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10 **Determination of ^{134}Cs activity by the sum-peak method**
11 **via a well type Ge detector**

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18 **Abstract**

19 The new sum peak method was applied to the samples containing both ^{137}Cs and ^{134}Cs
20 using a well-type HPGe detector. The standard sources containing ^{137}Cs and/or ^{134}Cs were
21 measured via a well-type HPGe detector. The activities estimated by the new sum-peak
22 method agreed with the certified activities of the standard sources. It was proved that the
23 activities of the samples collected around Fukushima Daiichi Nuclear Power Plant can be
24 estimated by the new sum-peak method.

25 **Keywords**

26 sum peak method, radioactivity, ^{134}Cs , ^{137}Cs , well type Ge detector

27 **Introduction**

28 Since in the decay of ^{134}Cs more than ten gamma-rays are emitted in several fast
29 cascades, one should thoroughly pay attention to the true coincidence summing (TCS)
30 effect [1,2]. Especially, the effect is severe for well-type detectors [2,8]. The full energy

31 peak (FEP) counting efficiencies for ^{134}Cs may be decreased by more than a factor of two
32 due to the coincidence summing, in comparison with the efficiencies at the same energies
33 in absence of coincidence effects [2,8]. However, there is a kind of absolute measurement
34 technique using the TCS effect, i.e.; the sum-peak method. The formula of the sum-peak
35 method is as;

$$36 \quad N_0 = \left(\frac{N_1 N_2}{N_{12}} + N_t \right) \bar{w}(0), \quad (1)$$

37 where N_0 is the activity of the source, N_1 and N_2 are the full energy peak count rates, N_{12} is
38 the sum peak count rate, N_t is the total count rate, $\bar{w}(0)$ is the angular correlation factor,
39 and subscripts 1 and 2 refer to the corresponding gamma rays [1,3-5]. For well-type of
40 detectors, the angular correlation is approximately unity. The formula is rigorously valid
41 for nuclides which decay emitting just two photons, 1 and 2, in a fast cascade, thus the
42 sum-peak method is successfully applied to determine the activity of ^{60}Co , ^{22}Na etc. But
43 since the method requires total count rate, N_t , it cannot be applied to sources containing
44 other radionuclides. To overcome the problem, the authors developed the modified sum-
45 peak method [6,7]. In this method, one should measure a sample with several source-to-
46 detector (SD) distances to obtain an extrapolated value. Therefore, it cannot be applied to
47 well-type detectors because sample should be usually positioned in the well of the detector.

48 Our purpose is to determine the activity of objects sampled after the accident of
49 Fukushima Daiichi Nuclear Power Plant (FDNPP) [9]. Especially, small amount of
50 objects like pollen, small plant or animal samples, etc. via a well-type detector. The
51 samples mainly contain both ^{137}Cs and ^{134}Cs . Since the total count rate includes the
52 contribution of both nuclides, the total count rate originated solely from the ^{134}Cs cannot
53 be obtained directly from the measurement data.

54 To solve the problem and to estimate the activity of ^{134}Cs , the total count rate due to ^{134}Cs
55 was estimated as below. The total number of counts originating from ^{137}Cs was guessed
56 from its 662 keV peak counts by measuring a ^{137}Cs mono-nuclide source. By subtracting
57 the contribution of ^{137}Cs from the total counts of the mixed source, the total count rate due
58 to ^{134}Cs can be estimated. Therefore, the sum-peak method can be applied to estimate ^{134}Cs

59 activity. The detail of the calculation is described in the previous article [8]. In this article,
60 we explain the results of application of this method to calculate the activities of real
61 samples collected around the FDNPP.

62 **Theory**

63 The decay scheme of ^{134}Cs is illustrated in Fig. 1, in which the gamma-rays with emission
64 probability below 1% were omitted [10]. We decided to use the main two gamma-rays, 796
65 keV and 605 keV, for our calculation because of the higher emission probabilities than
66 those of the other gamma-rays. The detailed calculation is explained in the previous paper
67 [8]. Equation (2) is used to estimate the activity of a source containing only ^{134}Cs .

$$68 \quad N_0 = \frac{N_{(796)}N_{(605)}}{N_{(796,605)}} + N_t, \quad (2)$$

69 where $N_{(796)}$ and $N_{(605)}$ are the peak count rates of 796 keV and 605 keV gamma-rays,
70 respectively. $N_{(796,605)}$ is the sum peak count rate of 796 keV and 605 keV gamma-rays, and
71 N_t is the total count rate. This is not exactly the sum-peak method, so we call this method
72 the sum-peak-like method. On the other hand, for a source containing both ^{134}Cs and ^{137}Cs ,
73 the following procedure is used to compute the activity. At first, the total count rate
74 originated from ^{137}Cs , $N'_{t(^{137}\text{Cs})}$, is computed using the peak-to-total (P/T) ratio;

$$75 \quad N'_{t(^{137}\text{Cs})} = \frac{N_{(662)}}{P/T_{(^{137}\text{Cs})}}. \quad (3)$$

76 Then the total count rate originated from ^{134}Cs , $N'_{t(^{134}\text{Cs})}$, is computed by subtracting the
77 total count rate originated from ^{137}Cs from the total count rate;

$$78 \quad N'_{t(^{134}\text{Cs})} = N_t - N'_{t(^{137}\text{Cs})}. \quad (4)$$

79 Finally, substituting the total count rate computed by Eq. (4) in Eq. (2), the activity of ^{134}Cs
80 can be computed using the following equation;

81
$$N_0 = \frac{N_{(706)}N_{(605)}}{N_{(796,605)}} + N_{t(^{134}\text{Cs})} \cdot \quad (5)$$

82 We call the method the compensated sum-peak-like method.

83 **Experimental**

84 The well-type HPGe detector (GWL-120230, Ortec) has a sensitive volume of 120 cm³,
85 the well inside diameter and the active depth are 10 mm and 40 mm, respectively. The
86 FWHM was 2 keV at 1333 keV. The gamma ray spectrum ranging from 0 to 2 MeV was
87 converted to 4 kch digital data with an ADC (EASY-MCA-8K, Ortec), which means 0.5
88 keV/ch. The spectrum was analysed using a software (Spectrum Navigator, SEIKO
89 EG&G).

90 The sources, ¹³⁴Cs, ¹³⁷Cs and their mixture, were prepared from the standard solutions
91 calibrated by Japan Radioisotope Association (JRIA). Several microliters of the standard
92 solutions were put into polyethylene tubes and weighed by a precision balance. The
93 certified activity was estimated from the weight of the solution. Then several sources of
94 various volume were prepared by adding into the tubes quantities in the range from 0.5 to
95 2.5 mL from a 100 mM CsCl solution. Six sources containing ¹³⁷Cs, six sources containing
96 ¹³⁴Cs, and ten sources containing both ¹³⁴Cs and ¹³⁷Cs were prepared as listed in Table 1.
97 The schematic diagram of the experiment is illustrated in Fig. 2.

98 The measurement time was determined such as to collect more than 10,000 counts in the
99 1401-keV sum peak of ¹³⁴Cs and the 662-keV peak of ¹³⁷Cs to reduce the statistical
100 uncertainty below 1%. The apparent FEP efficiencies for the 605 keV and 796 keV peaks
101 of ¹³⁴Cs and the 662 keV peak of ¹³⁷Cs were obtained using the prepared sources. The P/T
102 ratios for ¹³⁷Cs were obtained from the sources containing only ¹³⁷Cs as a function of the
103 sample height. The activities of the sources containing solely ¹³⁴Cs were estimated by the
104 sum-peak-like method using Eq. (2). The activities of the sources containing both ¹³⁴Cs
105 and ¹³⁷Cs were estimated by the compensated sum-peak-like method using Eq. (3-5). The
106 estimated activities were compared with the certified activities.

107 Soil sampled on Jun 2016 at 10 km from FDNPP and mouse feces sampled on Oct 2016 at
108 3 km from FDNPP were measured by the relative method and the new method proposed in
109 this study. The estimated activities were compared.

110 **Results and discussion**

111 The energy spectra of ^{134}Cs are illustrated in Fig. 3. A lot of peaks are observed in Fig. 3
112 (a), where the scale of the ordinate is logarithmic. The same spectra with linear scale is
113 illustrated in Fig. 3 (b). Three main peaks, 605 keV, 796 keV and their sum peak are
114 obvious, and the other peaks are negligible. The graph shows one of the proofs for
115 understanding the calculation method using Eq. (2), namely the fact that in the case of well-
116 type measurement the sum peak method can be applied with a good approximation to ^{134}Cs .

117 Table 2 shows the activities of the standard sources containing only ^{134}Cs . The activities
118 estimated by Eq. (2), N_0 , were compared with the certified activities, A_0 . As seen in the
119 table, the estimated activities almost agreed with the certified activities except for the
120 sources higher than 30 mm.

121 Table 3 shows the activities of the standard sources containing both ^{137}Cs and ^{134}Cs . The
122 upper six sources have almost the same activity of ^{137}Cs and ^{134}Cs , but different height.
123 The lower four sources have the same sample height but different ratios of the activities of
124 ^{137}Cs to ^{134}Cs . As seen in the table, the estimated activity agreed well with the certified
125 activity.

126 As seen in Table 4, the activities of the soil and the feces estimated by the compensated
127 sum-peak-like method agreed well with those by the relative method when the activity is
128 higher than 25 Bq. ~~The reasons why the activity of sample with low activity estimated by
129 the compensated sum peak like method is somewhat lower than that estimated by the
130 relative method will be the background of natural radionuclides. For example, natural
131 radionuclides ^{214}Bi emits 609 keV gamma ray, and the HP Ge detector has such peak in
132 background. The gamma ray affect the peak counts of 605 keV gamma ray from ^{134}Cs . To
133 correct enough counts for the sum peak area, the counting time long; 50,000 s for soil #1,~~

134 ~~524,000 s for feces b. And the peak counts for 605 keV area was not so high for low level~~
135 ~~samples. So that the peak counts would be underestimated. We considered that the new~~
136 ~~method should be applied to measure sample with relatively high activity. The reason why~~
137 ~~the activity of samples with low activity estimated by the compensated sum-peak-like~~
138 ~~method is somewhat lower than that estimated by the relative method, is the background~~
139 ~~of natural radionuclides. For example, the natural radionuclide ^{214}Bi emits a low intensity~~
140 ~~gamma-ray (1.3%) of energy 1401.5 keV, which can contribute to the sum peak count rate.~~
141 ~~Thus the denominator in Eq. (5) is increased due to this contribution and the computed~~
142 ~~activity is lower. This background contribution to the sum peak is negligible if the ^{134}Cs~~
143 ~~activity is not very low. But for low activity, when the counting time is very long, 50,000~~
144 ~~s for soil #1, 524,000 s for feces b, this background contribution may have an effect. Thus,~~
145 ~~we consider that the new method should be applied to measure sample with relatively high~~
146 ~~activity.~~

147 Well-type detectors have high efficiency, so that they have a merit to measure small amount
148 of samples. However, the measurements with this detector are considerably affected by the
149 TCS effect [2]. One should carefully correct the TCS effect. The most effective way to
150 avoid the TCS correction is to make measurements with respect to a standard containing
151 the same nuclide, having the same matrix of the sample and the same geometry. But such
152 standards are not always available, or rather expensive. However, if one obtains a sample
153 with relatively high activity, one can estimate the activity using the method proposed in
154 this work. Then one can obtain the apparent relative FEP efficiency using this sample.
155 Samples with relatively low activity can be estimated using the relative measurement with
156 respect to this sample.

157 The sum-peak method does not require standard sources. It can be applied to assess the
158 activity of ^{134}Cs even if another nuclide, like ^{137}Cs , is also present in the sample, by the
159 appropriate subtraction of total number of counts due to that nuclide. The method requires
160 the knowledge of the P/T ratio of ^{137}Cs . However, most laboratory have ^{137}Cs standard
161 sources for frequent calibration of the detectors and can easily obtain the P/T ratio.

162 The activities of the ^{134}Cs standard samples agreed well with the certified activities,
163 depending on the sample height. The height limit is 25 mm. The ^{134}Cs activities of the
164 mixture standard sources agreed well with the certified activity. The method is applicable
165 to samples collected around the FDNPP .

166 **Conclusions**

167 The new calculation techniques; (1) the sum-peak-like method and (2) the compensated
168 sum-peak-like method were proposed and were successfully applied to estimate ^{134}Cs
169 activity via a well-type Ge detector. This method is an approximation and has limitations,
170 but is quite simple and practical.

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200

201 **Table 1** The certified activities of the standard samples

No.	Volume (mL)	Height (mm)	¹³⁷ Cs (Bq)	¹³⁴ Cs A ₀ (Bq)	No.	Volume (mL)	Height (mm)	¹³⁷ Cs (Bq)	¹³⁴ Cs A ₀ (Bq)
#701	0.005	1	507±5	–	#4701	0.005	1	520±5	487±4
#702	0.5	10	455±4	–	#4702	0.5	10	485±5	491±4
#703	1.0	18	423±4	–	#4703	1.0	18	527±5	478±4
#704	1.5	25	594±5	–	#4704	1.5	25	435±4	481±4
#705	2.0	30	456±4	–	#4705	2.0	30	398±4	482±4
#706	2.5	39	515±5	–	#4706	2.5	39	514±5	466±4
#401	0.005	1	–	490±4	#4712	2.5	39	978±8	490±4
#402	0.5	10	–	486±4	#4714	2.5	39	955±8	232±2
#403	1.0	18	–	496±4	#4716	2.5	39	1,020±8	143±1
#404	1.5	25	–	486±4	#4720	2.5	39	1,061±8	94±1
#405	2.0	30	–	488±4	–	–	–	–	–
#406	2.5	39	–	487±4	–	–	–	–	–

Uncertainty (*k*=1)

202

203 **Table 2** The computed activities of the standard sources containing only ¹³⁴Cs

No.	¹³⁴ Cs Certified activity A ₀ (Bq)	¹³⁴ Cs New method N ₀ (Bq)	N ₀ /A ₀ (%)
#401	490±4	475±18	97.0±3.7
#402	486±4	476±18	97.8±3.7
#403	496±4	475±18	95.8±3.7
#404	486±4	462±17	95.1±3.6
#405	488±4	454±17	93.1±3.6
#406	487±4	433±16	88.9±3.4

Uncertainty (*k*=1)

204

205

206 **Table 3** The computed activities of the standard samples containing both ^{137}Cs and ^{134}Cs

Sample No.	^{134}Cs Certified activity A_0 (Bq)	^{134}Cs New method N_0 (Bq)	N_0/A_0 (%)
#4701	487±4	476±19	97.9±3.9
#4702	491±4	479±19	97.6±3.9
#4703	478±4	463±18	96.9±3.8
#4704	481±4	454±18	94.3±3.7
#4705	482±4	459±18	95.1±3.8
#4706	466±4	434±17	93.2±3.7
#4712	490±4	455±18	92.8±3.7
#4714	232±2	224±9	96.3±3.8
#4716	143±1	152±6	106±4
#4720	94±1	94±4	100±4

Uncertainty ($k=1$)

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208 **Table 4** The activities of the soil and the feces

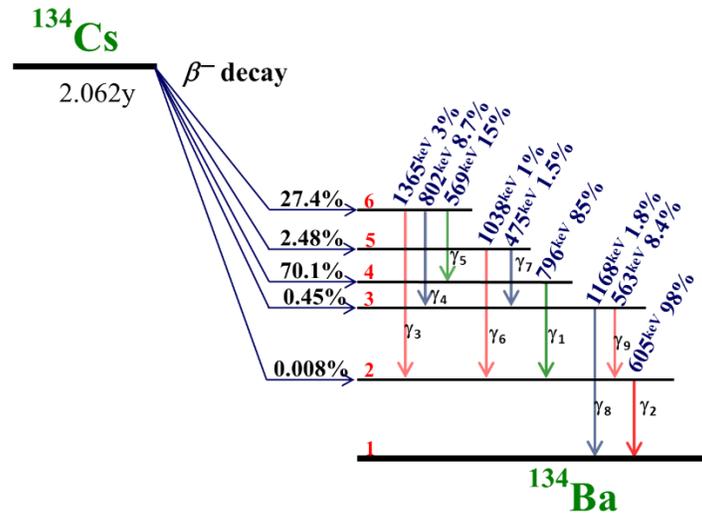
Sample	Height (mm)	Weight (mg)	^{137}Cs by relative method	^{134}Cs by relative method A_0 (Bq)	^{134}Cs by new method N_0 (Bq)	N_0/A_0 (%)
Soil #1	3	4.30	77.2±1.4	10.5±0.2	9.8±0.5	93.4±5.4
Soil #2	4	17.26	318±6	43.3±0.8	45±2	103.1±4.8
Soil #3	4	26.79	484±9	65.8±1.3	68±3	103.7±5.0
Soil #4	4	8.98	187±3	25.4±0.5	26±1	102.2±4.7
Feces a	4	1.20	340±6	46.9±0.9	47±2	100.3±4.4
Feces b	4	1.50	10.5±0.2	1.44±0.03	1.21±0.07	84.4±5.0

Uncertainty ($k=1$)

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Fig. 1 Decay scheme of ¹³⁴Cs

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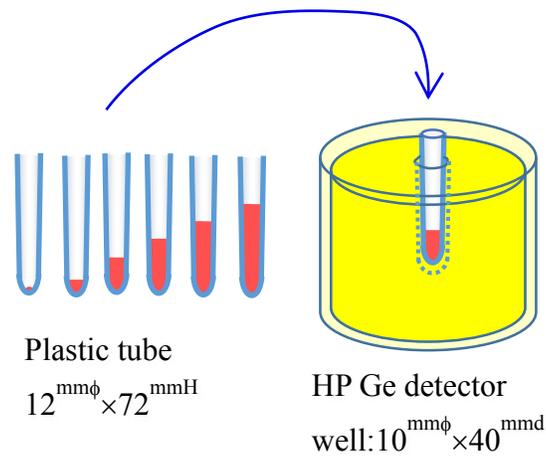


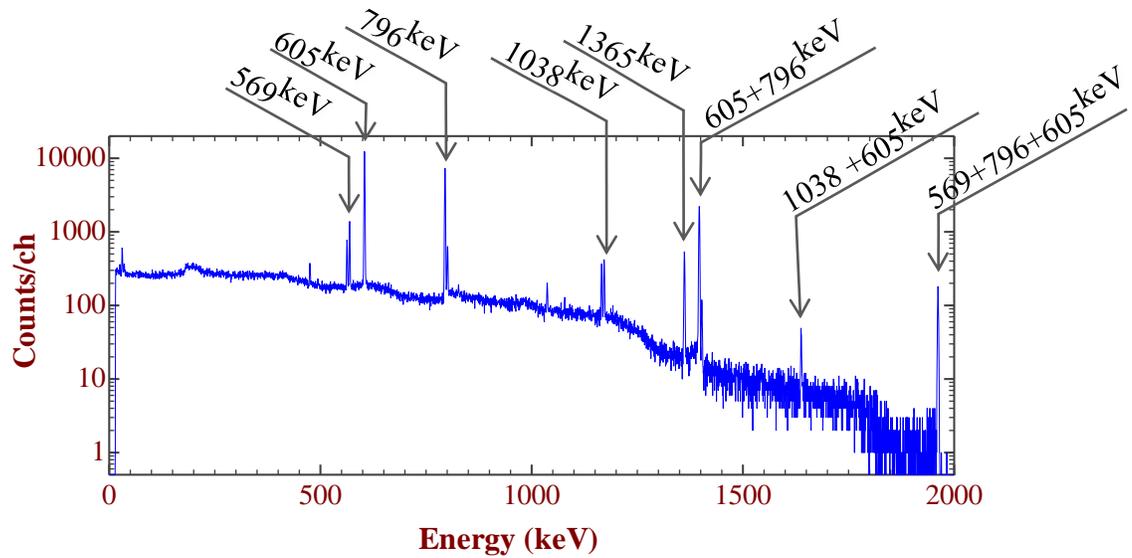
Fig. 2 The schematic diagram of the experiment

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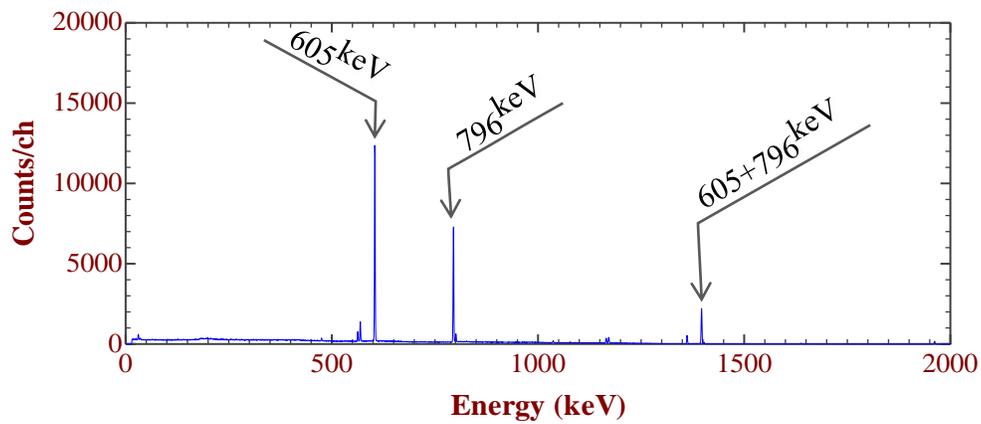
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(a)



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(b)

231 **Fig. 3** Energy spectra of ^{134}Cs ; ordinate with logarithmic scale (a) and that with linear
232 scale (b)

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