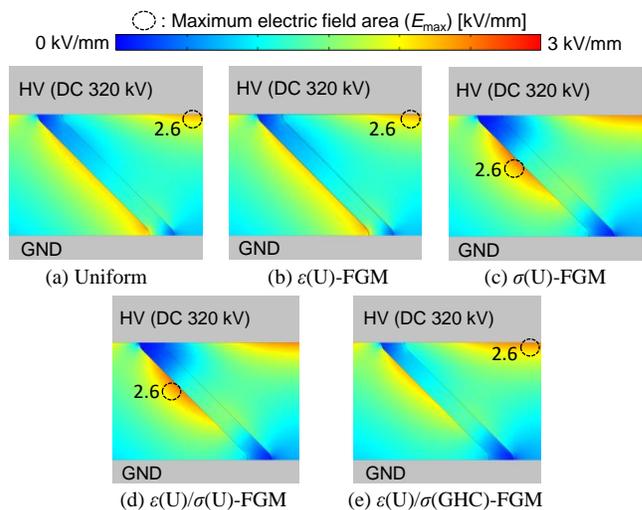


Figure 6.  $E$  distribution under DC steady state ( $E_{\text{DC}}$ ) at  $\Delta T = 20$  K.

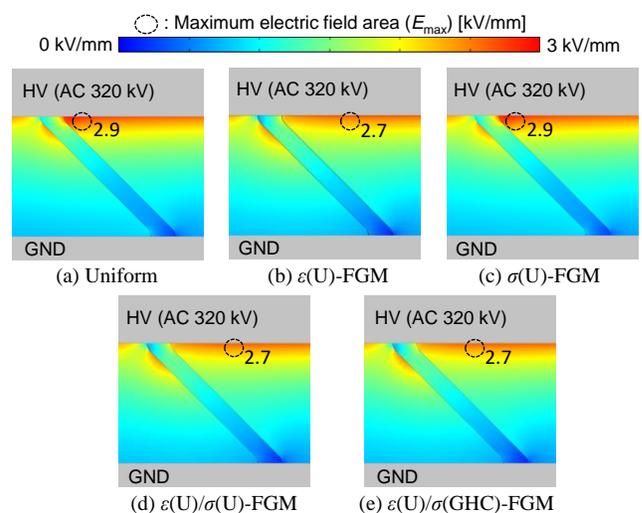


Figure 7.  $E$  distribution under AC steady state ( $E_{\text{AC}}$ ) at  $\Delta T = 20$  K.

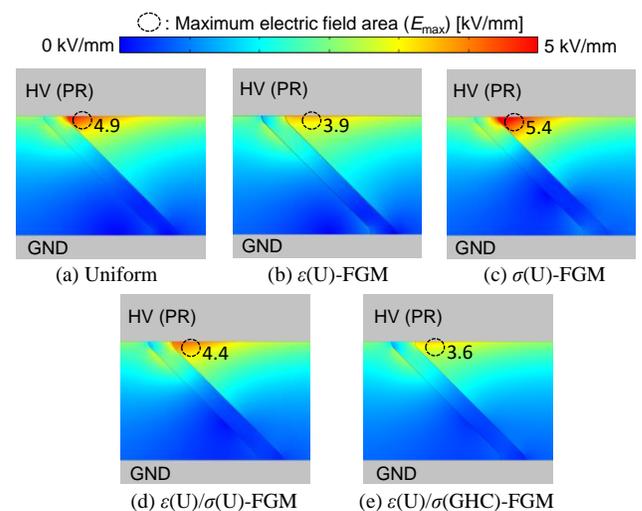


Figure 8.  $E$  distribution under DC-PR ( $E_{\text{PR}}$ ) at  $\Delta T = 20$  K.

from that around uniform spacer. The high  $E$  within the HV-TJ and GND-TJ are clearly reduced due to the higher  $\sigma$  of the spacer parts near those locations.

The opposite phenomena can be seen in Figure 7 which illustrates the capacitive field ( $E_{AC}$ ) distribution. The FGM spacers with graded  $\varepsilon$  (Figures 7b, 7d, and 7e) have high  $E_{AC}$  around HV-TJ, which is reduced owing to the higher  $\varepsilon$  of the spacer at the spacer/HV conductor interface.

Those  $E_{DC}$  and  $E_{AC}$  distributions around each spacer determine the  $E$  distribution at DC-PR ( $E_{PR}$ ) as shown in Figure 8, where  $E_{max}$  is found around the HV-TJ. The  $\sigma(U)$ -FGM spacer, which is effective in reducing  $E_{max}$  under DC steady state, shows on the contrary higher  $E$  compared to the uniform spacer at DC-PR (Figure 8c). This is because the  $E_{AC}$  around uniform and  $\sigma(U)$ -FGM spacers remain the same (Figures 7a and 7c) and the  $E_{DC}$  of  $\sigma(U)$ -FGM spacer at that point is greatly reduced (Figure 6c). As a result,  $E_{PR}$  of  $\sigma(U)$ -FGM spacer is higher than that of uniform spacer.

Meanwhile, the FGM spacers with graded  $\varepsilon$  (Figures 8b, 8d, and 8e) have suppressed  $E_{PR}$  compared to uniform spacer. Referring to equation (3), the effect of  $E_{AC}$  is more dominant than  $E_{DC}$  under PR condition. Therefore,  $\varepsilon$  grading can reduce  $E_{AC}$  component, hence  $E_{PR}$  is also lower than that of uniform or  $\sigma(U)$ -FGM spacer.

Particularly,  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer results in the lowest maximum electric field strength at polarity reversal ( $E_{PR}^{max}$ ) among all other  $\varepsilon/\sigma$ -FGM spacers. This is due to the fact that the higher  $\sigma$  in the spacer part near the ground side causes potential burden from the ground side shifted toward the middle and upper part of the spacer (near HV side) and slightly increases  $E_{DC}$  around those parts with lower  $\sigma$ . Therefore, the resulted  $E_{PR}$  near the HV-TJ of  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer is also reduced a little bit more compared to  $\varepsilon(U)$ -FGM or  $\varepsilon(U)/\sigma(U)$ -FGM spacers.

In order to compare the effect of each FGM spacer, Figure 9 shows  $E_{PR}^{max}$  against  $\Delta T$  between HV and GND conductors. It can be concluded that at DC-PR, the largest reduction of  $E_{PR}^{max}$  at each  $\Delta T$  is given by  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer. The maximum  $E_{PR}$  reduction of  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer is achieved by 30% at  $\Delta T=10$  K compared to uniform spacer. Based on this result, for the next two simulation conditions (DC-on and superimposed lightning impulse on DC steady state), only the  $E$  analysis around  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer with comparison to uniform spacer will be evaluated.

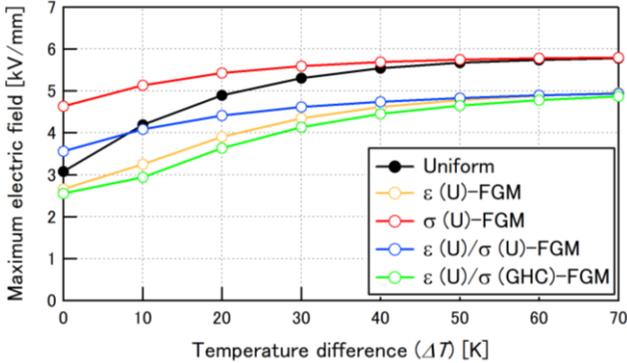


Figure 9.  $E_{max}$  under DC-PR ( $E_{PR}^{max}$ ) against temperature difference  $\Delta T$ .

### 3.3 DC-ON

The  $E$  analysis under DC-on condition is performed through time dependent simulation where positive 320 kV DC voltage

is applied to the HV conductor within 0.01 s switching time. The  $E$  characteristics are then evaluated over time until it reaches DC steady state, particularly at points A and B which are the critical points located at HV-TJ and GND-TJ, as illustrated in Figure 3.

Figures 10 and 11 show the  $E$  distribution around (a) uniform and (b)  $\varepsilon(U)/\sigma(GHC)$ -FGM spacers at different times for  $\Delta T = 20$  K and 70 K, respectively.

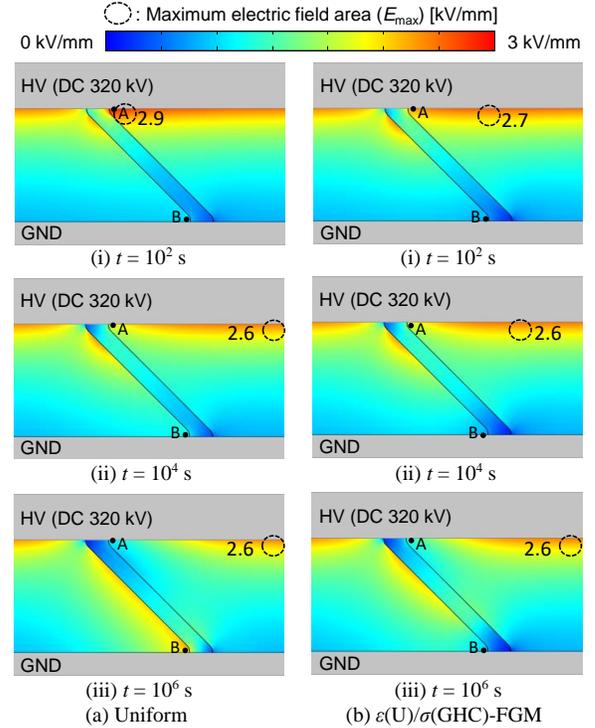


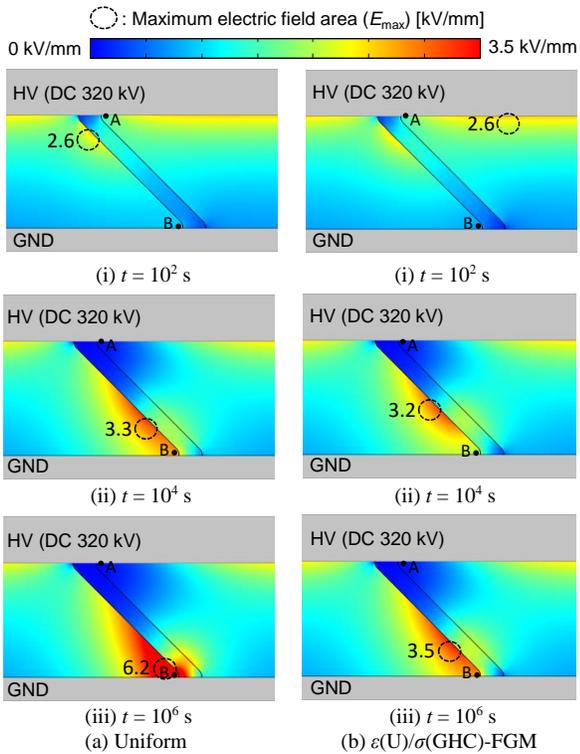
Figure 10.  $E$  distribution around (a) uniform spacer and (b)  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer during DC-on at  $\Delta T = 20$  K.

At lower  $\Delta T$  ( $\Delta T=20$  K), the high  $E$  at early stage of the temporal transition ( $t = 10^2$  s) since the voltage is applied, is concentrated near the HV-TJ (point A) and along the HV conductor surface for both spacers. As time passes, for the uniform spacer, the high  $E$  is shifted toward point B at  $t = 10^6$  s where the DC steady state has been already reached. However, for  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer, the high  $E$  distribution is concentrated on the middle part of the spacer at that time, so point B during DC steady state remains clear of high  $E$ .

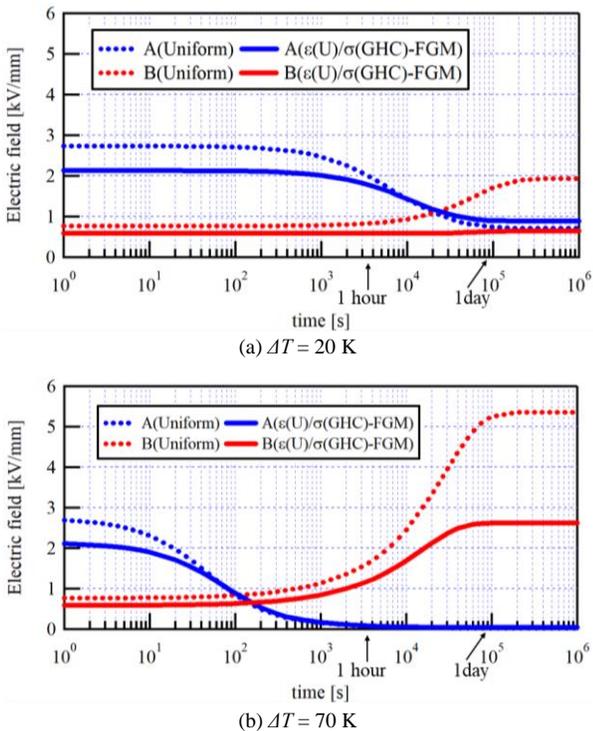
The same situation also applies at higher  $\Delta T$  ( $\Delta T=70$  K), as shown in Figure 11. The high temperature enhances the  $\sigma$  of both spacers near the warm HV side, pushing the potential burden from the HV side toward the GND side. However, the higher  $\sigma$  of  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer near the GND side is further enhanced with the temperature rise, causing the high  $E$  around point B reduced.

The magnitude of  $E$  at both points A and B are more clearly distinguished in Figure 12. At  $\Delta T=20$  K (Figure 12a), as soon as DC voltage is applied,  $E$  of  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer at point A is already lower than that of uniform spacer. This  $E$  reduction is caused by graded  $\varepsilon$  that has effect on  $E_{AC}$ . As time passes, the  $E$  at point A decreases until it reaches the steady state.

On the contrary, the  $E$  at point B around the uniform spacer increases over time due to the displacement of field



**Figure 11.**  $E$  distribution around (a) uniform spacer and (b)  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer during DC-on at  $\Delta T = 70$  K.



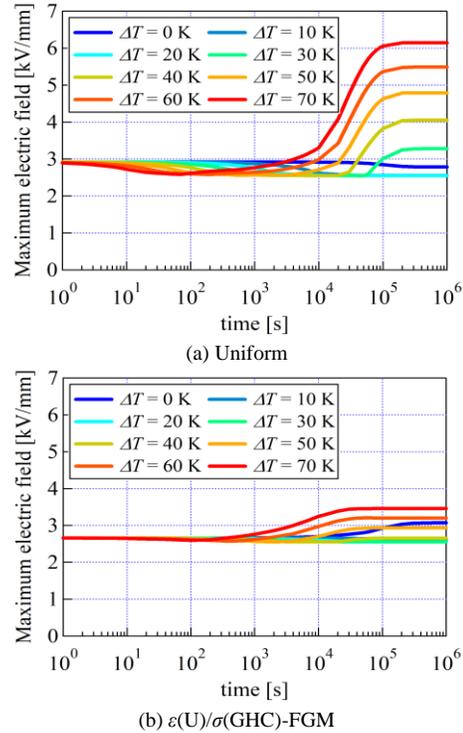
**Figure 12.** Time-varying  $E$  distribution at point A near HV-TJ and at point B near GND-TJ of uniform spacer and  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer at (a)  $\Delta T = 20$  K and (b)  $\Delta T = 70$  K.

concentrations from the HV to the GND side. Nevertheless, the  $E$  at point B around  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer remains the same right from the beginning owing to the higher  $\sigma$  of the spacer near point B.

At  $\Delta T = 70$  K (Figure 12b), the time-varying electric field at points A and B evolves the same way as that at  $\Delta T = 20$  K, with

higher increase of  $E$  at point B as the temperature increases. The transition time required for  $E_{AC}$  to shift into  $E_{DC}$  during DC-on can also be distinguished from the figures. As  $\Delta T$  increases, this capacitive-resistive transition time of  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer gets shorter.

Figure 13 shows the time-varying  $E_{\max}$  in gas around (a) uniform spacer and (b)  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer for different  $\Delta T$  from 0 K to 70 K. It is understood that both  $E_{AC}$  and  $E_{DC}$  of  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacer are relaxed than those of uniform spacer at each  $\Delta T$ , which is indicated by the  $E_{\max}$  location transition from point A to B. The  $E_{\max}$  reduction is by 43% at  $\Delta T = 70$  K, which is consistent with that under DC steady state in Section 3.1.



**Figure 13.** Time-varying  $E_{\max}$  in gas around (a) uniform and (b)  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacers under different  $\Delta T$ .

### 3.4 SUPERIMPOSED LIGHTNING IMPULSE (LI) VOLTAGE ON DC STEADY STATE

The  $E$  simulation under superimposed lightning impulse (LI) voltage on DC steady state is performed through time-dependent simulation, i.e. 320 kV DC voltage applied to the HV conductor until DC steady state is reached, then 1175 kV [17] positive and negative LI voltages are superimposed, as illustrated in Figure 14.

Figures 15 and 16 show  $E$  distribution around (a) uniform and (b)  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM spacers under superimposed standard positive and negative LI of 1175 kV<sub>peak</sub> on 320 kV DC steady state condition, respectively. According to the figures, under both superimposed positive or negative LI voltage on DC steady state, and with or without  $\Delta T$ ,  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM can reduce the  $E$  around the HV-TJ and shift the  $E_{\max}$  location away from the HV-TJ along the HV conductor surface.

In order to obtain the picture quantitatively, Figure 17 indicates the  $E$  at point A under different  $\Delta T$ . Under both

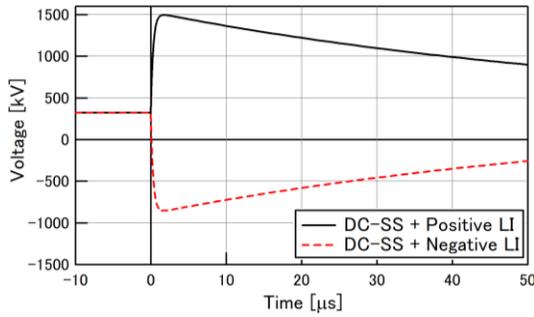


Figure 14. Superimposed LI voltage on DC steady state.

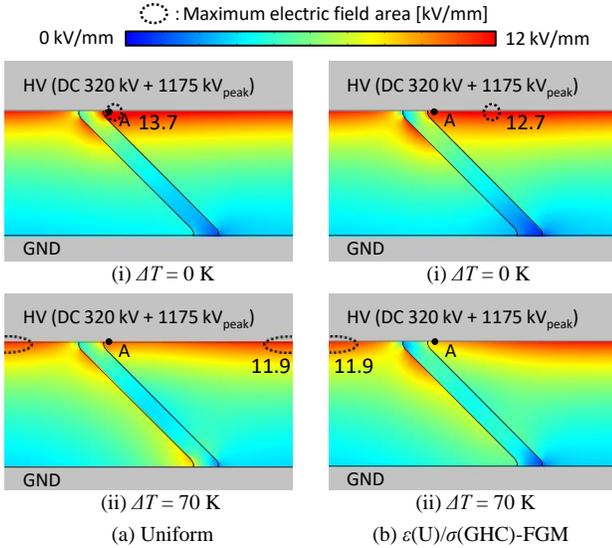


Figure 15.  $E$  distribution under superimposed positive LI voltage on DC steady state.

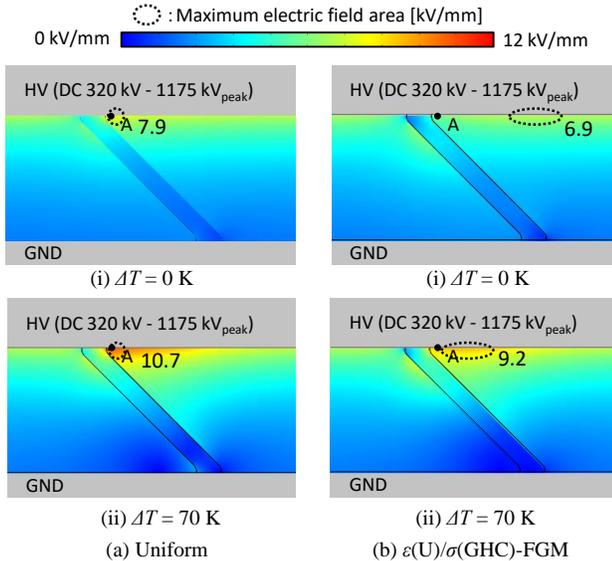


Figure 16.  $E$  distribution under superimposed negative LI voltage on DC steady state.

superimposed positive and negative LI voltages on DC steady state, the  $E$  at point A of  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer is constantly lower than that of uniform spacer even with the higher  $\Delta T$ . The  $E$  reduction is 1.6 kV/mm and 2.0 kV/mm under superimposed positive and negative LI, respectively.

Figure 18 shows  $E_{max}$  under superimposed positive ( $E_{+Imp}$ ) and negative ( $E_{-Imp}$ ) LI voltage on DC steady state against  $\Delta T$ .

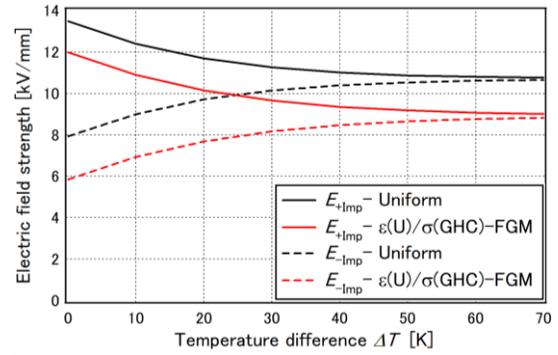


Figure 17.  $E$  at point A under superimposed positive and negative LI voltage on DC steady state.

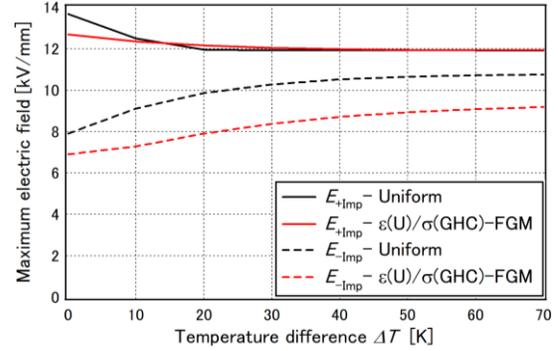


Figure 18.  $E_{max}$  under superimposed positive and negative LI voltage on DC steady state.

The maximum reduction of  $E_{+Imp}$  around  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer is 7% at  $\Delta T = 0$  K. The decrease is due to graded  $\varepsilon$  of  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer that reduces  $E_{AC}$  around HV-TJ. Meanwhile, the high  $\sigma$  at the GND side of the  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer causes potential burden from GND side shifted toward HV side and increases  $E_{DC}$  around HV side. Consequently, the  $E_{+Imp}$  reduction by this FGM model is relatively small.

When  $\Delta T$  increases,  $E_{max}$  around either uniform or  $\varepsilon(U)/\sigma(GHC)$ -FGM spacers converges at approximately 11.9 kV/mm. This value is consistent with the theoretical value of  $E_{max}$  at inner conductor of an infinite coaxial cylinder electrodes.

Similar to the case of DC-PR,  $E_{Imp}$  around  $\varepsilon(U)/\sigma(GHC)$ -FGM spacer is constantly reduced despite the increase in  $\Delta T$ . The highest  $E_{Imp}$  reduction by  $\varepsilon(U)/\sigma(GHC)$ -FGM application is 20% at  $\Delta T = 10$  K.

## 4 CONCLUSIONS

FGM application with graded  $\varepsilon$  and  $\sigma$  in a DC GIS spacer has been proposed and the effectiveness in  $E$  relaxation has been evaluated under various DC operating conditions. Through  $E$  simulation, the following results are revealed.

- (1) FGM application with graded  $\sigma$  is effective for  $E$  relaxation under DC steady state operation.  $\sigma(U)$ -FGM and  $\varepsilon(U)/\sigma(GHC)$ -FGM spacers can reduce the  $E_{max}$  by 43% at  $\Delta T$  of 70 K, compared to uniform spacer.
- (2) FGM application with both graded  $\varepsilon$  and  $\sigma$  is effective to reduce both resistive and capacitive field during other DC operating conditions with rapid voltage change over time, such as polarity reversal, DC-on, and superimposed positive and negative lightning impulse voltage on DC

steady state. The new idea of  $\varepsilon(U)/\sigma(\text{GHC})$ -FGM with low  $\sigma$  distribution near HV side of the spacer is currently evaluated as the most effective  $\varepsilon/\sigma$  distribution in reducing the  $E_{\max}$  in gas compared to uniform spacer. It is validated through electric field simulations with  $E_{\max}$  reduction of 30%, 43%, 7% and 20%, respectively, for each DC operating condition.

For  $\varepsilon/\sigma$ -FGM implementation in the future works, currently the actual permittivity and conductivity characteristics of SiC and SiO<sub>2</sub> filled epoxy insulation material have been measured and applied to the electric field analysis in order to gain more actual results with its temperature and electric field dependence properties. As flexible mixture casting (FMC) method has been reported successfully implemented to create  $\varepsilon$ -FGM spacer with desired  $\varepsilon$  distribution [8, 18-19], it is expected that with the same arrangement in controlling filler density of the epoxy resin throughout spacer length, the desired permittivity and conductivity distribution can be achieved in fabricating  $\varepsilon/\sigma$ -FGM.

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