

# Numerical study on laminar burning velocity and ignition delay time of ammonia flame with hydrogen addition

Jun Li <sup>a</sup>, Hongyu Huang <sup>b,c\*</sup>, Noriyuki Kobayashi <sup>a,\*</sup>, Chenguang Wang <sup>b,c</sup>, Haoran Yuan <sup>b,c</sup>

<sup>a</sup> Department of Chemical Engineering, Nagoya University, Nagoya, Aichi 464-8603, Japan

<sup>b</sup> Guangzhou Institute of Energy Conversion, Chinese Academy of Sciences, Guangzhou 510640, China

<sup>c</sup> Guangdong Key Laboratory of New and Renewable Energy Research and Development, Guangzhou 510640, China

## Corresponding author

\*Hongyu Huang, Tel.: +86 2037210762. Fax: +86 2087013240

E-mail address: [huanghy@ms.giec.ac.cn](mailto:huanghy@ms.giec.ac.cn)

\*Noriyuki Kobayashi, Tel.: +81 0527892733. Fax: +81 0527895428

E-mail address: [kobayashi@energy.gr.jp](mailto:kobayashi@energy.gr.jp)

## ABSTRACT

This study focuses on the application of NH<sub>3</sub> as a carbon-free alternative fuel in internal combustion devices. The two key parameters for fuel combustion, namely, laminar burning velocity and ignition delay time of the NH<sub>3</sub> flame at various H<sub>2</sub> blending levels, are numerically investigated. Results show that the selected modified Dagaut-Kéromnès mechanism is acceptable and repeatable for calculating the burning velocity and ignition delay time of NH<sub>3</sub>-air flame at various H<sub>2</sub> addition conditions. H<sub>2</sub> addition increases the reactivity of NH<sub>3</sub> combustion at all conditions and enhances the burning velocity. This enhancement is mainly due to chemical effect caused by the reduction in chemical activation energy and the transport effect resulting from the high mobility of H<sub>2</sub>. Furthermore, an increase in pressure and H<sub>2</sub> addition ratios can significantly decrease the ignition delay time of NH<sub>3</sub> mixtures and promote NH<sub>3</sub> ignition. The enhancement of H<sub>2</sub> addition on NH<sub>3</sub> ignition and laminar burning velocity is mainly attributed to the

contribution of the three following reactions:  $O + H_2 = OH + H$ ,  $H + O_2 = OH + O$ , and  $H_2 + OH = H_2O + H$ . These reactions can significantly increase the concentration of free radicals and accelerate the peak of radicals.

Keywords: laminar burning velocity; ignition delay time; ammonia flame; hydrogen addition

## 1. Introduction

In recent decades, the study of alternative and clean fuels has attracted increasing attention with the depletion of fossil fuels and strengthening of pollutant emission regulations [1,2]. One of the prospective alternative fuels is NH<sub>3</sub> [3]. NH<sub>3</sub> is recognized as one of the most promising alternative fuels demonstrating the following favorable properties: (a) free of CO<sub>2</sub>, SO<sub>x</sub>, and soot emission because no carbon is present in this fuel [3–5]; (b) synthesized from fossil fuels (e.g., petroleum, coal, and natural gas), or renewable sources (such as wind, solar, hydropower, and biomass) [5–7]; and (c) easily and economically stored and transported in the liquid phase in large quantities via NH<sub>3</sub> tanks, trucks, ships and pipelines [5–7]. Therefore, NH<sub>3</sub> has become a key alternative fuel candidate. NH<sub>3</sub> has been utilized in specific energy devices, such as industry gas turbines and gas engines operated at high pressure and temperature [8,9].

As a fundamental property for fuel combustion in practical energy devices, laminar burning velocity is determined by the combined properties of diffusivity, exothermicity, and reactivity of a fuel. The laminar burning velocity is a key parameter to describe flame stabilization, extinction limits, flame structures, and velocity [10–12]. Unfortunately, the burning velocity of NH<sub>3</sub> is usually low around 5–13 cm/s [6,7,13]. This low value obstructs its application in specific energy devices. NH<sub>3</sub> combustion at various conditions, such as dual fuel with H<sub>2</sub> [7,14–18] and CH<sub>4</sub> [19–21]with high burning velocity, preheating condition [9,22, 23] from exhaust heat, and O<sub>2</sub>-enriched condition [24,25], has been investigated to improve the laminar burning velocity of NH<sub>3</sub>. Lee et al [16] investigated the burning velocity and emission characteristics of NH<sub>3</sub> with H<sub>2</sub> addition ratio from 0% to 50%. They found that the laminar burning velocity substantially increases with H<sub>2</sub> addition, and low NO<sub>x</sub> formation occurs at fuel-rich conditions. Li et al. [17]

experimentally studied the combustion characteristics and NO<sub>x</sub> formation of NH<sub>3</sub>-H<sub>2</sub> combustion with H<sub>2</sub> ratio from 33.3 % to 60.0 %. The laminar burning velocity improved to a favorable level, similar to CH<sub>4</sub>; whereas NO<sub>x</sub> emission should be further treated when NH<sub>3</sub> is used as a fuel. The laminar burning velocities of pure NH<sub>3</sub> combustion at preheating and O<sub>2</sub>-enriched conditions have also been studied by Li et al. [23,25]. Preheating temperature and O<sub>2</sub> enrichment positively affect the laminar burning velocity of NH<sub>3</sub> because of the high reaction rate and free radical formations. Furthermore, NO reacts with NH<sub>x</sub> radicals and leads to low NO formation. Reducing NO emission in NH<sub>3</sub>-air combustion is also observed.

Ignition delay time is another key property for fuel combustion in practical energy devices. It is a significant validation parameter in the development of chemical kinetics. The ignition delay time directly determines the ignition of fuel in practical energy devices. The fuel ignition process is recognized as zero-dimensional and homogeneous in a standard shock tube measurement facility. For NH<sub>3</sub> combustion, the ignition temperature and ignition energy of NH<sub>3</sub> are high and limit the application of NH<sub>3</sub> as a practical fuel. Therefore, the studies on the ignition characteristics of NH<sub>3</sub> and the enhancement of NH<sub>3</sub> ignition are necessary. Many studies [26–32] on application of NH<sub>3</sub> in compression-ignition and spark-ignition engines have been reported. However, previous experiments showed shortage with poor ignition property of NH<sub>3</sub>. Additionally, little work has been conducted on the ignition delay time of NH<sub>3</sub> [33] and enhancement of NH<sub>3</sub> ignition. However, the fundamental key properties of NH<sub>3</sub>, such as burning velocity, auto-ignition temperature, and minimum ignition energy are far apart with H<sub>2</sub>, methanol, and gasoline as shown in Table 1 [30,31]. The burning velocity of NH<sub>3</sub> is only approximately 0.42% of H<sub>2</sub> (3.51 m/s), and the minimum ignition energy is 4440 times of H<sub>2</sub> (0.0018 mJ). By mixing with H<sub>2</sub>, it is possible for NH<sub>3</sub> to present promising properties at suitable H<sub>2</sub> addition ratios. Furthermore, the kinetic of NH<sub>3</sub> combustion at various H<sub>2</sub> addition conditions remains also unclear and needs further investigation. Thus, studies on the laminar burning velocity and ignition delay time of NH<sub>3</sub> combustion are still rare and worthwhile.

This study aims to evaluate the kinetic models of NH<sub>3</sub> combustion, investigate the laminar burning

velocity at various H<sub>2</sub> addition ratios (up to 90%), calculate the ignition delay time of NH<sub>3</sub> flames at various conditions, and discuss the effect of H<sub>2</sub> addition on the chain reaction mechanism, laminar burning velocity. The results will be used to provide a fundamental database and a favorable method for the enhancement of NH<sub>3</sub> combustion in practical energy devices.

## 2. Numerical simulations

The laminar burning velocity is simulated by a freely propagating adiabatic, premixed, laminar flame speed calculation model [34] in CHEMKIN 4.0. The hybrid time-integration/Newton-iteration technique with adaptive meshes and mixture-averaged transport parameters is applied to solve the steady-state mass, species and energy conservation equations of the flames; this technique has been described in detail in previous studies [22,23,25]. The inlet gas molar fractions for laminar burning velocity calculation at various H<sub>2</sub> addition ratios are summarized in Tables S1–S6 in Appendix A1. Estimated values for the initial, intermediate and production fractions along with temperature profiles are set before the simulations. The final solution is obtained at adaptive grid control based on the solution gradient and curvature (GRAD and CURV) set as 0.01 and 0.05, respectively. These values are sufficiently accurate for our results. The burning velocity is calculated with Soret effect using multicomponent transport method in CHEMKIN [34], which is shown as following equation based on Metghalchi and Kech power-low relation [25,35]:

$$S_u = S_{u0} \left( \frac{T_u}{T_0} \right)^\alpha \left( \frac{p}{p_0} \right)^\beta$$

where  $S_u$  is the laminar burning velocity (cm/s),  $T_u$  and  $p$  is the unburned temperature (K) and pressure (atm),  $S_{u0}$ ,  $\alpha$ , and  $\beta$  are constants, and the subscript 0 represents the standard state.

The ignition delay time is calculated using CHEMKIN package. A homogeneous charge compression-ignition model is selected for the simulations. A wide range of engine related conditions is investigated with pressure from 1.4 atm to 30 atm, temperature from 1500 K to 2500 K, and equivalence ratio from 0.5 to 2.0. The calculated ignition delay time of  $\tau_{\text{NH}_2}$  and  $\tau_{\text{OH}}$  is defined as the time interval between zero to the maximum molar fraction of NH<sub>2</sub>, and OH radical. The ignition process is calculated by

constraining pressure and solving the energy equation. The end ignition time is set as 0.5s, which is quite enough for the ignition process. The initial temperature and pressure, along with the inlet gas composition, are set at the beginning of simulations. The inlet gas compositions for calculating the ignition delay time of NH<sub>3</sub> flames at various H<sub>2</sub> addition ratios are summarized in Table S7 in Appendix A2.

Three mechanisms are employed in this research, namely, modified Dagaut–Kéromnès (DK) mechanism [36,37], Millar–Bowman (MB) mechanism [38], and Reductive Konnov (RE) mechanism [39]. There are 43 species and 271 elementary reactions containing 40 elementary reactions for H<sub>2</sub>/CO chemistry from Kéromnès [37] in the DK mechanism. The replacement of H<sub>2</sub>/CO chemistry from Kéromnès is proved to improve the prediction for the ignition delay time and laminar burning velocity of NH<sub>3</sub> for involving mixture with H<sub>2</sub> and O<sub>2</sub>. The DK mechanism can simulate the oxidation of NH<sub>3</sub>, H<sub>2</sub>, and carbon monoxide at elevated temperature and pressure conditions. The MB mechanism is a C4 kinetic model (including 58 species and 255 elementary reactions) in which the NH<sub>3</sub> oxidation reaction developed by Sandia National Laboratories and Stanford University is considered, which has confirmed to be a significant mechanism for NH<sub>3</sub> oxidation process during hydrocarbon combustion. The RE mechanism is a NH<sub>3</sub>/H<sub>2</sub> kinetic model with 19 species and 80 elementary reactions established by the Université Catholique de Louvain. The RE mechanism was developed from reduction of Konnov mechanism, those small quantities (<10<sup>-8</sup> mole fraction) and not necessary species for the formation and decomposition of main species are removed to obtain RE mechanism with only 19 species and 80 elementary reactions. These three mechanisms have been validated and added in Appendices B1–B3.

### 3. Results and discussion

#### 3.1 Laminar burning velocity

Fig. 1 shows the burning velocity of NH<sub>3</sub>-air flame at various H<sub>2</sub> addition ratios ( $X_{H_2}$ ) and equivalence ratios of (a) 0.80, (b) 1.00, and (c) 1.25. The simulated results in this study by the DK and RE mechanisms are compared with the measured results by Lee et al. [16], Li et al. [17], Lindstedt [40],

Kumar [41], and Ichikawa [42], as well as the simulated results by Li et al. [22, 23] with the MB mechanism [38]. Fig. 1 shows that the simulated results are in good agreement with previous findings. Meanwhile, Li et al. [25] found that the calculated laminar burning velocity based on the RE mechanism is larger than measured results but consistent with the previously predicted values for NH<sub>3</sub>-air flame. The laminar burning velocity of NH<sub>3</sub>-air flame by the DK mechanism in this study shows better agreement with those measured results than the RE mechanism at all H<sub>2</sub> addition and equivalence ratio ranges. Particularly, at equivalence ratio of 1.00, the predicted burning velocity under DK mechanism match more closely with experimental data (within ~15%) than that of RE mechanism (10%~98%) under all H<sub>2</sub> addition conditions, same tendency is also observed at fuel lean and fuel rich conditions. Therefore, this agreement in burning velocity confirms that the selected DK mechanism is acceptable and repeatable for calculation of the burning velocity of NH<sub>3</sub>-air flame at various H<sub>2</sub> addition conditions.

Fig. 2 shows the calculated laminar burning velocity of NH<sub>3</sub>-air flame as a function of  $\phi$ , with X<sub>H<sub>2</sub></sub> as a parameter. The values of the laminar burning velocity of NH<sub>3</sub>-air flame as a function of  $\phi$  at various X<sub>H<sub>2</sub></sub> are shown in Table S8 in Appendix C. The burning velocity of NH<sub>3</sub>-air flame for X<sub>H<sub>2</sub></sub> is used as the reference line. With increasing H<sub>2</sub> addition, thereby increasing X<sub>H<sub>2</sub></sub>, the laminar burning velocity increases as expected. Previous studies suggested that the laminar burning velocity has linear correlations with certain key radicals [25]. The laminar burning velocity of hydrocarbon and hydrogen fuel is linearly correlated with H and OH radicals [25,43]. However, the laminar burning velocity of NH<sub>3</sub> is linearly correlated with NH<sub>2</sub> radical [25], which differs from that of hydrogen and hydrocarbon fuels. Therefore, the burning velocity of NH<sub>3</sub>-air flame blending with H<sub>2</sub> can be correlated quasi-linearly with (NH<sub>2</sub>+H+OH)<sub>max</sub>, as shown in Fig. 3. This correlation is expressed as follows.

$$S_u = k * (NH_2 + H + OH)_{max} \text{ cm/s}$$

where k is the slope, which represents the sensitivity of the laminar burning velocity of NH<sub>3</sub>-air flame to the maximum mole fraction of (NH<sub>2</sub>+H+OH) in the flame and equals 3758.5.

The laminar burning velocity of NH<sub>3</sub>-air flame increases with the increase in X<sub>H<sub>2</sub></sub>. H<sub>2</sub> addition with X<sub>H<sub>2</sub></sub> = 0.3 shows a 192% increase in burning velocity (from 3.96 cm/s at pure NH<sub>3</sub> condition to 11.55 cm/s at X<sub>H<sub>2</sub></sub> = 0.3) at  $\phi$  of 0.8, whereas 169% (from 6.83 cm/s at pure NH<sub>3</sub> condition to 18.37 cm/s at X<sub>H<sub>2</sub></sub> = 0.3) and 198% increases (from 6.62 cm/s at pure NH<sub>3</sub> condition to 19.71 cm/s at X<sub>H<sub>2</sub></sub> = 0.3) are found at  $\phi$  of 1.0 and 1.25, respectively. These effects can be considered as thermal because the increase in adiabatic flame temperature (as shown in Fig. 4), chemical because the reduction in chemical activation energy, and transport because of the high mobility of H<sub>2</sub>. The thermal effect  $\Delta S_{u,\text{therm}}$  and chemical effect  $\Delta S_{u,\text{chem}}$  of H<sub>2</sub> addition on the laminar burning velocity can be defined as follows [44–46]:

$$\Delta S_{u,\text{therm}} = \frac{S_{u,T}(X_{H_2}) - S_u(X_{H_2} = 0)}{S_u(X_{H_2}) - S_u(X_{H_2} = 0)}$$

$$\Delta S_{u,\text{chem}} = \frac{S_{u,C}(X_{H_2}) - S_u(X_{H_2} = 0)}{S_u(X_{H_2}) - S_u(X_{H_2} = 0)}$$

Therefore, the transport effect of H<sub>2</sub> addition on the laminar burning velocity can be expressed as:

$$\Delta S_{u,\text{tran}} = 1 - \Delta S_{u,\text{therm}} - \Delta S_{u,\text{chem}}$$

where,  $\Delta S_{u,\text{therm}}$ ,  $\Delta S_{u,\text{chem}}$ , and  $\Delta S_{u,\text{tran}}$  are the thermal, chemical, and transport effects of H<sub>2</sub> addition on the laminar burning velocity respectively;  $S_u(X_{H_2} = 0)$  is the laminar burning velocity of pure NH<sub>3</sub> as a modified baseline fuel mixture;  $S_u(X_{H_2})$  is the laminar burning velocity of NH<sub>3</sub> at H<sub>2</sub> addition of X<sub>H<sub>2</sub></sub>;  $S_{u,T}(X_{H_2})$  is the laminar burning velocity of NH<sub>3</sub> at H<sub>2</sub> addition of X<sub>H<sub>2</sub></sub> caused by the thermal effect, which is calculated by replacing part of nitrogen into argon to increase the baseline flame temperature; and  $S_{u,C}(X_{H_2})$  is the laminar burning velocity of NH<sub>3</sub> at H<sub>2</sub> addition of X<sub>H<sub>2</sub></sub> caused by the chemical effect, which is calculated by replacing part of nitrogen into CO<sub>2</sub> to decrease the H<sub>2</sub>-added NH<sub>3</sub> flame temperature to the baseline flame temperature. The thermal, chemical, and transport effects of H<sub>2</sub> addition on the laminar burning velocity of NH<sub>3</sub>-air flame at various X<sub>H<sub>2</sub></sub> are shown in Fig. 5. The thermal, chemical, and transport effects of H<sub>2</sub> addition all contribute to the enhancement in the laminar burning velocity. The laminar burning velocity enhancement of NH<sub>3</sub>-air flame caused by the chemical and transport

effects is about 10 times of that by the thermal effect. Furthermore, at low H<sub>2</sub> addition ratios, the chemical effect plays a dominant role. The transport effect increases with rising H<sub>2</sub> addition ratios. Both the chemical and transport effects are the main reasons for the burning velocity enhancement at high H<sub>2</sub> addition ratios. High reactivity and mobility of H<sub>2</sub> lead to high chemical and transport effects. Similar results are obtained at fuel-lean ( $\phi$  of 0.8) and fuel-rich conditions ( $\phi$  of 1.25).

Results of sensitivity analysis of key elementary reactions that contribute to the enhancement of the laminar burning velocity of NH<sub>3</sub>-air flame at various H<sub>2</sub> addition ratios are shown in Fig. 6. The sensitivities of elementary reactions of R235: O + H<sub>2</sub> = OH + H and R239: H<sub>2</sub> + OH = H<sub>2</sub>O + H increase significantly with H<sub>2</sub> addition ratios. The most important elementary reaction of H<sub>2</sub> addition on laminar burning velocity of NH<sub>3</sub>-air flame is R236: H + O<sub>2</sub> = OH + O. The sensitivity coefficient of R236 is non-monotonically changed with X<sub>H<sub>2</sub></sub>, whereas, the sensitivity of R235: O + H<sub>2</sub> = OH + H, and R239: H<sub>2</sub> + OH = H<sub>2</sub>O + H on the laminar burning velocity of NH<sub>3</sub>-air flame emerges at X<sub>H<sub>2</sub></sub> of 0.3 and increases with increasing X<sub>H<sub>2</sub></sub>. The acceleration of R235, R236, and R239 with H<sub>2</sub> addition can enhance H, O, and OH radicals, which are crucial to the NH<sub>3</sub> decomposition reaction. The following three reactions are necessary to form NH<sub>2</sub> radical:



The enhancement of NH<sub>3</sub> decomposition is directly related to the burning velocity improvement of NH<sub>3</sub>. According to previous discussions on NH<sub>3</sub> combustion at preheating and O<sub>2</sub>-enriched conditions, the enhancement of H abstraction of NH<sub>3</sub> attacked by O, H, OH, and M radicals is caused by thermal decomposition reactions, which can also be proven to increase the burning velocity of NH<sub>3</sub> flame [22,23,25]. Therefore, R235: O + H<sub>2</sub> = OH + H, R236: H + O<sub>2</sub> = OH + O, and R239: H<sub>2</sub> + OH = H<sub>2</sub>O + H are most sensitive reactions on the burning velocity of NH<sub>3</sub>-air flame with H<sub>2</sub> addition.

### *3.2 Ignition delay time*

#### *3.2.1 Ignition delay time validation*

As a key parameter of fuel combustion in energy devices, the ignition delay time of NH<sub>3</sub> flame during the NH<sub>3</sub> auto-ignition process in a closed homogeneous batch reactor at various X<sub>H<sub>2</sub></sub> conditions is calculated. Figs. 7(a)–7(c) show comparisons between the experimental data [33] and numerical results of the ignition delay time based on NH<sub>2</sub> and OH radical using the DK, MB, and RE mechanisms at equivalence ratios of 0.5, 1.0, and 2.0, respectively. Fig. 7 shows that the predicted ignition delay of the NH<sub>3</sub>-O<sub>2</sub> mixture for each mechanism differs over all temperature and equivalence ratio ranges and has a maximum difference of up to one order of magnitude. Among these mechanisms, the ignition delay time of the DK mechanism based on NH<sub>2</sub> radical can be predicted well with the experimental data by Mathieu and Petersen [33] compared with that of the MB and RE mechanisms. Particularly, at equivalence ratio of 1.00, the predicted ignition delay time ( $\tau_{\text{NH}_2}$ ) under DK mechanism match more closely with experimental data (within ~14%) than that at RE mechanism (approximately 40%~70%) under all H<sub>2</sub> addition conditions, same tendency is also observed equivalence ratios of 0.5 and 2.0. Therefore, the DK mechanism is selected for the following ignition delay discussion. The specific selection of the DK mechanism does not alter the generality of the discussion. In other words, the main and controlling reactions for NH<sub>3</sub> ignition are the same, whereas the kinetic parameters are different from other mechanisms.

For the fuel-lean and stoichiometric conditions as shown in Fig. 7(a) and 7(b), the simulated results agree well with the experimental data [33]. For the fuel-rich condition shown in Fig. 7(c), the simulated results are one or two times larger than the experimental data [33]. Although the selected kinetic mechanism can predict the laminar burning velocity and ignition delay time for almost all operating conditions, its ability to predict the ignition delay time for NH<sub>3</sub> combustion is less reliable at fuel-rich conditions.

#### *3.2.2 Ignition delay time at various hydrogen addition*

Fig. 8(a)–8(c) show the effect of H<sub>2</sub> addition on the ignition delay time for the NH<sub>3</sub>-O<sub>2</sub> mixture diluted in 99% at various  $\phi$  of 0.5, 1.0, and 2.0 respectively. The ignition delay time of NH<sub>3</sub> is dramatically reduced with H<sub>2</sub> addition over all tested conditions. In particular, at a high temperature (1950 K), the reduction in ignition delay time is 93.2% at  $\phi$  of 0.5 and increases to 93.6% and 93.7% at  $\phi$  of 1.0 and 2.0, respectively. Meanwhile, H<sub>2</sub> addition shows a strong effect on activation energy (E<sub>a</sub>) changes (50.3 kcal mol<sup>-1</sup> for X<sub>H<sub>2</sub></sub> = 0, and 17.9 kcal mol<sup>-1</sup> for X<sub>H<sub>2</sub></sub> = 0.9 at  $\phi$  of 1.0 and pressure of 1.4 atm) as shown in Table 1.

Fig. 9 shows the effect of pressure on the ignition delay time for NH<sub>3</sub>-O<sub>2</sub>-Ar mixture at various X<sub>H<sub>2</sub></sub>. The black, red, and blue lines show the simulation results, whereas the dots are the measurement results of NH<sub>3</sub>-O<sub>2</sub>-Ar mixture by Mathieu and Petersen [33] at 1.4, 11, and 30 atm. Fig. 9 shows that an increase in pressure can significantly decrease the ignition delay time of NH<sub>3</sub> mixtures and promote of NH<sub>3</sub> ignition. The addition of H<sub>2</sub> does not change the pressure dependence phenomenon of the NH<sub>3</sub> ignition delay time. Interestingly, the reduction in the ignition delay time with pressure changing from 1.4 atm to 10 atm is more pronounced than that from 10 atm to 30 atm. The reaction rate of the two most significant dominant radicals during NH<sub>3</sub> ignition process (i.e., OH reaction together with elementary reactions of R92: NH<sub>3</sub> + O = NH<sub>2</sub> + OH, R235: O + H<sub>2</sub> = OH + H, and R236: H + O<sub>2</sub> = OH + O for OH radical production, as well as NH<sub>2</sub> reaction together with elementary reactions of R93: NH<sub>3</sub> + OH = NH<sub>2</sub> + H<sub>2</sub>O, R91: NH<sub>3</sub> + H = NH<sub>2</sub> + H<sub>2</sub>, and R92: NH<sub>3</sub> + O = NH<sub>2</sub> + OH for NH<sub>2</sub> production) increases with increasing pressure and H<sub>2</sub> addition ratios (Fig. 10). The enhancement of OH radical can increase unreactive species of NH<sub>3</sub> into reactive NH<sub>2</sub>, NH, and N radicals with H abstraction of NH<sub>3</sub> decomposition. Furthermore, the enhancement in the reaction rate of OH radical from 10 atm to 30 atm is much higher than that from 1.4 atm to 10 atm. This difference leads to a more significant reduction in the ignition delay time. The solid black lines in Fig. 9 shows that the ignition delay time of pure NH<sub>3</sub> decreases with increasing pressure at  $\phi$  ranging from 0.5 to 2.0. The effect of  $\phi$  on the ignition delay time for NH<sub>3</sub>-O<sub>2</sub>-Ar mixture at various H<sub>2</sub> addition ratios and pressure of 1.4 atm is shown in Fig. 11. The solid, dash, and dot lines are the simulation

results at H<sub>2</sub> addition ratios of 0.0%, 50.0%, and 90%, respectively. For pure NH<sub>3</sub> mixture, only a minimal effect is observed when  $\phi$  increases from 0.5 to 2.0. At high X<sub>H<sub>2</sub></sub>, the effect becomes obvious with a change in  $\phi$ . This finding indicates that NH<sub>3</sub> ignition has a strong X<sub>H<sub>2</sub></sub> dependence upon  $\phi$ .

NH<sub>3</sub> ignition is closely related to the H<sub>2</sub> addition ratio, pressure, and equivalence ratio. To quantitatively understand the pressure-dependent behavior in NH<sub>3</sub> ignition, the effect of pressure on the reduction ratio of the ignition delay time at 1950 K and various  $\phi$  of 0.5, 1.0, and 2.0 is shown in Fig. 12(a)–12(c), respectively. Fig. 12 shows that the reduction ratio of the ignition delay time increases with an increase in H<sub>2</sub> addition ratio but decreases with rising pressure at all equivalence ratios. At fuel-lean and stoichiometric conditions, the reduction at high pressure is similar to that at low pressure and shows small pressure-dependent effects. For fuel-rich conditions, the pressure-dependent effects on the ignition delay time become large. To quantitatively understand the equivalence ratio-dependent behavior in NH<sub>3</sub> ignition, the effects of the equivalence ratio on the reduction ratio of the ignition delay time at 1950 K and various pressures of 1.4, 11, and 30 atm is shown in Figs. 13(a)–13(c), respectively. As shown in Fig. 13, the reduction of ignition delay time increase with increasing H<sub>2</sub> addition ration at all equivalence ratio. At lower pressure below 11.0 atm, equivalence ratio effect on the reduction ratio of ignition delay time is similar. Specifically, at same pressure of 11 atm and H<sub>2</sub> addition ration of 0.3, the reduction ratio of ignition delay time reaches 78.6%, 75.7%, and 76.9% at stoichiometric condition, fuel-lean and fuel rich conditions, respectively. At high pressure of 30.0 atm, H<sub>2</sub> addition provides the strongest effect on the reduction ratio of ignition delay time at stoichiometric condition. The reduction ratio of ignition delay time at stoichiometric condition reaches 78.2%, which is about 5% higher than that at fuel-lean (74.2%) and fuel rich (74.7%) conditions at H<sub>2</sub> addition ration of 0.3. However, the reduction at fuel-lean and fuel-rich conditions exhibits similar increasing tendency on NH<sub>3</sub> ignition with H<sub>2</sub> addition.

### 3.2.3 Sensitivity analysis

To further identify the important reactions for NH<sub>3</sub> ignition, sensitivity analysis on the OH radical is

performed at various H<sub>2</sub> addition ratios and pressures. Previous studies showed that sensitivity analysis of OH and NH<sub>2</sub> produces results that are crucial to NH<sub>3</sub> oxidation and combustion [25,33]. Furthermore, the formation of OH free radical is closely related to NH<sub>3</sub> decomposition. Therefore, OH sensitivity analysis is highly similar to sensitivity analysis of the ignition delay time. The dominant reactions from OH radical sensitivity analysis can be assumed as the important reactions for NH<sub>3</sub> ignition.

Fig. 14 shows the results of normalized sensitivity analysis at certain selected conditions. For fuel-lean condition, Figs. 14(a)–14(c) illustrate the results at  $\phi = 0.5$ , 1950 K, and pressure of 1.4, 11, and 30 atm at X<sub>H<sub>2</sub></sub> of 0.0, 0.5, and 0.9, respectively. The two most enhancing reactions are R235: O + H<sub>2</sub> = OH + H, and R236: H + O<sub>2</sub> = OH + O, and the most inhibiting reaction is R239: H<sub>2</sub> + OH = H<sub>2</sub>O + H. These reactions are revealed in sensitivity analysis. Apart from the three most effective reactions, R93: NH<sub>3</sub> + OH = NH<sub>2</sub> + H<sub>2</sub>O, and R98: NH<sub>2</sub> + OH = NH + H<sub>2</sub>O also show important effect on NH<sub>3</sub> ignition at H<sub>2</sub> addition and high pressure conditions.

At stoichiometric conditions, Figs. 14(d)–14(f) show the results at  $\phi = 1.0$ , 1950 K, and pressure of 1.4, 11, and 30 atm at X<sub>H<sub>2</sub></sub> of 0.0, 0.5, and 0.9, respectively. Sensitivity analysis at stoichiometric conditions shows that almost all important reactions are the same or nearly at the same order in terms of normalized sensitivity at fuel-lean conditions. The two most enhancing reactions are R235: O + H<sub>2</sub> = OH + H, and R236: H + O<sub>2</sub> = OH + O, whereas the most inhibiting reaction is R239: H<sub>2</sub> + OH = H<sub>2</sub>O + H. These reactions are similar to the results of sensitivity analysis on burning velocity.

For fuel-rich condition, Figs. 14(g)–14(i) show the results at  $\phi = 2.0$ , 1950 K, and pressure of 1.4, 11, and 30 atm at X<sub>H<sub>2</sub></sub> of 0.0, 0.5, and 0.9, respectively. The reactions of R235: O + H<sub>2</sub> = OH + H, R236: H + O<sub>2</sub> = OH + O, and R239: H<sub>2</sub> + OH = H<sub>2</sub>O + H are the also most important ones based on the results of sensitivity analysis. These reactions can significantly increase the concentration of free radicals and accelerate the peak of H, O, and OH; such events promote NH<sub>3</sub> ignition. The results of this sensitivity analysis show that the most inhibiting reaction of R239: H<sub>2</sub> + OH = H<sub>2</sub>O + H becomes less important,

whereas R93:  $\text{NH}_3 + \text{OH} = \text{NH}_2 + \text{H}_2\text{O}$  becomes dominant; this reaction is the thermal decomposition reaction of  $\text{NH}_3$  (i.e., with involvement of  $\text{NH}_3$  and  $\text{OH}$  radical). The importance of R93:  $\text{NH}_3 + \text{OH} = \text{NH}_2 + \text{H}_2\text{O}$  illustrates some potential advantages at fuel-rich conditions,  $\text{NH}_3$  can be completely consumed and converted to  $\text{H}_2$ , which has also been proved by previous studies [9,25,39].

#### 4. Conclusions

This study focuses on the application of  $\text{NH}_3$  as a carbon-free alternative fuel in internal combustion devices. The laminar burning velocity and ignition delay time of  $\text{NH}_3$  flames at various  $\text{H}_2$  blending levels have been numerically investigated. The main conclusions are summarized as follows:

- (1) The addition of  $\text{H}_2$  from thermal decomposition of  $\text{NH}_3$  increases the reactivity of  $\text{NH}_3$  combustion and enhances the burning velocity of  $\text{NH}_3$ , enabling  $\text{NH}_3$  as a practical fuel in various energy devices.
- (2) The enhancement of burning velocity of  $\text{NH}_3$  is mainly due to the chemical effect caused by the reduction in chemical activation energy and transport effect resulting from the high mobility of  $\text{H}_2$ .
- (3) An increase in pressure and  $\text{H}_2$  addition ratios can significantly decrease the ignition delay time of  $\text{NH}_3$  mixtures and promote of  $\text{NH}_3$  ignition.
- (4) The enhancement of  $\text{H}_2$  addition on  $\text{NH}_3$  ignition and laminar burning velocity is mainly attributed to the three following reactions:  $\text{O} + \text{H}_2 = \text{OH} + \text{H}$ ,  $\text{H} + \text{O}_2 = \text{OH} + \text{O}$ , and  $\text{H}_2 + \text{OH} = \text{H}_2\text{O} + \text{H}$ . These reactions can significantly increase the concentration of free radicals and accelerate the peak of  $\text{H}$ ,  $\text{O}$ , and  $\text{OH}$  radicals.

#### References

- [1] Riaz A, Zahedi G, Klemeš JJ. A review of cleaner production methods for the manufacture of methanol. *J Cleaner Product* 2013;57: 19–37.
- [2] Astbury GR. A review of the properties and hazards of some alternative fuels. *Process Saf Environ* 2008;86: 397–414.

- [3] Zamfirescu C, Dincer I. Using ammonia as a sustainable fuel. *J Power Sources* 2008;185: 459–465.
- [4] Zhao BT, Su YX, Cui GM. Post-combustion CO<sub>2</sub> capture with ammonia by vortex flow-based multistage spraying: Process intensification and performance characteristics. *Energy* 2016;102: 106–117.
- [5] Um DH, Kim TY, Kwon OC. Power and hydrogen production from ammonia in a micro-thermophotovoltaic device integrated with a micro-reformer. *Energy* 2014;73: 531–542.
- [6] Um DH, Joo JM, Lee S, Kwon OC. Combustion stability limits and NO<sub>x</sub> emissions of nonpremixed ammonia-substituted hydrogen-air flames. *Int J Hydrogen Energy* 2013;38: 14854–14865.
- [7] Wang FC, Zhou ZJ, Dai ZH, Gong X, Yu GS, Liu HF, Wang YF, Yu ZH. Development and demonstration plant operation of an opposed multi-burner coal-water slurry gasification technology. *Front Energy Power Eng China* 2007;1: 251–258.
- [8] Verkamp FJ, Hardin MC, Williams JR. Ammonia combustion properties and performance in gas-turbine burners. *Symp (Int) Combust* 1967;11: 985–992.
- [9] Duynslaegher C, Jeanmart H, Vandooren J. Ammonia combustion at elevated pressure and temperature conditions. *Fuel* 2010;89: 3540–3545.
- [10] Aung KT, Hassan MI, Faeth GM. Flame stretch interactions of laminar premixed hydrogen/air flames at normal temperature and pressure. *Combust Flame* 1997;109: 1–24.
- [11] Hu EJ, Li XT, Meng X, Chen YZ, Cheng Y, Xie YL, Huang ZH. Laminar flame speeds and ignition delay times of methane-air mixtures at elevated temperatures and pressures. *Fuel* 2015;158: 1–10.
- [12] Bayraktar H, Durgun O. Investigation the effects of LPG on spark ignition engine combustion and performance. *Energy Convers Manage* 2005;46: 2317–2333.

- [13] Ronney PD. Effect of chemistry and transport properties on near limit flames at microgravity. *Combust Sci Technol* 1988;59: 123–141.
- [14] Kumar P. An experimental and numerical study of NO<sub>x</sub> formation mechanisms in NH<sub>3</sub>-H<sub>2</sub>-Air flam. Iowa State University, 2012.
- [15] Joo JM, Lee S, Kwon OC. Effects of ammonia substitution on combustion stability limits and NO<sub>x</sub> emissions of premixed hydrogen-air flames. *Int J Hydrogen Energy* 2012;37: 6933–6941.
- [16] Lee JH, Kim JH, Park JH, Kwon OC. Study on properties of laminar premixed hydrogen-added ammonia/air flames for hydrogen production. *Int J Hydrogen Energy* 2010;35: 1054–1064.
- [17] Li J, Huang HY, Kobayashi NY, He ZH, Nagai YH. Study on using hydrogen and ammonia as fuels: combustion characteristics and NO<sub>x</sub> formation. *Int J Energ Res* 2014;38: 1214–1223.
- [18] Armjtage JW, Gray P. Flame speeds and flammability limits in the combustion of ammonia: ternary mixtures with hydrogen, nitric oxide, nitrous oxide or oxygen. *Combust Flame* 1965;9:173–184.
- [19] Henshaw PF, D'andrea T, Mann KRC, Ting DSK. Premixed ammonia-methane-air combustion. *Combust Sci Technol* 2005;177:2151–2170.
- [20] Pfahl U J, Ross M C, Shepherd J E, Pasamehmetoglu K O, Unal C. Flammability limits, ignition energy, and flame speeds in H<sub>2</sub>-CH<sub>4</sub>-NH<sub>3</sub>-N<sub>2</sub>O-O<sub>2</sub>-N<sub>2</sub> mixtures. *Combust Flame* 2000;123: 140–158.
- [21] Tian ZY, Li YY, Zhang LD, Glarborg P, Qi F. An experimental and kinetic modeling study of premixed NH<sub>3</sub>/CH<sub>4</sub>/O<sub>2</sub>/Ar flames at low pressure. *Combust Flame* 2009;156: 1413–1426.
- [22] Li J, Huang HY, Yuan HR, Zeng T, Yagami MY, Kobayashi NY. Modeling of ammonia combustion characteristics at preheating combustion: NO formation analysis. *Int J Global Warming* 2016;10: 230–241.

- [23] Li J, Huang HY, Kobayashi NY, He ZH, Zeng T. Research on combustion and emission characteristics of ammonia under preheating conditions. *J Chem Eng Jpn* 2016; 49: 641–648.
- [24] Takeishi H, Hayashi J, Kono S, Iino K, Akamatsu F. Characteristics of ammonia/N<sub>2</sub>/O<sub>2</sub> laminar premixed flame in oxygen-enriched condition. 11th Annual NH<sub>3</sub> Fuel Conference 2014.
- [25] Li J, Huang HY, Kobayashi NY, He ZH, Zeng T. Numerical study on effect of oxygen content in combustion air on ammonia combustion. *Energy* 2015;92: 2053–2068.
- [26] Aaron JR, Song CK. Combustion and emissions characteristics of compression-ignition engine using dual ammonia-diesel fuel. *Fuel* 2011;90: 87–89.
- [27] Boretti AA. Novel heavy duty engine concept for operation dual fuel H<sub>2</sub>-NH<sub>3</sub>. *Int J Hydrogen Energy* 2012;37: 7869–7876.
- [28] Grannell SM, Assanis DN, Bohac SV, Gillespie DE. The fuel mix limits and efficiency of a stoichiometric, ammonia, and gasoline dual fueled spark ignition engine. *J Eng Gas Turbines Power* 2008;130: 1–8.
- [29] Ryu K, Zacharakis-Jutz GE, Kong SC. Effects of gaseous ammonia direct injection on performance characteristics of a spark-ignition engine. *Appl Energy* 2014;116: 206–215.
- [30] MØrch CS, Bjerre AMP, GØttrup SCS, Schramm J. Ammonia/hydrogen mixtures in an SI-engine: Engine performance and analysis of a proposed fuel system. *Fuel* 2011;90: 854–864.
- [31] Liu R., Ting DSK, Checkel D. Ammonia as a fuel for SI engine. SAE Technical Paper 2003;01-3095: 1–7.
- [32] Christopher WG, Song CK. Performance characteristics of a compression-ignition engine using direct – injection ammonia – DME mixtures. *Fuel* 2013;103: 1069–1079.
- [33] Mathieu O, Petersen EL. Experimental and modeling study on the high-temperature oxidation of ammonia and related NO<sub>x</sub> chemistry. *Combust Flame* 2015;162: 554–570.

- [34] Miller JA, Smooke MD, Green RM, Kee RJ. Kinetic modeling of the oxidation of ammonia in flames. *Combust Sci Technol* 1983;34: 149–176.
- [35] Metghalchi M, Keck J C. Burning velocities of mixtures of air with methanol, isoctane, and indolene at high pressure and temperature. *Combust Flame* 1982;48: 191–210.
- [36] Dagaut P, Nicolle A. Experimental and kinetic modeling study of the effect of SO<sub>2</sub> on the reduction of NO by ammonia. *Proc Combust Inst* 2005;30: 1121–1218.
- [37] Kéromnès A, Metcalfe WK, Heufer KA, Donohoe N, Das AK et al. An experimental and detailed chemical kinetic modeling study of hydrogen and syngas mixture oxidation at elevated pressures. *Combust Flame* 2013;160: 995–1011.
- [38] Miller JA, Bowman CT. Mechanism and modeling of nitrogen chemistry in combustion. *Prog Energ Combust Sci* 1989;15: 287–338.
- [39] Duynslaeger C, Jeanmart H, Vandooren J. Flame structure studies of premixed ammonia/hydrogen/oxygen/argon flames: Experimental and numerical investigation. *Proc Combust Inst* 2009;32: 1277–1284.
- [40] Lindstedt RP, Lockwood FC, Selim MA. Detailed kinetic modeling of chemistry and temperature effects on ammonia oxidation. *Combust Sci Tech* 1994;99: 253–276.
- [41] Kumar P, Meyer TR. Experimental and modeling study of chemical-kinetics mechanisms for H<sub>2</sub>-NH<sub>3</sub>-air mixtures in laminar premixed jet flames. *Fuel* 2013;108:166–76.
- [42] Ichikawa AN, Hayakawa AH, Kitagawa YC, Somaratne KDKA, Kudo T, Kobayashi HA. Laminar burning velocity and Markstein length of ammonia/hydrogen/air premixed flames at elevated pressures. *Int. J. Hydrogen Energy* 2015;40:9570–78.
- [43] Zhang W, Chen ZH, Shen YG, Shu GQ, Chen GS, Xu B, et al. Influence of water emulsified diesel & oxygen-enriched air on diesel engine NO smoke emissions and combustion characteristics. *Energy* 2013;55:369–77.

- [44] Wang H, Hahn TO, Sung CJ, Law CK. Detailed oxidation kinetics and flame inhibition effects of chloromethane. *Combust Flame* 1996;105:291–307.
- [45] Li ZS, Han W, Liu D, Chen Z. Laminar flame propagation and ignition properties of premixed iso-octane/air with hydrogen addition. *Fuel* 2015;158:443–450.
- [46] Sung CJ, Huang Y, Eng JA. Effects of reformer gas addition on the laminar flame speeds and flammability limits of n-butane and iso-butane flames. *Combust Flame* 2001;126:1699–713.

## Nomenclature

$\phi$	Equivalence ratio (-)
$X_{H_2}$	$H_2$ addition ratio in $NH_3$ (-)
P	Pressure (atm)
T	Temperature (K)
$S_u$	Laminar burning velocity ( $cm\ s^{-1}$ )
$\Delta S_{u,therm}$	Thermal effect on laminar burning velocity (-)
$\Delta S_{u,chem}$	Chemical effect on laminar burning velocity (-)
$\Delta S_{u,tran}$	Transport effect on laminar burning velocity (-)
$S_u(X_{H_2} = 0)$	Laminar burning velocity of $NH_3$ at $H_2$ addition ratio of 0 ( $cm\ s^{-1}$ )
$S_u(X_{H_2})$	Laminar burning velocity of $NH_3$ at $H_2$ addition ratio of $X_{H_2}$ ( $cm\ s^{-1}$ )
$S_{u,T}(X_{H_2})$	Laminar burning velocity of $NH_3$ at $H_2$ addition of $X_{H_2}$ caused by thermal effect ( $cm\ s^{-1}$ )
$S_{u,C}(X_{H_2})$	Laminar burning velocity of $NH_3$ at $H_2$ addition of $X_{H_2}$ caused by chemical effect ( $cm\ s^{-1}$ )
$\tau_{NH_2}$	Ignition delay time based on maximum molar fraction of $NH_2$ ( $\mu s$ )
$\tau_{OH}$	Ignition delay time based on maximum molar fraction of $OH$ ( $\mu s$ )
$E_a$	Activation energy (kcal mol <sup>-1</sup> )

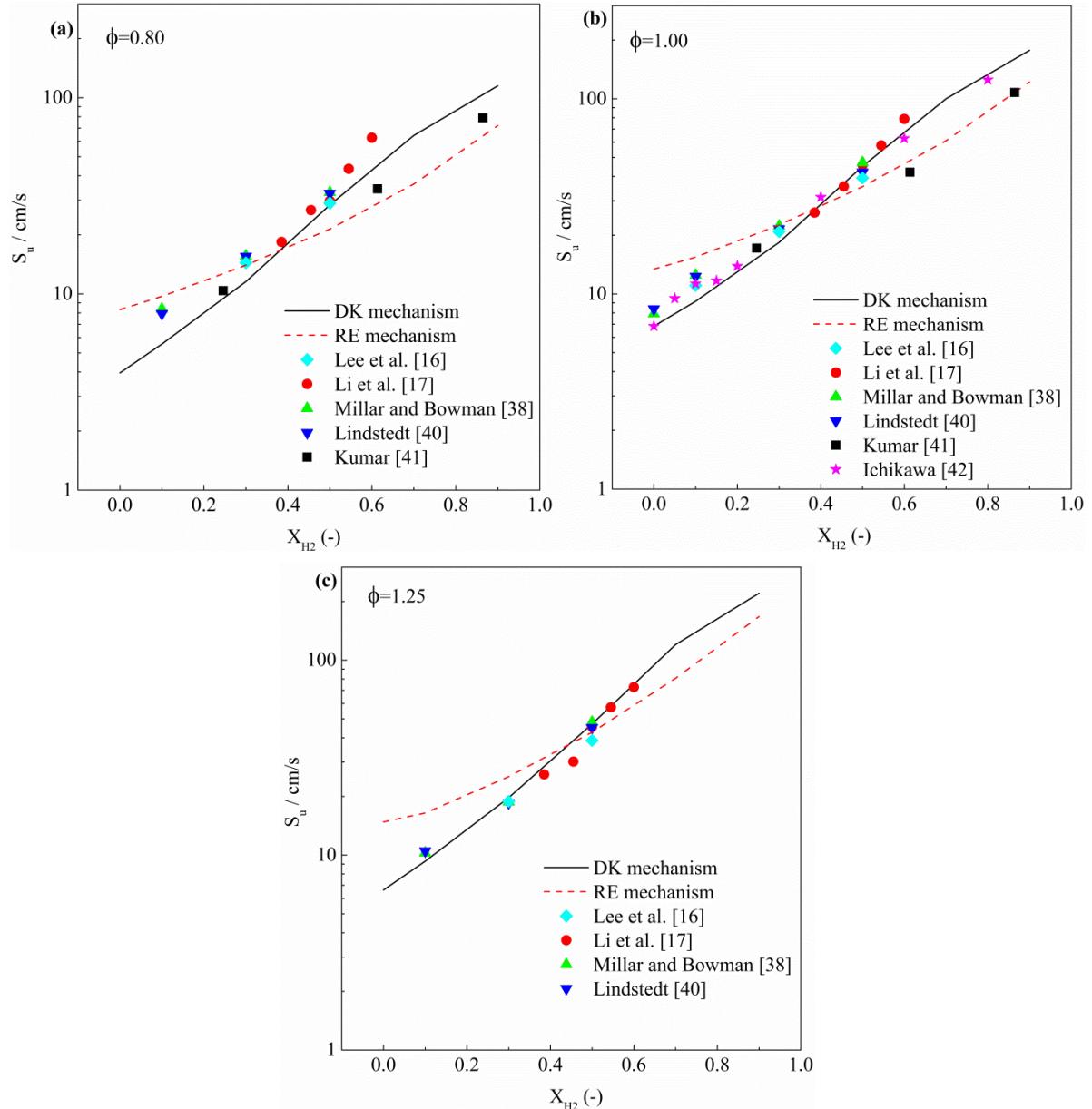
**Table 1.**

Fundamental key properties of various fuels [30,31]

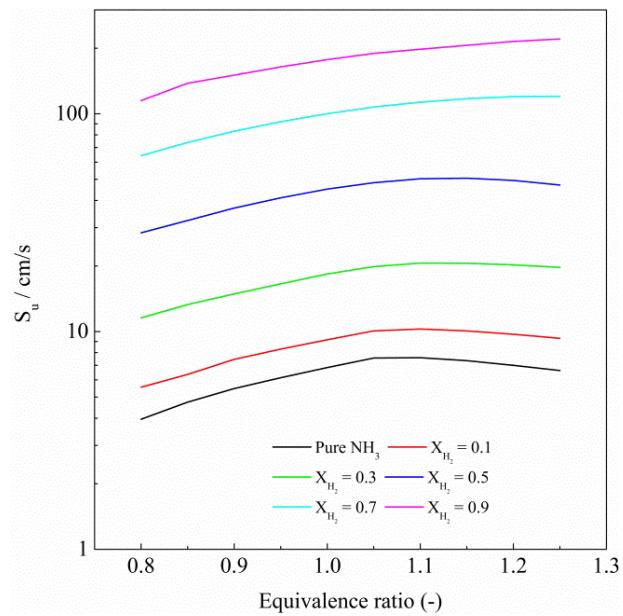
Items	Ammonia	Hydrogen	Methanol	Gasoline
Lower heating value / MJ/kg	18.8	120.1	19.7	44.5
Lower heating value / MJ/L	11.3	8.5	15.5	29.7
Laminar burning velocity / m/s	0.015	3.51	0.50	0.58
Flammability limits, gas in air / vol.%	15-28	4.7-75	6-36	0.6-8
Auto-ignition temperature / °C	651	571	470	230
Minimum ignition energy / mJ	8.0	0.0018	0.14	0.14
Density, 25°C, 1 atm / g/L	0.703	0.082	787	740

**Table 2.**Activation Energy of NH<sub>3</sub>-O<sub>2</sub>-Ar mixtures at various H<sub>2</sub> addition ratio and pressure of 1.4 atm / kcal mol<sup>-1</sup>

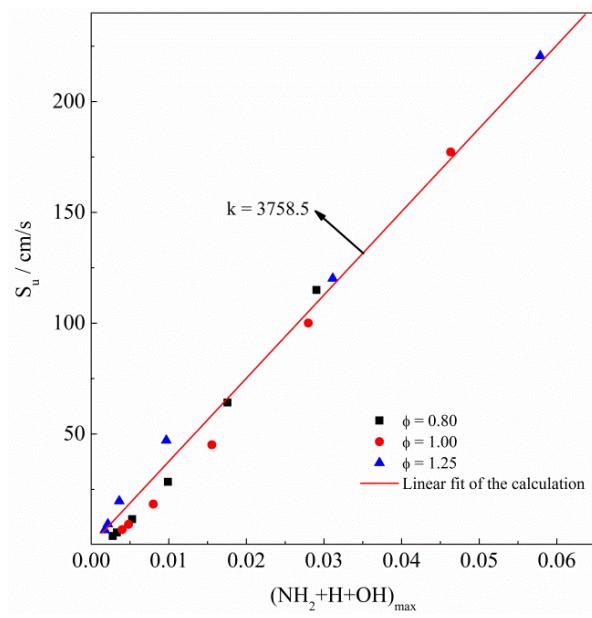
$\phi$	X <sub>H2</sub> / -						
	0.0	0.1	0.3	0.5	0.7	0.9	
Experimental	This work						
data [33]							
0.5	44.6	43.9	36.7	26.7	23.1	19.1	16.8
1.0	51.7	50.3	40.8	30.7	23.7	19.9	17.9
2.0	56.3	55.1	44.7	31.1	26.2	22.7	18.9



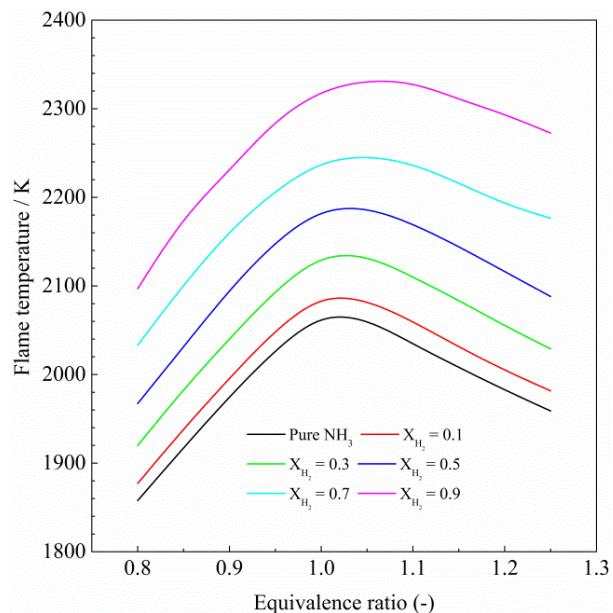
**Fig. 1.** Laminar burning velocity as a function of  $X_{H_2}$  at various equivalence ratios: (a)  $\phi=0.80$ ; (b)  $\phi=1.00$ ; (c)  $\phi=1.25$ . Symbols: Measurements results by Lee et al. [16], Li et al. [17], Millar and Bowman [38], Lindstedt [40], Kumar [41], Ichikawa [42]; Line: Simulated results in this study.



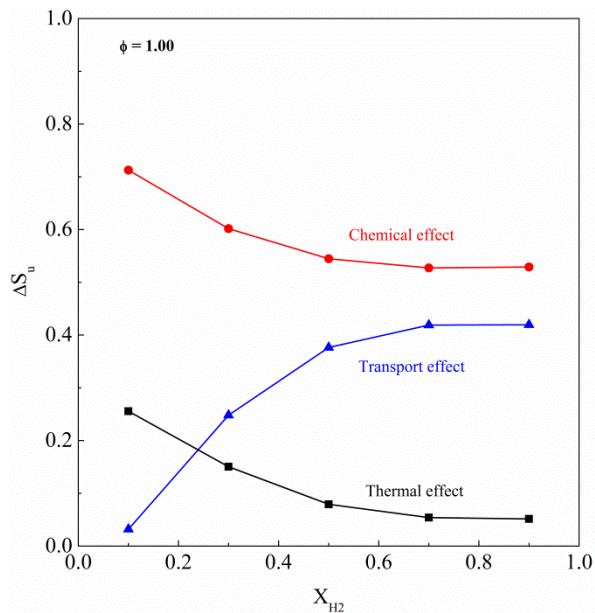
**Fig. 2.** The function of NH<sub>3</sub>-air laminar burning velocity with equivalence ratios at various  $X_{H_2}$ .



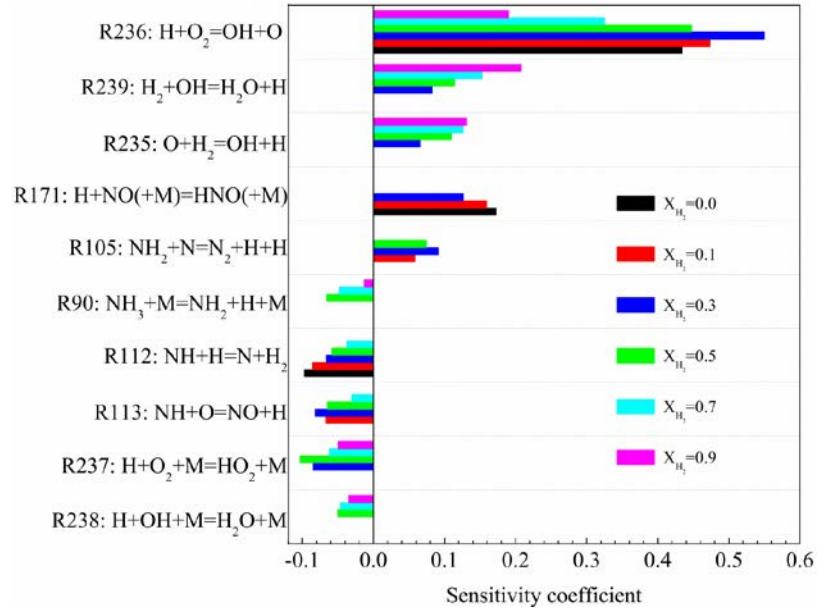
**Fig. 3.** Laminar burning velocity correlation with maximum mole fraction of  $\text{NH}_2+\text{H}+\text{OH}$  radicals.



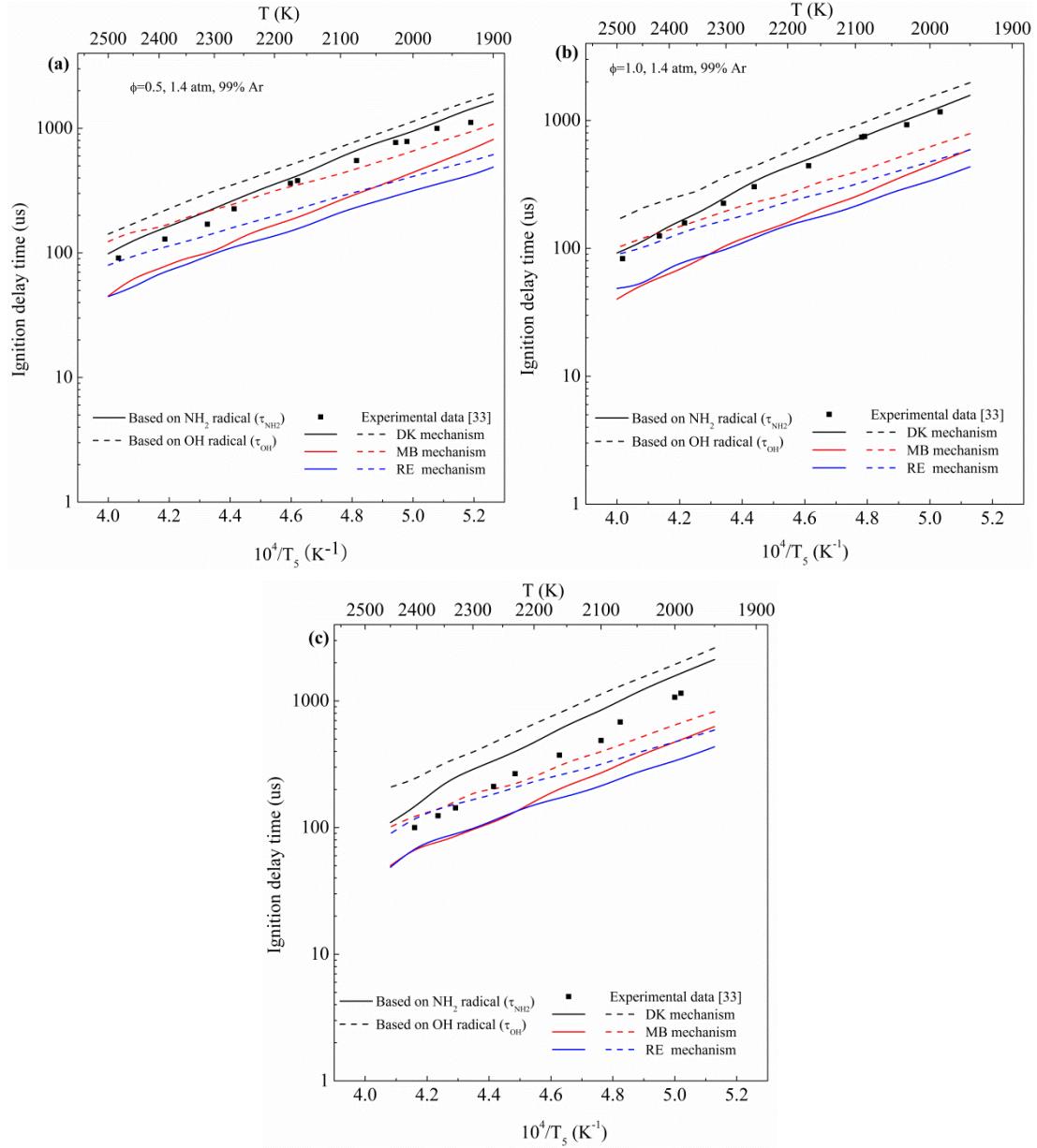
**Fig. 4.** The function of adiabatic flame temperature of  $\text{NH}_3$ -air flame with equivalence ratios at various  $X_{\text{H}_2}$ .



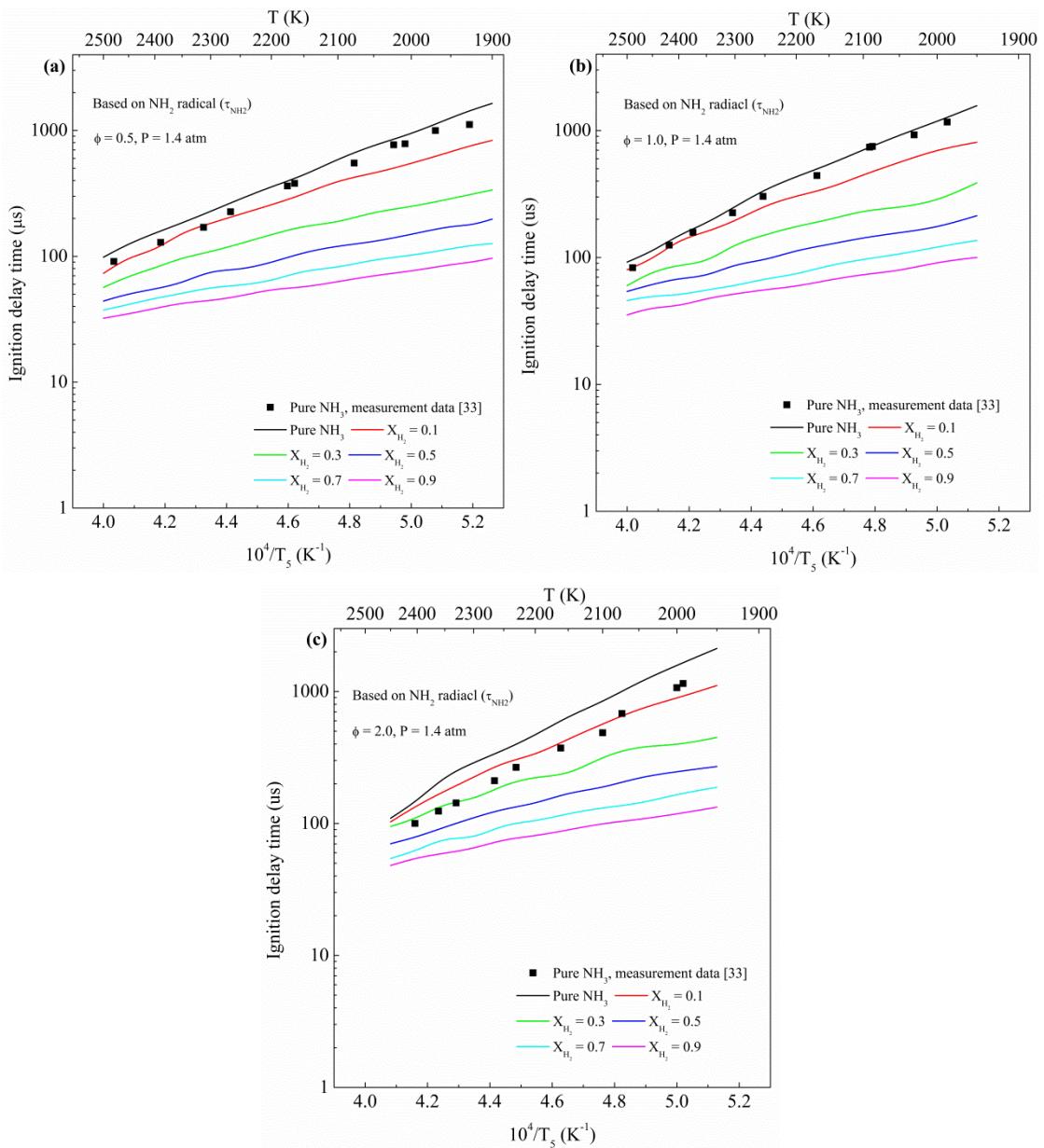
**Fig. 5.** Thermal, chemical, and transport effect of H<sub>2</sub> addition on the laminar burning velocity of NH<sub>3</sub>-air flame ( $\phi=1.0$ ).



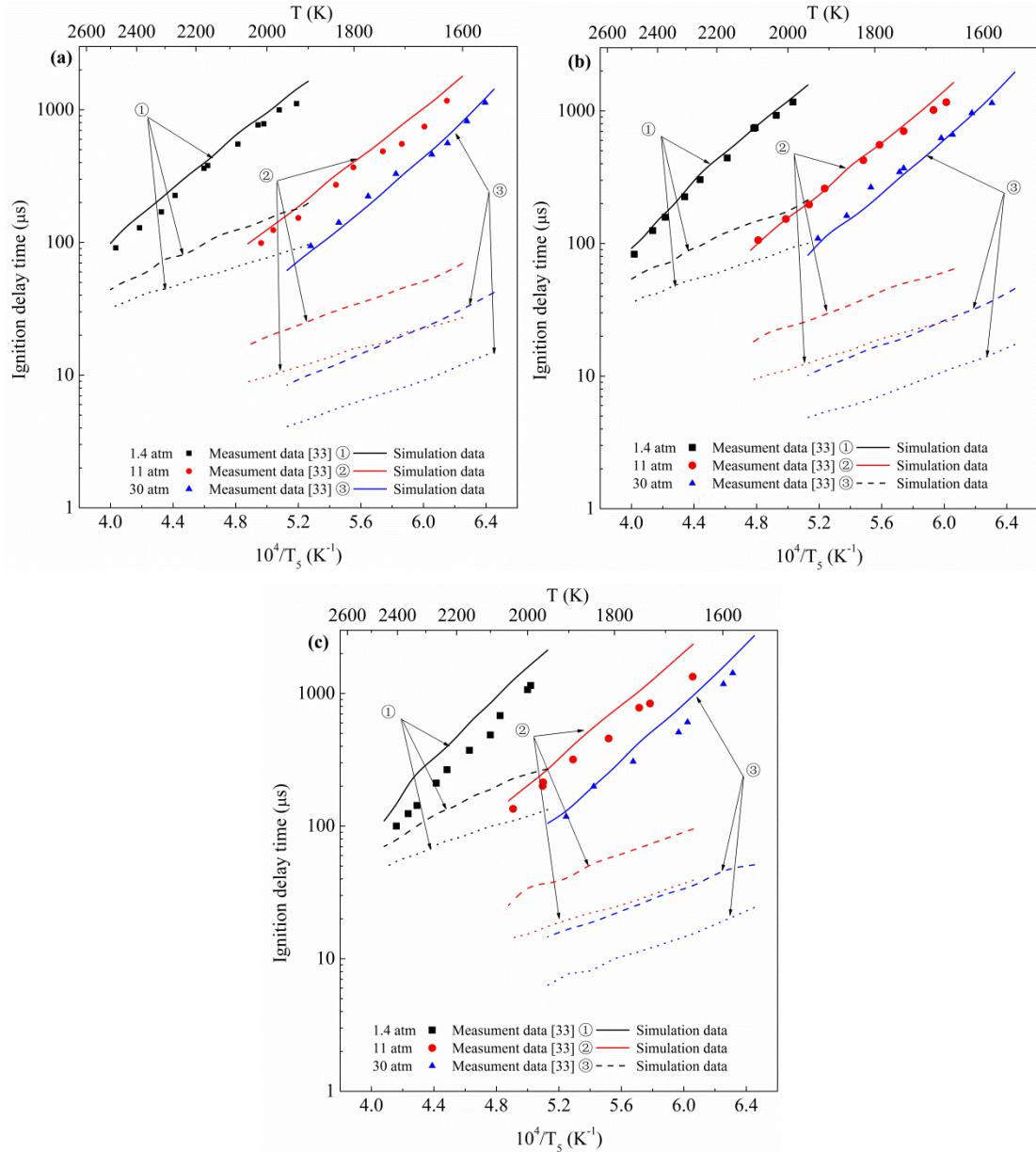
**Fig. 6.** The sensitivitiy analysis of elementary reactions to laminar burning velocity of NH<sub>3</sub>-air flame at various X<sub>H<sub>2</sub></sub> (ϕ=1.0).



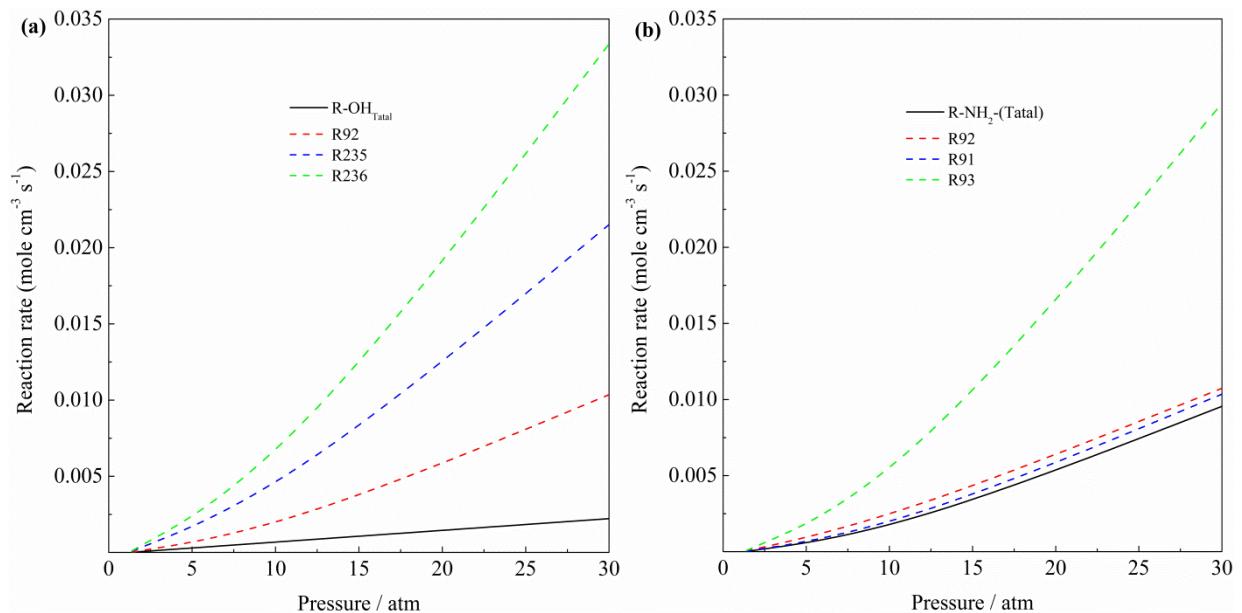
**Fig. 7.** Comparison between experimental and numerical ignition delay times based on  $\text{NH}_2$  radical (Solid line) and OH radical (Dash line) for  $\text{NH}_3\text{-O}_2$  mixture diluted in 99% Ar at various equivalence ratios: (a)  $\phi=0.5$ ; (b)  $\phi=1.0$ ; (c)  $\phi=2.0$ .



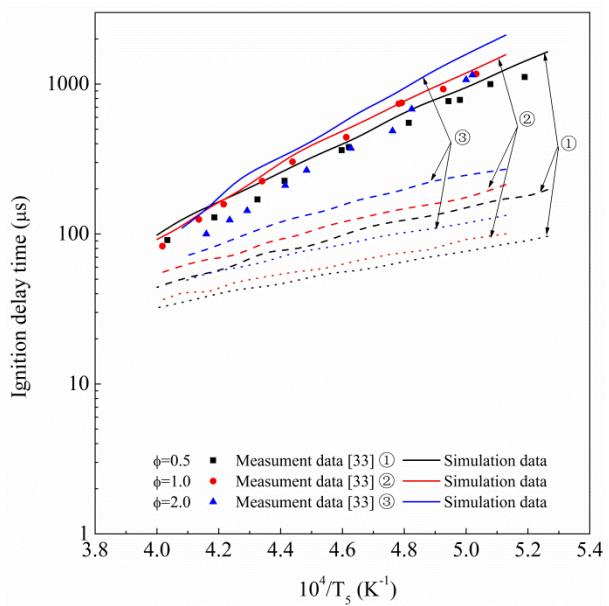
**Fig. 8.** Effect of  $\text{H}_2$  addition on ignition delay times for  $\text{NH}_3\text{-O}_2$  mixture diluted in 99% Ar at various equivalence ratios: (a)  $\phi=0.5$ ; (b)  $\phi=1.0$ ; (c)  $\phi=2.0$ .



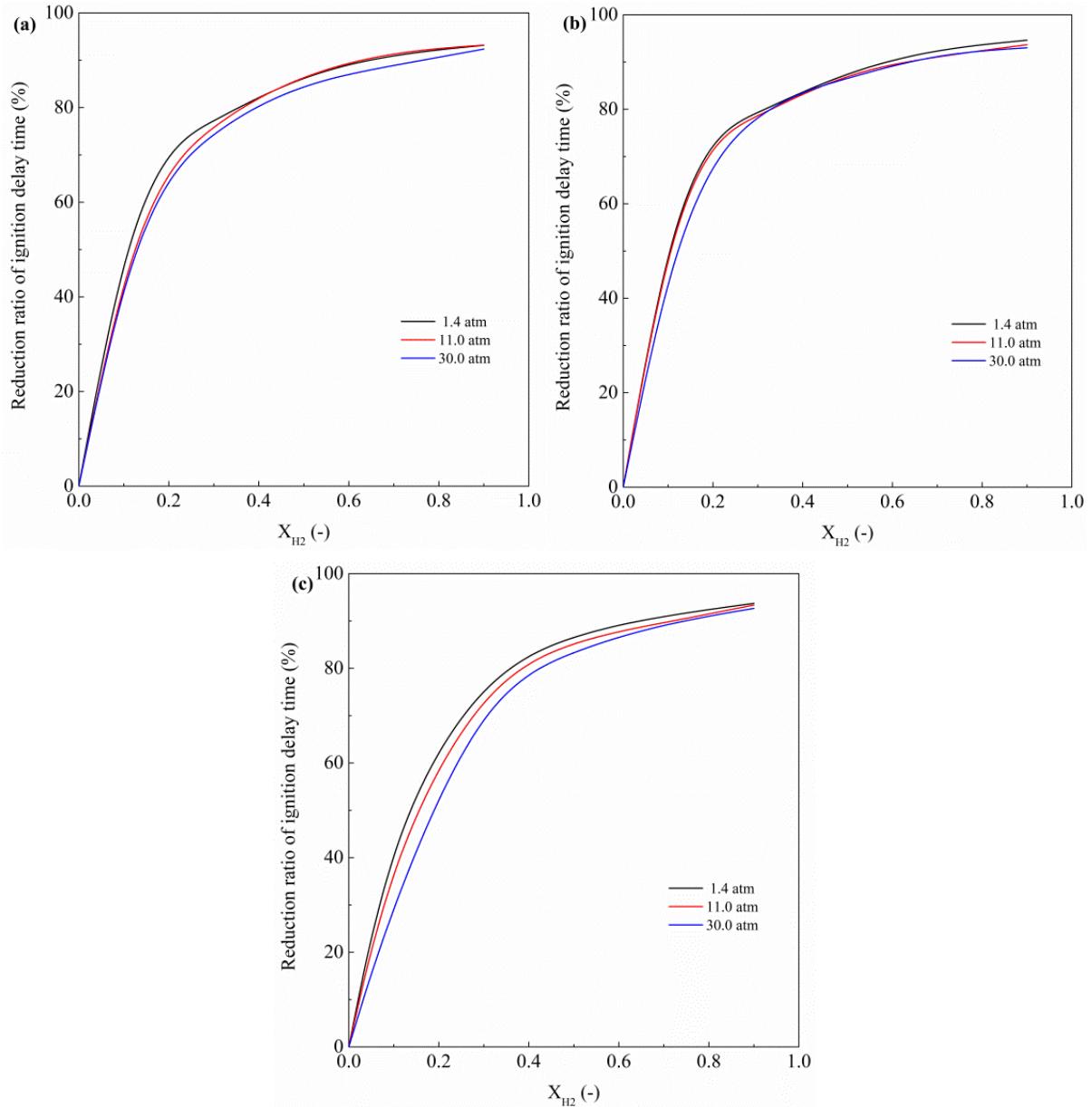
**Fig. 9.** Effect of pressure on ignition delay times for NH<sub>3</sub>-O<sub>2</sub> mixture at H<sub>2</sub> addition ratio of 0 (Solid line), 0.5 (Dash line), and 0.9 (Dot line): (a)  $\phi=0.5$ ; (b)  $\phi=1.0$ ; (c)  $\phi=2.0$ .



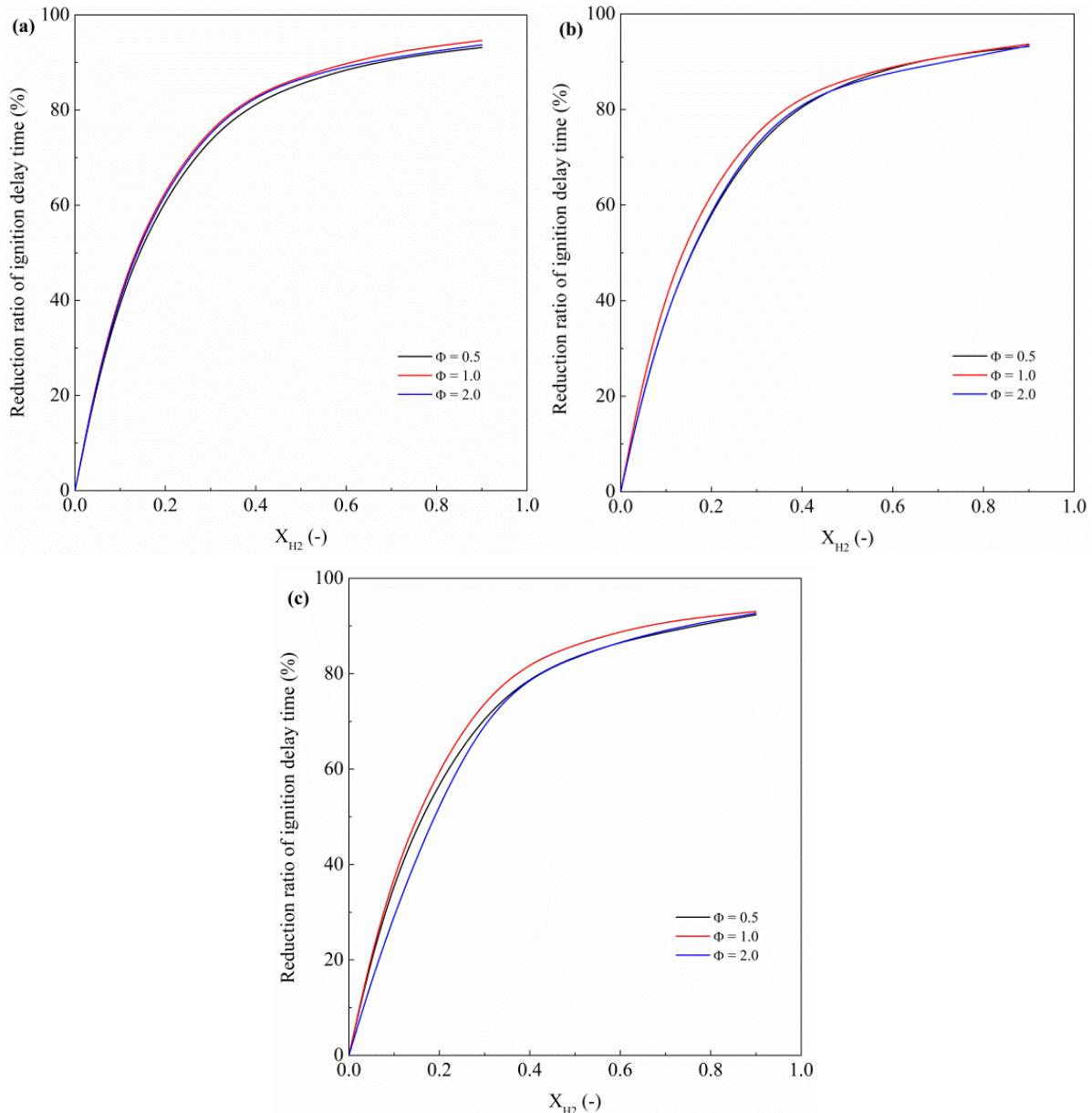
**Fig. 10.** Effect of pressure on total and elementary reaction rate of OH (a) and NH<sub>2</sub> (b) radicals at  $X_{\text{H}_2}$  of 0.5.



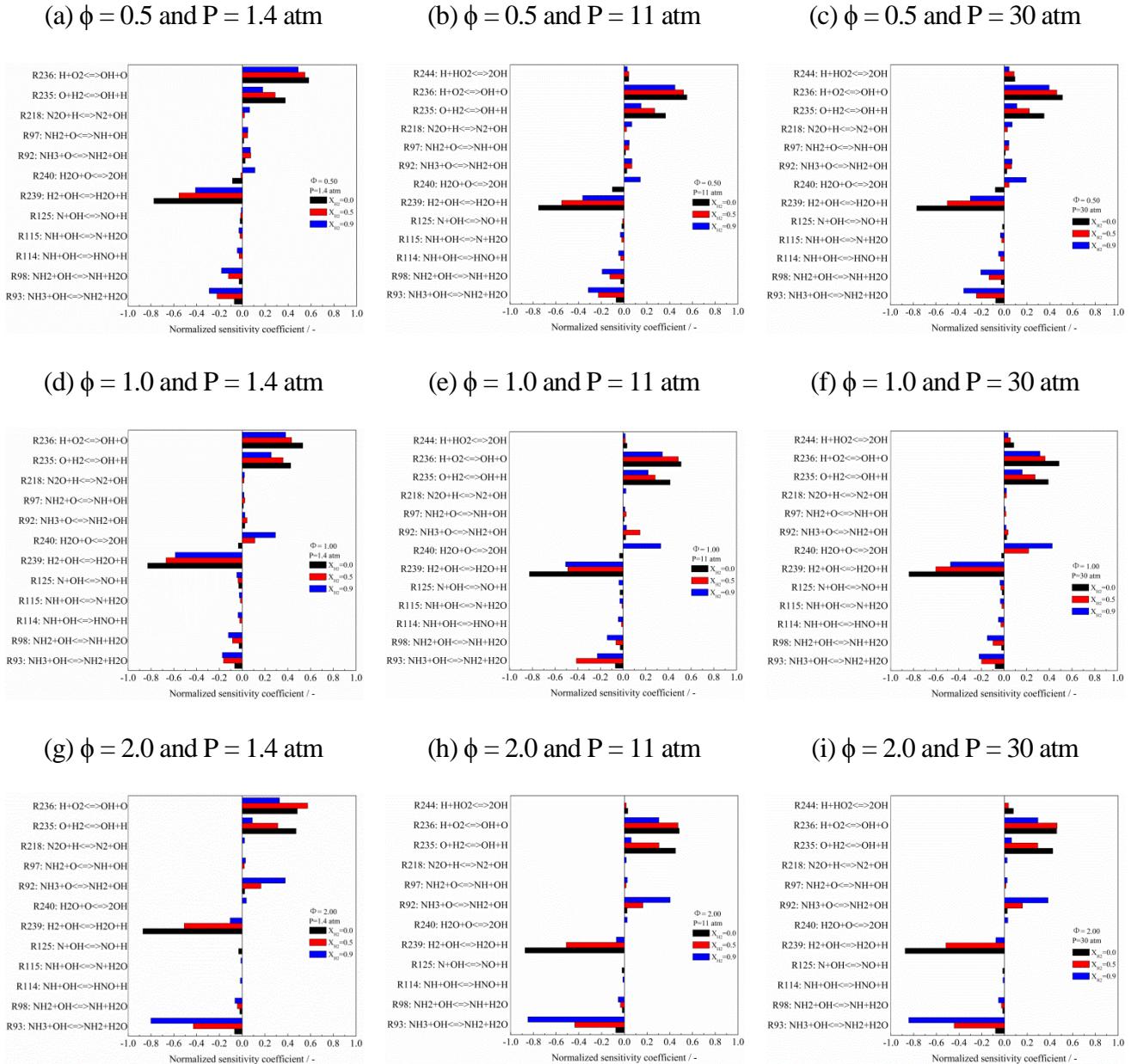
**Fig. 11** Effect of  $\phi$  on ignition delay time for  $\text{NH}_3\text{-O}_2\text{-Ar}$  mixture at pressure of 1.4 atm and various  $\text{H}_2$  addition ratios of 0.0 (Solid line), 0.5 (Dash line), and 0.9 (Dot line).



**Fig. 12** Pressure effect on the reduction ratio of ignition delay time compared to pure NH<sub>3</sub> with various H<sub>2</sub> addition ratios over pressure of 1.4-30 atm at 1950 K: (a)  $\phi = 0.50$ , (b)  $\phi = 1.00$ , (c)  $\phi = 2.0$ .



**Fig. 13** Equivalence ratio effect on the reduction ratio of ignition delay time compared to pure NH<sub>3</sub> with various H<sub>2</sub> addition ratios over pressure of 1.4-30 atm at 1950 K: (a) P = 1.4 atm, (b) P = 11 atm, (c) P = 30 atm.



**Fig. 14** Normalized sensitivity analysis of OH under DK mechanism with H<sub>2</sub> addition ratio of 0.0, 0.5, and 0.9 and  $\phi$  of 0.5: (a)  $P = 1.4$  atm, (b)  $P = 11$  atm, (c)  $P = 30$  atm;  $\phi$  of 1.0: (d)  $P = 1.4$  atm, (e)  $P = 11$  atm, (f)  $P = 30$  atm; and  $\phi$  of 2.0: (g)  $P = 1.4$  atm, (h)  $P = 11$  atm, (i)  $P = 30$  atm.

Appendix files:



Appendix A.rar



Appendix B.rar



Appendix C.rar