Structural Relaxation and Viscoelasticity of a Higher Alcohol with Mesoscopic Structure

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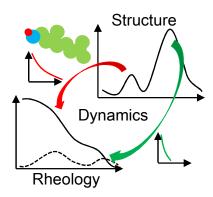
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This work studied the slow dynamics of liquids with mesoscopic structure and its relation to shear viscosity. Quasielastic scattering measurements were made on a liquid higher alcohol, 3,7-dimethyl-1-octanol, using γ -ray time-domain interferometry at a synchrotron radiation facility, SPring-8. The quasielastic scattering spectra were measured to determine the structural relaxation at two wavenumbers of the prepeak and the main peak of the static structure factor. It was found that relaxation at the prepeak is more than 10 times slower than that at the main peak. Compared with the viscoelastic spectrum, which exhibits bimodal relaxation, the relaxations at the prepeak and the main peak were shown to correspond to the slower and faster modes of the viscoelastic relaxation, respectively. This indicates that the dynamics of the mesoscopic structure represented as the prepeak contributes to the shear viscosity through the slowest mode of the viscoelastic relaxation.

TOC GRAPHICS



The properties of liquids with mesoscopic structures have attracted many researchers for a decade. The intermolecular correlation in simple liquids appears at a wavenumber corresponding to the contact distance, usually $10 \text{ nm}^{-1} - 20 \text{ nm}^{-1}$, as a peak of the static structure factor called "the main peak." In some liquids, an additional peak, called a "prepeak" is observed at a wavenumber lower than that of the main peak. The prepeak exhibits the presence of a characteristic mesoscopic structure whose spatial dimension is much larger than the intermolecular contact distance. The prepeak structures have been reported on room-temperature ionic liquids (RTILs)^{1,2,3} and higher alcohols,^{4,5} and they are ascribed to mesoscopic structures composed of polar and nonpolar domains.

The rheology of structured fluids, including surfactant, colloid, and polymer systems, is governed by the dynamics of characteristic mesoscopic structures. On the other hand, the shear viscosity of molecular liquids has been discussed in terms of microscopic liquid structure and intermolecular interactions. The mechanical properties of molecular and structured fluids have thus been studied from quite different points of views so far. Although the RTILs and higher alcohols introduced above belong to molecular liquids, they exhibit a mesoscopic structure that resembles those seen in surfactant solutions. They can thus bridge the rheology of molecular and structured fluids. To unveil the character of structured fluids in RTILs and higher alcohols, we need to evaluate the slow dynamics of the mesoscopic structure and examine its role in viscoelastic relaxation.

In this work, we have chosen a higher alcohol, 3,7-dimethyl-1-octanol, as an example, which has been a target of studies on the dynamics of supercooled liquids.⁶ The branched structure of the alkyl group prevents crystallization, which enables us to determine the dynamics in a wide temperature range.

The mesoscopic structure of the liquid alcohol appears as a prepeak in a small-angle X-ray scattering profile.^{4,5,7} Its dynamics, described in terms of the intermediate scattering function (ISF) at the prepeak, is probed by quasielastic scattering spectroscopies. On the other hand, the dynamics relevant to the shear viscosity is reflected in the viscoelastic relaxation. One of us (Tsuyoshi Yamaguchi) recently showed computationally that the domain dynamics of higher alcohols actually contributes to the shear viscosity through the slowest mode of the viscoelastic relaxation.⁷ We shall demonstrate experimentally in this work that a strong relationship between the domain dynamics and viscoelastic relaxation of higher alcohols exists.

The structural dynamics was determined by means of quasielastic scattering spectroscopy using multiline γ -ray time-domain interferometry.^{8,9,10} Utilizing the γ -rays from the ⁵⁷Fe nucleus excited by synchrotron radiation, which shows a relatively narrow energy width of 4.7 neV, compared with its energy of 14.4 keV, we can measure the slow dynamics of the X-ray ISF in the ns–µs domain. The quasielastic scattering using γ -ray time-domain interferometry was used successfully to study the microscopic slow dynamics of glass-forming systems.^{11,12} The technique was also applied to the study of the slow dynamics of the layered structure of smectic-A liquid crystals.¹³ The viscoelastic spectra were determined in a range 5 MHz – 205 MHz and 238 K – 298 K using shear impedance spectroscopy, which has been applied to a variety of viscous liquids.^{14,15,16,17} The details of the experimental methods are described in Supporting Information.

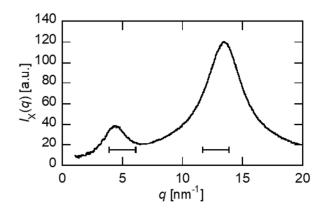


Figure 1. The X-ray structure factor of 3,7-dimethyl-1-octanol at room temperature. The two horizontal bars indicate the *q*-ranges of the measurement of the ISFs.

The X-ray static structure factor of the sample is shown in Fig. 1. A prepeak is found at the wavenumber $q = 4.5 \text{ nm}^{-1}$ in addition to the strong main peak at $q = 13 \text{ nm}^{-1}$, as in the cases of *n*-alcohols.^{4,5} The measurements of the quasielastic scattering were performed at two *q*-ranges, 5.0 $\pm 1.1 \text{ nm}^{-1}$ and $12.8 \pm 1.1 \text{ nm}^{-1}$, covering these two peaks.

The Kohlrausch-Williams-Watts (KWW) functional form,

$$\frac{I(q,t)}{I(q,0)} = f(q) \exp\left[-\left(\frac{t}{\tau(q)}\right)^{\beta(q)}\right],\tag{1}$$

was applied to the ISFs, I(q,t), at both peaks, where t stands for time, and the parameters f, β , and τ are related to the amplitude of the slow relaxation mode, the distribution of the relaxation time, and the relaxation time, respectively. The parameters in eq. 1 were optimized to reproduce the time-domain interference signal. The examples of the raw signals and the fitting curves are presented in Fig. S1 of Supporting Information. The values of β were fixed to be 0.60 and 0.66 for the prepeak and the main peak, respectively, as described in Supporting Information, and the

values of f and τ were optimized. The mean relaxation time, $\langle \tau \rangle$, was evaluated according to eq.

2,

$$\left\langle \tau \right\rangle \equiv \frac{\tau}{\beta} \Gamma \left(\frac{1}{\beta} \right), \tag{2}$$

where $\Gamma(x)$ stands for the gamma function.

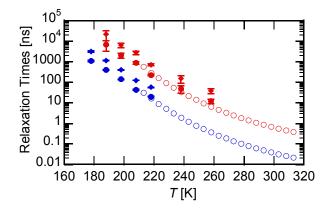


Figure 2. The relaxation times of the prepeak (red filled symbols) and main peak (blue filled symbols) are plotted as a function of temperature. The mean relaxation times of the ISF, $\langle \tau \rangle$ defined by eq. 2, are shown with diamonds, while the mean relaxation times of the squared ISF, $\langle \tau_2 \rangle$ defined by eq. 4, are plotted with circles. They are compared with the relaxation times of the slower (red) and faster (blue) modes of the viscoelastic relaxation, τ_s and τ_f , respectively, plotted with open circles.

The mean relaxation times of the ISFs at both peaks are exhibited in Fig. 2 with the filled diamonds. We succeeded in determining the relaxation times of ISFs at the prepeak in addition to those at the main peak. The structural relaxation at the prepeak is more than 10 times slower

than that at the main peak, and the temperature dependences of the relaxation times at both peaks are similar to each other.

The slower relaxation at the prepeak has been reported in various systems, including RTILs^{18,19} and concentrated electrolyte solutions.¹⁶ In the case of alcohols, Sillrén and coworkers measured the ISFs of liquid 1-propanol at the prepeak and the main peak, and showed that the relaxation at the prepeak is several times slower than that at the main peak.²⁰ Bertrand and coworkers determined the ISFs of liquid methanol using neutron spin echo (NSE) spectroscopy with isotope substitution and also demonstrated that the ISF at the prepeak relaxes several times more slowly.²¹ The molecular dynamics (MD) simulation by one of us showed the slower relaxation at the prepeak in the cases of 1-alcohols, and the separation of the relaxation times at the prepeak increases with lengthening the alkyl chain.⁷ The slow domain dynamics is thus a property of various liquids with prepeak structures, and 3,7-dimethyl-1-octanol follows the trend.

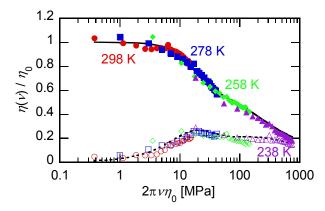


Figure 3. The frequency-dependent complex shear viscosity normalized to the steady-state shear viscosity is plotted against the angular frequency multiplied by the steady-state shear viscosity. The spectra at four different temperatures are shown with different colors, and the correspondence between the color and the temperature is given in the panel. The real and

imaginary parts of the complex spectra are shown with filled and open symbols, respectively. The curve fitting using a Cole–Davidson and a Debye function is shown with the solid (real part) and the dotted (imaginary part) curves, respectively.

The frequency-dependent complex shear viscosity, $\eta(v)$, at four different temperatures is shown in Fig. S2 of Supporting Information. The spectra normalized to the steady-state shear viscosity, η_0 , are plotted in Fig. 3 against the angular frequency multiplied by η_0 . They reduce to a master curve, which indicates that the temperature dependence of the shear viscosity is governed by that of the relaxation time.

As seen in Fig. 3, the normalized spectra appear to be bimodal, with the reduced relaxation frequencies of $2\pi\eta_0 v \sim 20$ MPa and 400 MPa. The bimodal viscoelastic relaxation of higher alcohols was suggested by the combination of the transverse and longitudinal ultrasonic spectroscopies,²² which was later confirmed by MD simulation.⁷ The presence of the bimodal relaxation has also been confirmed in a deeply supercooled region using conventional rheometers.^{23,24,25}

The master curve was approximated by the sum of the Debye and Cole–Davidson functions as

$$\frac{\eta(v)}{\eta_0} = \frac{A}{1 + \frac{2\pi i \eta_0 v}{G_s}} + \frac{1 - A}{\left(1 + \frac{2\pi i \eta_0 v}{G_f}\right)^{\beta_f}},$$
(3)

where the first Debye and the second Cole–Davidson terms describe the slower and the faster relaxation modes, respectively. The relative amplitude of the former is denoted as A, and G_s and G_f are parameters related to the shear moduli of these modes, respectively. The stretch parameter of the Cole-Davidson function is given by β_f . The fitting curve reproduces the

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experimental spectra fairly well, as is shown in Fig. 3. Given the values of G_s and G_f , the relaxation times of the slower and faster modes are evaluated from η_0 as $\tau_s = G_s/\eta_0$ and $\tau_f = G_f/(\beta_f \eta_0)$, respectively.

Mode-coupling theory (MCT) is a theory that can relate the microscopic structural dynamics of liquids to the macroscopic shear viscosity. It describes the viscoelastic relaxation as a superposition of the bilinear product of the ISFs.²⁶ When the dynamics at a particular wavenumber, q^* is dominant in a viscoelastic relaxation mode, MCT predicts that the dynamics of the relaxation mode is proportional to the square of the ISF at q^* . A comparison between the viscoelastic relaxation spectra and the squared ISF at a wavenumber thus provides information on whether the structural dynamics at the wavenumber is related to the shear viscosity. Such a comparison has been made for various viscous liquids, including RTILs, with the prepeak structure.^{14–16}

Provided that the ISF is described by the KWW function, eq. 1, the mean relaxation time of the squared ISF is given by

$$\langle \tau_2 \rangle \equiv \frac{\tau}{2^{\frac{1}{\beta}} \beta} \Gamma \left(\frac{1}{\beta} \right).$$
 (4)

The relaxation times $\langle \tau_2 \rangle$ at the two peaks are plotted as a function of the reciprocal temperature in Fig. 2 as the filled circles, and they are compared with the relaxation times of the viscoelastic spectra, τ_s and τ_f .

As is demonstrated clearly in Fig. 2, the relaxation times $\langle \tau_2 \rangle$ of the prepeak and the main peak agree with those of the slower and faster modes of the viscoelastic relaxation, respectively.

The correspondence between the structural dynamics and the viscoelastic relaxation has been suggested by MD simulation.⁷ The present experimental results support the prediction of the MD simulation. In particular, the mesoscopic dynamics of the domain structure of a higher alcohol is shown to contribute to its shear viscosity through the slower mode of the viscoelastic relaxation.

One may question the difference in the functional forms of the slower mode because the ISF is approximated by the KWW function with $\beta = 0.60$, while the Debye function is used for the slower mode of the viscoelastic relaxation. Given that the qualities of both ISF and the viscoelastic spectra is not sufficiently high to analyze the detailed shape of the relaxation spectra, unfortunately, we limit our discussion simply on the mean relaxation time in this work.

Based on the observation of the bimodal shear relaxation of RTILs and the structural resemblance between RTILs and higher alcohols,²⁷ Cosby and coworkers proposed that the slower modes of the shear relaxation of supercooled higher alcohols^{23–25} are assigned to the slow dynamics of the mesoscopic structure.²⁸ Their assignment on higher alcohols is in harmony with our present experiment and the previous MD simulation.⁷ Sillrén and coworkers compared the relaxation times of ISFs at the main peak and the prepeak of 1-propanol with the shear relaxation time estimated from the steady-state shear viscosity and the high-frequency shear modulus in the supercooled region. They showed that the shear relaxation time corresponds to the relaxation time of ISF at the main peak rather than to that at the prepeak.²⁰ Their comparison was however based on the relaxation time of the ISF itself, <r> in this work, and we consider that the comparison based on the squared ISF will, at least partly, explain the discrepancy between the prepeak dynamics and the viscoelastic relaxation.

Our recent MD simulation demonstrated that the coupling between the shear stress and the prepeak dynamics exists even in the smallest alcohol, methanol. Yamaguchi and Faraone studied the coupling between the shear stress and the prepeak structure by means of MD simulation through the evaluation of the cross-correlation between the shear stress and the transient two-body density. It has been found that the coupling accompanies the alignment of the linear hydrogen-bonding chain of methanol along the expansion axis of the shear deformation.²⁹

The relaxation dynamics of ISF can be probed by various quasielastic scattering experiments whose time window ranges from fs to µs, which corresponds to the MHz–THz frequency domain. On the other hand, the viscoelastic relaxation determined by conventional mechanical rheometers is slower than 10 kHz. The comparison between these two relaxation times thus requires a large extrapolation of the temperature dependence of the relaxation time, which inevitably involves a large ambiguity. We thus believe that ultrasonic measurements in the MHz region are desirable for the determination of viscoelastic properties of liquids for comparison with structural dynamics obtained by quasielastic scattering spectroscopies.

In summary, we determined the structural dynamics of the prepeak of a higher alcohol using quasielastic γ-ray scattering spectroscopy using time-domain interferometry and found that the relaxation dynamics of the mesoscopic domain structure agrees with the slower mode of the viscoelastic relaxation. This indicates that the mesoscopic structure of higher alcohols contributes to the shear viscosity through the slower mode of the viscoelastic relaxation, as was suggested by MD simulation. Provided that the mesoscopic structure of higher alcohols is regarded as a precursor of that of surfactant systems, the shear viscosity of higher alcohols has its origin common to the structural viscosity of surfactant solutions. Further experimental and

theoretical studies will be required for the examination of the applicability of other classes of liquids such as RTILs.

Supporting Information. Experimental details, time-domain interference signals, shear relaxation spectra at various temperatures, and a short review on the relation between the ISF at the prepeak and the viscoelastic relaxation of RTILs (PDF).

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Notes

The authors declare no competing financial interests.

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