# Application of Bayesian Optimization for High-Performance TiO<sub>x</sub>/SiO<sub>y</sub>/c-Si Passivating Contact

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# Highlights

• Bayesian optimization was applied to the practical fabrication process of titanium oxide/silicon oxide/crystalline silicon passivating contact.

• Bayesian optimization using multiple sets of samples with different pre-deposition treatments could permit optimization of deposition and post-deposition processes while choosing superior pre-deposition treatment.

• The optimization of the carrier selectivity estimated by independent measurements of the saturation current density and contact resistance was achieved by Bayesian optimization of only 12 cycles and 10 initial random experiments.

# Abstract

We report on the application of Bayesian optimization (BO), which could accelerate the time-intensive process optimization of many parameters, to fabrication of the highperformance titanium oxide/silicon oxide/crystalline silicon passivating contact. The process contains pre-deposition treatment to form SiO<sub>y</sub> interlayer, atomic layer deposition (ALD) of TiO<sub>x</sub>, and hydrogen plasma treatment (HPT) as post-process. We attempted to optimize seven parameters for ALD and HPT by dealing with samples treated by three kinds of chemical solutions in the same batch. This permits to perform BO for each structure at the same time and determine the superior pre-deposition treatment. Consequently, carrier selectivity  $S_{10}$  estimated by independent measurements of the saturation current density and contact resistance was significantly improved by BO of only 12 cycles and 10 initial random experiments. These results certify that BO could efficiently provide experimental conditions in multidimensional parameter space although we need to consider the impact of the metallization process on the passivation performance.

Keyword

Passivating contacts Bayesian optimization Silicon heterojunction solar cell Titanium oxide Hydrogen plasma treatment

# 1. Introduction

Silicon heterojunction (SHJ) solar cells have accomplished high power conversion efficiency (PCE) around 25% [1-4]. In SHJ solar cells, passivating contacts (PCs) play a key role in the efficient separating and transporting of photo-generated carriers in crystalline silicon (c-Si). Furthermore, PCs require the suppression of carrier recombination at the PCs/c-Si heterointerface for reducing the carrier recombination loss of solar cells. In PCs, hydrogenated amorphous Si (a-Si:H) is known as an excellent PC material due to its great passivation performance [1-4]. However, the bandgap energy ( $E_g$ ) of a-Si:H is relatively low (~1.7 eV), resulting in decreasing in the short current density owing to parasitic absorption in a-Si:H layer [5-7]. In this regard, alternative materials to a-Si:H is crucial for further improvement in SHJ solar cells.

Recently, there are a lot of studies of transition metal oxides to utilize for PCs. Molybdenum oxide [8-11], vanadium oxide [8,12] and tungsten oxide [8,13] are gathering attention for hole-selective contacts (HSCs). On the other hand, titanium oxide (TiO<sub>x</sub>) is intensively studied as electron-selective contacts (ESCs) for SHJ solar cells [14-17]. The TiO<sub>x</sub>/c-Si heterostructure forms the small conduction band offset (< 0.05 eV) and large valence band offset (> 2.0 eV), and thus electrons can be transported whereas holes are repelled [14,18,19]. Moreover, the parasitic absorption of TiO<sub>x</sub> is negligible due to the wider  $E_g$  of 3.3 eV than that of a-Si:H [20,21].

However, the passivation performance of  $TiO_x$  is inferior to that of a-Si:H. Many studies have been devoted to improving the passivation performance of  $TiO_x$  and the following process are developed to realize high passivation performance [22-34]. Firstly,  $TiO_x$  should be prepared by atomic layer deposition (ALD) for good passivation performance due to the low deposition damage and large-area uniformity [22-24]. Furthermore, ALD provides precise film thickness control to fabricate a few nm  $TiO_x$  film which suppresses the increase of the series resistance due to  $TiO_x$  itself. Secondly, the inserting silicon oxide  $(SiO_{y})$  interlayer between  $TiO_{x}$  and c-Si has been reported to improve the passivation performance [25-29]. It is considered that this improvement is attributed to the formation of Si-O-Ti bonds by the diffusion of Ti and O atoms from TiO<sub>x</sub> to SiO<sub>y</sub> [27]. Finally, the thermal process after TiO<sub>x</sub> deposition is important to enhance the passivation performance. There are many reports that the ALD-TiO<sub>x</sub> layer can provide a high passivation performance after post-annealing [22-30]. These reports suggest that the improved passivation performance can be caused by an O-terminated c-Si surface [29]. In recent years, hydrogen plasma treatment (HPT) is found to improve the performance of TiO<sub>x</sub>/c-Si heterostructure [31-34]. HPT can supply hydrogen to the TiO<sub>x</sub>/c-Si interface and thus interfacial dangling bonds are terminated by hydrogen atoms [32]. Moreover, HPT can be performed at a lower temperature than annealing, which leads to the deterioration of the passivation performance due to suppression of the  $TiO_x$ phase transformation [29,30,32].

In this study, we applied HPT to ALD-TiO<sub>x</sub>/SiO<sub>y</sub>/c-Si heterostructures to improve the performance for ESC as an index of the carrier selectivity ( $S_{10}$ ). Brendel *et al.* reported that the potential of PCs is evaluated by the following equation [35]:

$$S_{10} = \log_{10} \frac{V_{\rm th}}{J_0 \cdot \rho_c}$$
 (1)

where,  $V_{\text{th}}$ ,  $J_0$ , and  $\rho_c$  denote thermal voltage at 25 °C, the saturation current density, and contact resistivity, respectively. The simultaneous reduction of  $J_0$  and  $\rho_c$  is necessary to

improve  $S_{10}$  and thus increase the PCE of solar cells. The improvement of the passivation performance reduces  $J_0$  which is related to carrier recombination current. It is reported that  $J_0$  is reduced with the increase of TiO<sub>x</sub> thickness. On the other hand,  $\rho_c$  is associated with the bulk resistivity of TiO<sub>x</sub> and increases with increasing TiO<sub>x</sub> thickness. Therefore, TiO<sub>x</sub> thickness is a vital factor due to the trade-off relationship between  $J_0$  and  $\rho_c$  [27].

In general, even if the materials and deposition methods are limited, the fabrication processes including the chemical solution process before deposition, deposition process, and post-deposition process have many parameters. To prepare TiO<sub>x</sub>/SiO<sub>y</sub>/c-Si heterostructures, there are many parameters such as kinds of a chemical solution to form SiO<sub>y</sub> interlayers, ALD cycle ( $C_{ALD}$ ) which determined the TiO<sub>x</sub> thickness and HPT parameters: process temperature ( $T_{HPT}$ ), process time ( $t_{HPT}$ ), H<sub>2</sub> pressure ( $p_{H_2}$ ), H<sub>2</sub> flow rate ( $R_{H_2}$ ), RF power ( $P_{RF}$ ) and electrode distance (d). Therefore, the optimization by the comprehensive experiments costs an inordinate amount of time. Recently, materials informatics to integrate machine learning with materials research is developing rapidly. Meanwhile, a few previous works report that machine learning applied to practical experiments of fabrication process (often termed as process informatics) [33,36-39]. Bayesian optimization (BO) is gathering attention as an effective measure to achieve the optimization with a small number of experiments since it can globally optimize the multiple parameters by stochastic prediction [40].

In this research, we applied BO to optimize the fabrication process of ALD- $TiO_x/SiO_y/c$ -Si heterostructures. The batch process of ALD and HPT was performed onto the three kinds of structure with different pre-deposition treatments to obtain experimental data efficiently. By performing BO for each structure at the same time, we could reveal the superior pre-deposition treatment while optimizing multiple process parameters.

#### 2. Experimental

## 2.1 Sample preparation

All the  $TiO_x$  layers were deposited on double-side-polished, float-zone-grown n-type c-Si(100) substrates by thermal ALD (GEMStar-6, Arradiance). The resistivity and thickness of the substrates were 2.0-4.0  $\Omega$  cm and 280  $\pm$  20  $\mu$ m, respectively. Three different kinds of chemical solution processes were performed before the deposition of a  $TiO_x$  layer. One set of the substrates were only dipped in 5% HF for 30 seconds (referred to as TiO<sub>x</sub>/c-Si hereafter). To insert SiO<sub>y</sub> interlayer, after HF dipping, another set of substrates were immersed in 30% hydrogen peroxide (H<sub>2</sub>O<sub>2</sub>) at room temperature for 10 minutes (referred to as TiOx/SiOy(H2O2)/c-Si hereafter) and the other set of substrates were immersed in Standard Clean 2 (SC2, 35% hydrochloric acid (HCl): 30% H<sub>2</sub>O<sub>2</sub>: deionized water = 1:1:4) solution at 60 °C for 10 minutes (referred to as  $TiO_x/SiO_y(SC2)/c-Si$  hereafter). Then,  $TiO_x$  layers were deposited by ALD at a substrate heater temperature of 150 °C. The metal precursor and oxidant were tetrakis(dimethylamido)titanium and water vapor, respectively. The ALD cycle related to TiO<sub>x</sub> layer thickness was changed in a range of 15 to 60 cycles (Table I). After depositing, samples were exposed to the hydrogen plasma produced by a VHF power supply with a frequency of 60 MHz. The electrode area was 138.5 cm<sup>2</sup>. There were six variable parameters in HPT: process temperature ( $T_{HPT}$ ), process time ( $t_{HPT}$ ), H<sub>2</sub> pressure ( $p_{H_2}$ ), H<sub>2</sub> flow rate  $(R_{\rm H_2})$ , RF power  $(P_{\rm RF})$  and electrode distance (d). Table I shows the empirically determined minimum and maximum values of each parameter.

	C <sub>ALD</sub> [cycle]	$T_{\rm HPT}$ [°C]	t <sub>HPT</sub> [min]	р <sub>Н2</sub> [Ра]	$R_{\rm H_2}$ [sccm]	P <sub>RF</sub> [W]	<i>d</i> [mm]
Minimum value	15	50	0.25	100	10	270	10
Maximum value	60	300	4	1000	100	420	40

Table I. Maximum and minimum values of ALD cycle and each parameter of HPT

# 2.2 Characterization

 $J_0$  and the effective carrier lifetime ( $\tau_{eff}$ ) were measured by quasi-steady-state photoconductance decay (QSSPC) using a WCT-120 (Sinton Instruments).

 $\rho_{c}$  was measured by using the Cox-Strack method [41,42]. After HPT, six dots of aluminum (Al)/magnesium (Mg) stack with different diameters in a range of 0.5 to 1.5 mm were deposited on the front side by thermal evaporation. It is noted that the presence of the Mg interlayer plays an important role in reducing the contact resistance without significant degradation of the passivation performance owing to the low workfunction. After removing native oxides on the rear side by HF cleaning, indium gallium (InGa) paste as the electrode was coated on the rear side. For each front electrode dot, current-voltage (*I-V*) measurement was performed and  $\rho_{c}$  was calculated from the relationship between the resistance and contact area. The details of the Cox-Strack method are given elsewhere [41,42].

The thickness of  $TiO_x$  was determined by a spectroscopic ellipsometer (SE, M-2000DI, J. A. Woollam). Previous work revealed that ALD- $TiO_x$  was in the amorphous phase by transmission electron microscopy, thus the Tauc-Lorentz model [43] was used to model the dielectric function of the  $TiO_x$  layer [27].

#### 2.3 Bayesian optimization (BO)

BO is an effective measure to globally search the minimum or maximum value of an unknown objective function which has multiple parameters [40]. We used Gaussian process regression (GPR) which can describe the non-linear function and estimate the mean  $\mu(x)$  and variance  $\sigma^2(x)$  of the posterior probability distribution. The objective function f(x) is modeled as follows:

$$f(\mathbf{x}) \approx N(\mu(\mathbf{x}), \sigma^2(\mathbf{x}))$$
(2)

where *N* is the Gaussian distribution. BO can manage the exploration and exploitation in a well-balanced manner by using the prediction uncertainty. The exploration means the searching in the region with large uncertainty which corresponds to the region with few data points. On the other hand, exploitation means searching in the region with a high expected value. An acquisition function determined how the balance between exploration and exploitation. In this work, upper confidence bound (UCB), which expresses the weighted sum of  $\mu(\mathbf{x})$  and  $\sigma(\mathbf{x})$ , was used, as follows:

$$a_{\rm UCB}(\mathbf{x}) \approx \mu(\mathbf{x}) + \kappa \sigma(\mathbf{x})$$
 (3)

where  $\kappa$  is the user parameter that controls the balance between the exploration and the exploitation. Fig. 1 shows the results of GPR and the states of the optimization by BO. In Fig. 1 (a), the orange line and red circles are the virtual true function and the observations, respectively. Fig. 1 (b) represents the regression result after two observations, and the black dotted line and gray band show  $\mu(\mathbf{x})$  and  $\sigma(\mathbf{x})$ , respectively. It is noted that the band of  $\sigma(\mathbf{x})$  becomes narrower around observations because the uncertainty of prediction is

reduced. The value of  $a_{UCB}(x)$  corresponds to the top edge of the gray band. The blue arrows show the conditions to maximize  $a_{UCB}(x)$ , which are adopted as the next experimental condition. And then, the prediction model is updated by adding the result at the next experimental condition. Fig. 1 (d) shows that the optimization was performed without being trapped by the localized maximum value ( $x \approx 0.2$ ) due to the uncertainty. And then, in Fig.1 (i), the optimization was achieved. We extended this model to sevendimensional parameters to optimize the ALD cycle and six variable parameters in HPT.



Fig. 1. Results of GPR and state of the optimization by BO based on UCB. The orange line and red circles are the virtual true function and the observations, respectively. The black dotted line and gray band show the expected value curve and the uncertainty of the prediction computed by GPR, respectively. The blue arrows show the maximum value of UCB and the experimental condition that is adopted as the next experimental condition. And then, the prediction model is updated by adding the result at the next experimental condition.

## 2.4 Cycle of experiments and computations

Fig. 2 shows a schematic of the experimental process and optimization cycle of fabrication of the  $TiO_x/c-Si$ ,  $TiO_x/SiO_y(H_2O_2)/c-Si$ , and  $TiO_x/SiO_y(SC2)/c-Si$ heterostructures. Before BO, random ALD cycle and HPT conditions were carried out for 10 samples of each structure in the range of the maximum and minimum values of each parameter (Table I). After HPT,  $J_0$  and  $\rho_c$  were measured by QSSPC and Cox-Strack method, respectively. Then  $S_{10}$  was calculated from obtained  $J_0$  and  $\rho_c$  by eq. (1). It should be remarked that  $S_{10}$  neglects the deterioration of the passivation performance by the metallization although we attempted to minimize this effect by employing the Mg interlayer. Those experimental conditions and  $S_{10}$  values were set to initial data. Since there are three kinds of structures prepared by different chemical solution processes, a 3fold number of experiments is required if the parameters are optimized for each structure independently by BO. To obtain the experimental data efficiently, a batch process of ALD and HPT was performed onto the three kinds of structures with different pre-deposition treatments while keeping other experimental conditions the same. After adding the experimental results to the dataset and conducting GPR, UCB values were calculated for each structure. The experimental condition which maximizes UCB value in the three structures was adopted as the next experimental condition. Although this experimental condition is most likely not suitable for improving the performance of other structures, the addition of data will help to expand the search and improve the prediction accuracy of the model. In this way, experiments and computations were sequentially repeated until the experimental condition determined by UCB was unchanged, and thus optimization was completed. By doing this, we can discriminate which pre-deposition treatment is superior while obtaining the optimized condition.



Fig. 2 Schematic of the experimental process and optimization cycle of fabrication of the  $TiO_x/c-Si$ ,  $TiO_x/SiO_y(H_2O_2)/c-Si$ , and  $TiO_x/SiO_y(SC_2)/c-Si$  heterostructures.

#### 3. Experimental results and discussion

Fig. 3 (a) shows the transition of  $S_{10}$  of the TiO<sub>x</sub>/c-Si, TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures. At BO of 12 cycles, the condition determined by UCB was unchanged and thus the optimization is completed. In TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures, the high values of  $S_{10}$  were obtained when the optimization was achieved at only BO of 12 cycles. In case we use the exhaustive search, there are 234375 different combinations of experimental condition when there are 3 kinds of structures, 7 parameters and 5 levels ( $3 \times 5^7 = 234375$ ). In contrast, the optimization was achieved in a significantly fewer number of experiments by BO. When we used the conventional optimization method based on the principle of local control which fixes all other parameters, it possibly leads to a local maximum or minimum value. Meanwhile, if we assume that the objective function of  $S_{10}$ , is the smooth function without singularities in the parameter space of the experimental conditions, we could consider that the global

optimization is achieved by BO.

Fig. 3 (b) shows the transition of the structure which takes the maximum value of UCB, experimental condition, and  $S_{10}$  obtained by practical experiment. Hypothetically, when the structure to take the maximum value of UCB remains unchanged for each experiment, the optimization proceeds in only one structure. Then, returned values of the parameters by BO are not optimized values for the others because they may have a higher value than that of the optimized one. However, as shown in Fig. 3(b), the structure which takes the maximum value of UCB changed for each experiment. This result indicates that even in a non-optimized structure the experiments were performed in the batch process under the condition that had not been performed yet and thus the search progressed. Consequently, we can obtain the optimized condition of the superior structure.



Fig.3 (a) Transition of carrier selectivity  $S_{10}$  of the TiO<sub>x</sub>/c-Si, TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures. The blue dotted line, the green dashed line and the red solid line represent the TiO<sub>x</sub>/c-Si, TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si, and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures, respectively. (b) The transition of the structure which takes the maximum value of UCB, experimental conditions, and  $S_{10}$  obtained by practical experiment.

Fig. 4 shows the expected value curved surfaces of the  $S_{10}$  of TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si as a function of  $T_{\rm HPT}$  and  $p_{\rm H_2}$  at BO of (a) 1, (b) 7 and (c) 12 cycles, respectively. Each figure shows the cross-section from the seven-dimensional space where other parameters were set to the optimized values at that cycle. It is noted that the actual experimental points may not exist on that cross-section because the other parameters are unfixed for each experiment. The expected value curved surface became steeper with the increasing number of cycles, indicating parameters converge on optimized parameter values.

Table II summarizes the optimized conditions and  $S_{10}$  values of the TiO<sub>x</sub>/c-Si, TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si, and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures until BO of 12 cycles. At the optimized condition, the simultaneous reduction of  $J_0$  and  $\rho_c$  is achieved. The optimized  $C_{ALD}$  of TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si is 30 cycles and then the thickness of TiO<sub>x</sub> measured by SE is  $1.97 \pm 0.12$  nm. This thickness suppresses the increase in the resistance of the TiO<sub>x</sub> layer and maintains the high passivation performance and thus obtained high  $S_{10}$ .

On the other hand, there are some phenomena related to HPT such as hydrogen radical generation, radical transportation, and radical diffusion into  $TiO_x$  as well as plasma damage and crystallization of  $TiO_x$ . As regards radical generation, radical generation rate *G* is given as follows:

$$G = k_r N_{H_2} N_e \tag{4}$$

where  $k_r$ ,  $N_{H2}$  and  $N_e$  are reaction rate constant, H<sub>2</sub> density, and electron density, respectively. The increase of  $k_r$ ,  $N_{H_2}$ , and  $N_e$  leads to increasing G and thus raising the production of the radical. It is needed to increase electron temperature for larger  $k_r$ . Lower  $p_{\rm H_2}$  or lower d leads to raising electron temperature. On the other hand, increasing  $p_{\rm H_2}$ and  $R_{\rm H_2}$  needs to increase  $N_{\rm H_2}$ . As for  $N_{\rm e}$ , larger  $P_{\rm RF}$  leads to increase of  $N_{\rm e}$ . In terms of radical transportation, it is necessary to consider  $p_{\rm H_2}$  and  $R_{\rm H_2}$  in order to form a uniform plasma. When  $p_{\rm H_2}$  is too high, the amount of radical incident on the TiO<sub>x</sub> surface may decrease because of the short free-path length of the radical. Meanwhile, as for  $R_{H_2}$  lower value causes unstable plasma, whereas a higher value induces turbulence. Regarding radical diffusion into  $TiO_x$ , it is necessary to consider  $T_{HPT}$  for sufficient diffusion to heterointerface. It was reported that hydrogen easily diffuses into crystalline TiO<sub>x</sub> films at 200 °C [44] and it is consistent with this research. Moreover, sufficient  $t_{\rm HPT}$ is needed for the adequate supply of radical to heterointerface which is necessary for enhancing the passivation performance. Regarding plasma damage, it is needed to consider the ion bombardment and light soaking. It was reported that an increase of the a-Si:H/c-Si interface defect density was observed after plasma processing [45] and lower  $P_{\rm RF}$  or higher  $p_{\rm H_2}$  are needed to decrease the ion bombardment [46]. Moreover, it was reported that the performance of solar cells using TiO<sub>x</sub> deteriorates during light soaking [34]. Therefore, it is desired short  $t_{\rm HPT}$  to reduce plasma damage. In terms of crystallization of TiO<sub>x</sub>, lower  $T_{HPT}$  and short  $t_{HPT}$  are needed to suppress the crystallization of  $TiO_x$  which causes the deterioration of the passivation performance. As above, these phenomena are complexly intertwined via six HPT parameters. Therefore, it is hard to find the optimized conditions by conventional methods. Although optimization can be done based on expert experience and hypothesis, the optimized parameters are likely to be local maximum or minimum. Meanwhile, BO globally optimized the HPT parameters and thus the optimized  $S_{10}$  could be the global maximum within determined parameter dimensions.



Fig.4 The expected value curved surfaces of the  $S_{10}$  of TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si as a function of process temperature and H<sub>2</sub> pressure at BO of (a) 1, (b) 7 and (c) 12 cycles, respectively.

Structure	$C_{ALD}$	$T_{\rm HPT}$	$t_{ m HPT}$	$p_{\mathrm{H_2}}$	$R_{\rm H_2}$	P <sub>RF</sub>	d	<i>S</i> <sub>10</sub>
Silucture	[cycle]	[°C]	[min]	[Pa]	[sccm]	[W] [mm]	[-]	
TiO <sub>x</sub> /c-Si	15	100	0.75	100	70	390	10	13.27
$TiO_x/SiO_y(H_2O_2)/c-Si$	30	200	1.5	200	70	300	20	13.63
TiO <sub>x</sub> /SiO <sub>y</sub> (SC2)/c-Si	30	200	1.5	200	70	300	20	13.63

Table II The conditions which obtained the highest  $S_{10}$  and  $S_{10}$  values of the TiO<sub>x</sub>/c-Si, TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si, and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures until BO of 12 cycles.

Table III The  $S_{\text{eff}}$  (at MCD of  $1 \times 10^{15} \text{ cm}^{-3}$ ),  $J_0$  (at MCD of  $5 \times 10^{15} \text{ cm}^{-3}$ ),  $\rho_c$ ,  $S_{10}$  and  $\eta_{\text{theoretical}}$  of TiO<sub>x</sub>/c-Si, TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and TiO<sub>x</sub>/SiO<sub>y</sub>(SC<sub>2</sub>)/c-Si heterostructures at the condition which obtained the highest  $S_{10}$ .

Stavetyre	$S_{\mathrm{eff}}$	$J_0$	$ ho_{ m C}$	$S_{10}$	$S_{10}^{*}$
Structure	[cm/s]	[fA/cm <sup>2</sup> ]	$[\Omega \cdot cm^2]$	[-]	[-]
TiO <sub>x</sub> /c-Si	20.3	33.3	0.0410	13.27	12.85
$TiO_x/SiO_y(H_2O_2)/c-Si$	10.0	18.5	0.0320	13.63	13.21
TiO <sub>x</sub> /SiO <sub>y</sub> (SC2)/c-Si	11.5	20.7	0.0286	13.63	13.21

It should be remarked that the optimized  $S_{10}$  does not include the deterioration of the passivation performance by the metallization. In order to estimate this effect, we prepared asymmetric samples passivated with a-Si:H at the front side and the stack of TiO<sub>x</sub>/SiO<sub>y</sub> at the rear side. Photoluminescence images were taken before and after the full metallization of the rear side by Al with the Mg interlayer. From the reduction of PL intensity, the increase in  $J_0$  by the metallization was estimated as a factor of 2.6. If we apply this factor,

we could estimate  $S_{10}^*$  including the impact of the metallization.

Table III shows the effective surface recombination velocity ( $S_{eff}$ ),  $J_0$ ,  $\rho_c$ ,  $S_{10}$ , and  $S_{10}^*$  of the TiO<sub>x</sub>/c-Si, the TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si, and the TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures at the condition which obtained the highest  $S_{10}$ . The  $J_0$  values were extracted at minority carrier density (MCD) of 5×10<sup>15</sup> cm<sup>-3</sup>.  $S_{eff}$  of symmetrically coated c-Si is defined as follows:

$$\frac{1}{\tau_{\rm eff}} = \frac{1}{\tau_{\rm bulk}} + \frac{2S_{\rm eff}}{W}$$
(5)

where,  $\tau_{\text{bulk}}$  and W are bulk Si lifetime and wafer thickness of 280 µm, respectively. Here the  $\tau_{\text{bulk}}$  is assumed to be infinite in the calculation since high-quality Si substrates were used. The  $\tau_{\text{eff}}$  at an excess MCD of  $1.0 \times 10^{15}$  cm<sup>-3</sup> was used to calculate  $S_{\text{eff}}$ .  $J_0$  is defined as follows:

$$\frac{1}{\tau_{\rm eff}} - \frac{1}{\tau_{\rm Auger}} = \frac{1}{\tau_{\rm bulk}} + 2J_0 \frac{n}{q n_{\rm i}^2 W} \tag{6}$$

where,  $\tau_{Auger}$ , q,  $n_i$ , and n are Auger lifetime, elementary charge, intrinsic carrier density, and excess MCD, respectively. When  $1/\tau_{eff} - 1/\tau_{Auger}$  is plotted versus n, a straight-line results which have a slope proportional to  $J_0$  [47].

Fig. 5 shows  $1/\tau_{eff} - 1/\tau_{Auger}$  of as-deposited and optimized condition performed each structure as a function of excess MCD. In all of the structures, the  $J_0$  at excess MCD of 5  $\times 10^{15}$  was decreased by HPT. In previous work, hydrogen radicals formed by HPT diffuses to TiO<sub>x</sub>/c-Si and terminates the dangling bonds and thus the chemical passivation

improves [32]. Besides, when TiO<sub>x</sub> is partially reduced, the number of oxygen vacancy increases, and then free electrons are generated [31]. This rise of the electron density leads to the large band bending at TiO<sub>x</sub>/c-Si heterointerface, which can improve field effect passivation and electron selectivity. Compared with the TiO<sub>x</sub>/c-Si heterostructure, low  $J_0$ values are observed for the TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and the TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures. This results from Si-O-Ti bonding by inserting SiO<sub>y</sub> interlayer which enhances the diffusion of Ti and O atoms from TiO<sub>x</sub> to SiO<sub>y</sub>. The difference of  $J_0$  between the TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and the TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures is probably caused by the film density of SiO<sub>y</sub> interlayer depends on chemicals. In terms of  $S_{10}$ , however, both of them take almost the same value, indicating that carrier selectivity is not mainly dominated by the structure of the SiO<sub>y</sub> interlayers but also by HPT condition.

Fig. 6 shows the difference between total resistance ( $R_T$ ) and spreading resistance ( $R_s$ ) as a function of contact area (S). The  $\rho_c$  is defined as follows:

$$R_{\rm T} - R_{\rm S} = \frac{\rho_c}{s} + R_0 \tag{7}$$

where  $R_0$  is residual resistance. The relatively low  $\rho_c$  values of the TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and the TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures can be achieved. These results indicate Fermi-level depinning thanks to their high passivation performance. On the other hand, the  $\rho_c$  value of TiO<sub>x</sub>/c-Si is high due to the Fermi energy pinning which is known to be pinned at the defect level at the heterointerfaces.

The  $\eta_{\text{theoretical}}$  is calculated by the equation as follows [35]:

$$\eta_{\text{theoretical}} = ((2.452 \, S_{10} - 4.240)^{-19.52} + (29.21)^{-19.52})^{-\frac{1}{19.52}}.$$
 (8)

In the TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and the TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures, the highest  $\eta_{\text{theoretical}}$  of 27.59% was obtained by using  $S_{10}^*$ . In addition, low thermal budget thanks to short process time and low process temperature suppresses causing phase transformation and crystallization of TiO<sub>x</sub>. Therefore, this fabrication process of TiO<sub>x</sub>/SiO<sub>y</sub>/c-Si heterostructure is desirable to apply SHJ solar cells and the high PCE could be expected.



Fig. 5 The  $1/\tau_{eff} - 1/\tau_{Auger}$  of as-deposited and after optimized HPT of (a) TiO<sub>x</sub>/c-Si, (b) TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si and (c) TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures as a function of excess minority carrier density.



Fig. 6 The difference between total resistance ( $R_T$ ) and spreading resistance ( $R_s$ ) of TiO<sub>x</sub>/c-Si, TiO<sub>x</sub>/SiO<sub>y</sub>(H<sub>2</sub>O<sub>2</sub>)/c-Si, and TiO<sub>x</sub>/SiO<sub>y</sub>(SC2)/c-Si heterostructures performed optimized process as a function of contact area (S).

## 4. Conclusion

We applied BO to optimize the fabrication process of the ALD-TiO<sub>x</sub>/SiO<sub>y</sub>/c-Si heterostructure to improve the performance for passivating contacts. We attempted to optimize three kinds of chemical solution before deposition of TiO<sub>x</sub>, ALD cycle, and HPT parameters: process temperature, process time, H<sub>2</sub> pressure, H<sub>2</sub> flow rate, RF power and electrode distance. At BO of 12 cycles, the condition determined by UCB was unchanged and thus the optimization is achieved. Although we need to consider the deterioration of the passivation by the metallization, we could conclude that BO is useful to optimize the experimental conditions which has multidimensional parameter space. Fine tuning of the conditions starting with the optimized conditions by BO, we could expect realization of high efficiency SHJ solar cells utilizing TiO<sub>x</sub>.

# Data Availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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