## Thermoelectric phase diagram in a CaTiO<sub>3</sub>–SrTiO<sub>3</sub>–BaTiO<sub>3</sub> system

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Herein the authors propose a compositional thermoelectric phase diagram, which includes the density of states effective mass  $(m_d^*)$  carrier relaxation time  $(\tau)$ , and thermoelectric power factor  $(S^2\sigma, \text{ where } S \text{ and } \sigma \text{ are Seebeck coefficient and electrical conductivity})$  for high-quality epitaxial films composed of 20%-Nb-doped CaTiO<sub>3</sub>-SrTiO<sub>3</sub>-BaTiO<sub>3</sub> solid solutions [(Ca,Sr,Ba)  $\times$ (Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>]. The  $m_d^*$  values almost proportionally increase with the in-plane lattice parameter of (Ca,Sr,Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> epitaxial film, while the  $\tau$  values drastically decrease when Ca and/or Ba are substituted for Sr in Sr(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>, indicating that the Sr-site substitution negatively affects the thermoelectric performance of Nb-doped SrTiO<sub>3</sub>. © 2007 American Institute of Physics. [DOI: 10.1063/1.2475878]

Recently, complex metal oxides such as heavily electron-doped SrTiO<sub>3</sub>,<sup>1–3</sup> Na<sub>x</sub>CoO<sub>2</sub> ( $x \sim 0.7$ ),<sup>4,5</sup> and Ca<sub>3</sub>Co<sub>4</sub>O<sub>9</sub> (Refs. 6–8) have attracted much attention for generating thermoelectric power at high temperatures ( $\sim 1000$  K). Although 20%-Nb-doped SrTiO<sub>3</sub> [Sr(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>] (Refs. 9–11) exhibits the largest thermoelectric figure of merit ( $ZT=S^2\sigma T\kappa^{-1}$ , S: Seebeck coefficient,  $\sigma$ : electrical conductivity, T: absolute temperature, and  $\kappa$ : thermal conductivity) among reported *n*-type metal oxides of  $\sim 0.37$  at 1000 K, the performance is insufficient to generate thermoelectric power at high temperatures using waste heat from automobiles and industrial plants.

Muta et al.<sup>12,13</sup> have reported that Sr-site substitution of  $SrTiO_3$  with Ca or Ba may be a good way to improve ZT of Nb-doped SrTiO<sub>3</sub> because these substitutions may efficiently reduce the lattice thermal conductivity due to the fact that alloying scatter phonons if the substitution does not affect the electron transport properties. In order to clarify whether substituting the Sr site in  $Sr(Ti_{0.8}Nb_{0.2})O_3$  affects the electron transport properties, we measured the carrier transport and thermoelectric properties of high-quality epitaxial films of 20%-Nb-doped CaTiO<sub>3</sub>-SrTiO<sub>3</sub>-BaTiO<sub>3</sub> solid solutions [hereafter referred to as (Ca,Sr,Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>] at room temperature (300 K). Consequently, we established a thermoelectric phase diagram for the  $(Ca, Sr, Ba)(Ti_{0.8}Nb_{0.2})O_3$ system. Although the density of states effective mass  $(m_d^*)$ increases almost proportionally with the in-plane lattice parameter of (Ca,Sr,Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> film, the carrier relaxation time ( $\tau$ ) drastically decreases when Ca and/or Ba are substituted for Sr in  $Sr(Ti_{0.8}Nb_{0.2})O_3$ , indicating that Sr-site substitution negatively affects the thermoelectric performance of  $Sr(Ti_{0.8}Nb_{0.2})O_3$ .

Epitaxial films of  $(Ca, Sr, Ba)(Ti_{0.8}Nb_{0.2})O_3$  were grown on the (001) face of a stepped LaAlO<sub>3</sub> substrate<sup>14</sup> at 900 °C by pulsed laser deposition (Pascal) using a KrF excimer laser (Lambda Physik COMPex 102, 20 ns, ~1 J cm<sup>-2</sup> pulse<sup>-1</sup>, 10 Hz) as an ablation light source. Details of our film growth technique have been reported elsewhere.<sup>9,11</sup> Film thickness, crystallographic orientation, and lattice parameters of the resultant films were evaluated by high-resolution x-ray diffraction (HRXRD, Cu  $K\alpha_1$ , ATX-G, Rigaku Co.). The surface morphologies of the films were analyzed by an atomic force microscope (AFM) (Nanoscope E, Digital Instruments).

The resultant films were ~40 nm thick, which were precisely measured by the out-of-plane HRXRD and grazing incidence x-ray reflectivity. Intense streak patterns are observed in the reflection high energy electron diffraction (RHEED) pattern of the films [Fig. 1(a) inset], indicating that the (Ca,Sr,Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films are heteroepitaxially grown on the (001) face of LaAlO<sub>3</sub>, while an epitaxia 1 relationship of (001)[100](Ca,Sr,Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>||(001) ×[100]LaAlO<sub>3</sub> is maintained. Atomically flat terraces and



FIG. 1. (Color online) Crystallographic evaluation of (Ca,Sr,Ba)  $\times$ (Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films. (a) Topographic AFM image of a (Ca<sub>0.4</sub>Sr<sub>0.2</sub>Ba<sub>0.4</sub>)  $\times$ (Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> film with clear atomically flat terraces and steps (~0.4 nm). Typical RHEED pattern of the film with an intense streak pattern is also shown in the inset. (b) RSMs of the 013 diffraction spot for the (Ca,Sr,Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films. Dotted line, which corresponds to cubic lattice ( $q_z/q_x=-3$ ), is also shown.

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FIG. 2. (Color online) Density of states effective mass  $(m_d^*)$  of the  $(Ca, Sr, Ba)(Ti_{0.8}Nb_{0.2})O_3$  films. (a) Compositional mapping of the  $m_d^*$ . The  $m_d^*$  values of the Ca(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>, Sr(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>, and Ba(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films are  $7.8m_0$ ,  $9.8m_0$ , and  $12.1m_0$ , respectively. (b) Plots for the  $m_d^*$  values vs in-plane lattice parameter (a).

steps, which correspond to the unit cell height ( $\sim 0.4$  nm) of (Ca, Sr, Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>, are clearly seen in the topographic AFM image of a (Ca<sub>0.4</sub>Sr<sub>0.2</sub>Ba<sub>0.4</sub>)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> film [Fig. 1(a)]. From these results, we conclude that the film quality is sufficient to evaluate thermoelectric properties.

Figure 1(b) shows the x-ray reciprocal space mappings (RSMs) for the 013 diffraction spot of (Ca,Sr,Ba)  $\times$ (Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films. The dotted line, which corresponds to the cubic lattice  $(q_z/q_x=-3)$ , is also shown. The 013 diffraction spot of Sr(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> film is located on the dotted line, indicating that the crystallographic symmetry of the film is cubic. However, those of (Ca,Sr,Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> and  $(Sr, Ba)(Ti_{0.8}Nb_{0.2})O_3$  films slightly deviate from the dotted line, indicating that Sr-site substitution in  $Sr(Ti_{0.8}Nb_{0.2})O_3$ with Ca and/or Ba induces an asymmetrical lattice expansion.

The carrier concentration  $(n_e)$  and Hall mobility  $(\mu_{\text{Hall}})$ of the (Ca, Sr, Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films were measured by the dc four probe method with a van der Pauw configuration at room temperature.<sup>15</sup> The Seebeck coefficient (S) was mea-



FIG. 3. (Color online) Compositional mapping of (a) Carrier relaxation time ( $\tau$ ) and (b) thermoelectric power factor ( $PF=S^2\sigma$ ) for (Ca,Sr,Ba)  $\times$ (Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films at room temperature.

sured at room temperature by the conventional steady state method and by introducing a temperature gradient in the inplane direction. The  $m_d^*$  value was calculated according to the following equations using the observed  $n_e$  and S values:

$$m_d^* = \frac{h^2}{2k_B T} \left[ \frac{n_e}{4\pi F_{1/2}(\xi)} \right]^{2/3},\tag{1}$$

$$F_{r}(\xi) = \int_{0}^{\infty} \frac{x^{r}}{1 + e^{x - \xi}} dx,$$
(2)

$$S = -\frac{k_B}{e} \left[ \frac{(r+2)F_{r+1}(\xi)}{(r+1)F_r(\xi)} - \xi \right],$$
(3)

where h,  $k_B$ , T (300 K),  $F_r$ ,  $\xi$ , and r are Planck constant, the Boltzmann constant, absolute temperature, Fermi integral, chemical potential, and scattering parameter of relaxation time [0.5 (Ref. 9 and 10)], respectively. Figure 2(a) shows the composition mapping of the  $m_d^*$  values for the (Ca, Sr, Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films.<sup>16</sup> The  $m_d^*$  values of the om temperature.<sup>15</sup> The Seebeck coefficient (S) was mea-Downloaded 20 Sep 2007 to 133.6.32.11. Redistribution subject to AIP license or copyright, see http://apl.aip.org/apl/copyright.jsp

TABLE I. Carrier concentration  $(n_e)$ , Hall mobility  $(\mu_{\text{Hall}})$ , and Seebeck coefficient (*S*) for the  $(\text{Ca}, \text{Sr}, \text{Ba})(\text{Ti}_{0.8}\text{Nb}_{0.2})\text{O}_3$  epitaxial films at room temperature.

A-site comp. of $A(\text{Ti}_{0.8}\text{Nb}_{0.2})\text{O}_3$	$n_e (10^{21} \mathrm{cm}^{-3})$	$\mu_{ m Hall} \ ( m cm^2  V^{-1}  s^{-1})$	S (μV K <sup>-1</sup> )
Ca	1.5	0.33	-147
Ca <sub>0.8</sub> Sr <sub>0.2</sub>	3.2	0.92	-106
Ca <sub>0.5</sub> Sr <sub>0.5</sub>	2.5	1.3	-123
Ca <sub>0.2</sub> Sr <sub>0.8</sub>	3.3	1.3	-111
Sr	3.9	4.9	-108
Sr <sub>0.8</sub> Ba <sub>0.2</sub>	3.0	1.5	-128
Sr <sub>0.5</sub> Ba <sub>0.5</sub>	4.1	0.97	-111
$Sr_{0.2}Ba_{0.8}$	3.0	0.076	-142
Ba	7.2	0.068	-92
Ca <sub>0.8</sub> Sr <sub>0.2</sub> Ba <sub>0.2</sub>	1.7	0.14	-148
Ca <sub>0.2</sub> Sr <sub>0.8</sub> Ba <sub>0.2</sub>	3.1	0.37	-123
Ca <sub>0.2</sub> Sr <sub>0.2</sub> Ba <sub>0.6</sub>	3.0	0.10	-136
Ca <sub>0.4</sub> Sr <sub>0.4</sub> Ba <sub>0.2</sub>	2.6	0.44	-124
Ca <sub>0.4</sub> Sr <sub>0.2</sub> Ba <sub>0.4</sub>	2.5	0.34	-129
Ca <sub>0.2</sub> Sr <sub>0.4</sub> Ba <sub>0.4</sub>	4.0	0.56	-109

films are  $7.8m_0$ ,  $9.8m_0$ , and  $12.1m_0$ , respectively. A nearly linear relationship is clearly seen in the plots of the  $m_d^*$  values as a function of the in-plane lattice parameter (*a*) [Fig. 2(b)]. This clearly indicates that lattice expansion leads to an enhanced  $m_d^*$  because the overlap population of Ti  $3d-t_{2g}$  orbitals decreases with the Ti–Ti distance.

We then calculated the  $\tau$  value of the (Ca,Sr,Ba)  $\times$  (Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films according to the following equation:

$$\tau = \frac{\mu_{\text{Hall}} m_d^*}{e}$$

Figure 3(a) summarizes the calculated  $\tau$  values for the (Ca, Sr, Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films. The  $\tau$  values of Ca(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>, Sr(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub>, and Ba(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films are 1.5, 27.1, and 0.47 fs, respectively. The  $\tau$  value of Sr(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> drastically decreases when the Sr site is substituted with Ca and/or Ba. This decrease may be due to the asymmetrical expansion of the TiO<sub>6</sub> octahedra, which reduces the linearity of the electron conduction paths. A similar compositional phase diagram is obtained in the thermoelectric power factor ( $PF=S^2\sigma$ ) for the (Ca,Sr,Ba) ×(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> films [Fig. 3(b)]. These results indicate that Ca and/or Ba substitution for Sr in Sr(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> negatively affects the thermoelectric performance of

 $Sr(Ti_{0.8}Nb_{0.2})O_3$  because these substitutions seriously reduce  $\sigma$ .

In summary, herein we have proposed a thermoelectric phase diagram for the  $(Ca, Sr, Ba)(Ti_{0.8}Nb_{0.2})O_3$  system. Although the  $m_d^*$  value almost proportionally increases with the in-plane lattice parameter of  $(Ca, Sr, Ba)(Ti_{0.8}Nb_{0.2})O_3$  film, the  $\tau$  value drastically decreases when Sr is substituted by Ca and/or Ba in Sr(Ti\_{0.8}Nb\_{0.2})O\_3, which implies that Sr-site substitution with Ca and/or Ba negatively affects the thermoelectric performance of Sr(Ti\_{0.8}Nb\_{0.2})O\_3. The fact that the solid solution affects the carrier transport properties is useful for the design concept of thermoelectric materials.

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- <sup>1</sup>H. P. R. Frederikse, W. R. Thurber, and W. R. Hosler, Phys. Rev. **134**, A442 (1964).
- <sup>2</sup>T. Caillat, A. Borshchevsky, and J. P. Fleurial, J. Appl. Phys. **80**, 4442 (1996).
- <sup>3</sup>T. Okuda, K. Nakanishi, S. Miyasaka, and Y. Tokura, Phys. Rev. B **63**, 113104 (2001).
- <sup>4</sup>I. Terasaki, Y. Sasago, and K. Uchinokura, Phys. Rev. B **56**, R12685 (1997).
- <sup>5</sup>Y. Wang, N. S. Rogado, R. J. Cava, and N. P. Ong, Nature (London) **423**, 425 (2003).
- <sup>6</sup>R. Funahashi, I. Matsubara, H. Ikuta, T. Takeuchi, U. Mizutani, and S. Sodeoka, Jpn. J. Appl. Phys., Part 2 **39**, L1127 (2000).
- <sup>7</sup>M. Shikano and R. Funahashi, Appl. Phys. Lett. 82, 1851 (2003).
- <sup>8</sup>K. Sugiura, H. Ohta, K. Nomura, M. Hirano, H. Hosono, and K. Koumoto, Appl. Phys. Lett. **89**, 032111 (2006).
- <sup>9</sup>S. Ohta, T. Nomura, H. Ohta, M. Hirano, H. Hosono, and K. Koumoto, Appl. Phys. Lett. **87**, 092108 (2005).
- <sup>10</sup>S. Ohta, T. Nomura, H. Ohta, and K. Koumoto, J. Appl. Phys. **97**, 034106 (2005).
- <sup>11</sup>S. Ohta, H. Ohta, and K. Koumoto, J. Ceram. Soc. Jpn. **97**, 034106 (2005).
- <sup>12</sup>H. Muta, A. Ieda, K. Kurosaki, and S. Yamanaka, Mater. Lett. **58**, 3868 (2004).
- <sup>13</sup>H. Muta, K. Kurosaki, and S. Yamanaka, J. Alloys Compd. 368, 22 (2004).
- <sup>14</sup>T. Ohnishi, K. Takahashi, M. Nakamura, M. Kawasaki, M. Yoshimoto, and H. Koinuma, Appl. Phys. Lett. **74**, 2531 (1999).
- <sup>15</sup>The carrier concentration  $(n_e)$ , Hall mobility  $(\mu_{\text{Hall}})$ , and Seebeck coefficient (*S*) for the (Ca, Sr, Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> epitaxial films at room temperature are summarized in Table I.
- $^{16}$ A single-phase film of (Ca, Ba)(Ti<sub>0.8</sub>Nb<sub>0.2</sub>)O<sub>3</sub> was not obtained possibly because the size difference between Ca<sup>2+</sup> (134 pm) and Ba<sup>2+</sup> (161 pm) suppresses the formation of a homogeneous solid solution.